QCD Theory meets Information Theory

Jesse Thaler



Bay Area Particle Theory Seminar — April 4, 2025

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Returning to My Roots!

Event Generation with GenEvA, version of parton shower/matrix element merging/matching



I was "dissuaded" from pursuing this further by a DOE Reviewer in 2011...

"Ideal" Strategy

Exclusive event generator that reproduces the results of any inclusive measurement function to the calculated accuracy.

> $N^{i}LO$: $O(\alpha_{s^{i}})$ beyond Born Level N^jLL : Resummation of $\alpha_s^n \log^{2n-j} r$ terms (r is ratio of kinematic scales)

Fully hadronized events (exclusive) using best perturbative calculations (inclusive).

MC@NLO is a concrete example in this direction for NLO/LL calculations (see also POWHEG)

[slides from my 2008 talk; Bauer, Tackmann, JDT, JHEP 2008a, JHEP 2008b]

Returning to My Roots!

Event Generation with GenEvA, version of parton shower/matrix element merging/matching



Can these be merged with showers that go to NLL accuracy or beyond leading color (e.g. PanScales, Deductor)?

Non-perturbative corrections? "Proper" theory systematics?

[from Campbell, Diefenthaler, Hobbs, Höche, Isaacson, Kling, Mrenna, Reuter, et al., Snowmass 2022]

Now NNLO+PS matching with GENEVA (and NNLOPS, MiNNLO_{PS}, TOMTE, ...)!

[slides from my 2008 talk; Bauer, Tackmann, JDT, JHEP 2008a, JHEP 2008b]

Today: Theory Synthesis from "Thinking like a Machine"



Instead of treating parton shower/matrix element merging/ matching as a domain-specific problem in QCD, we can treat it as a generic problem in information theory

Remarkably, this will reveal a new understanding about the difference between fixed-order and resummed calculations, as captured by ordinary versus logarithmic moments

Possibility that this approach could dramatically simplify the experiment/theory interface for precision predictions









QCD Theory meets Information Theory



Colloquium Version of the Story

When physicists "think like a machine", we can translate thorny theoretical challenges into optimization problems



Basics of ML and Information Theory

We can leverage the flexibility of loss functions to learn and constrain physically meaningful moments of distributions



Logarithmic Moments and QCD

Logarithmic moments are particularly powerful probes of QCD that distinguish resummed from fixed-order calculations





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The NSF Institute for Artificial Intelligence and Fundamental Interactions (IAIFI /aI-faI/ iaifi.org)

Launched August 2020

Deep Learning (AI) + Deep Thinking (Physics)

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Deeper Understanding





Learning through dynamical systems, power of statistical reasoning, broad implications for scientific discovery

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Restricted Boltzmann Machine



[discussed at IAIFI Fireside Chat]

Lessons from the HEP + ML Collision

To meet the standards of scientific rigor and performance, we need to teach machines to "Think like a Physicist"

E.g.: symmetries, robustness to systematics, exactness guarantees, statistical inference, ...

But to fully capitalize on AI technologies, we also need to teach physicists to "Think like a Machine"

E.g.: computational complexity, reframing via optimization/search, algorithmic reasoning, ...

The Power of "Centaur Science"

Progress in computation and information theory has long been intertwined with progress in the physical sciences (e.g. statistical mechanics, quantum computers)





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JOEDATOR

[Joe Dator, The New Yorker 2025; h/t Kyle Cranmer]

Danger of "Thinking Like a Machine"?

Position: Is machine learning good or bad for the natural sciences?

Abstract

Machine learning (ML) methods are having a huge impact across all of the sciences. However, ML has a strong ontology—in which only the data exist—and a strong epistemology—in which a model is considered good if it performs well on held-out training data. These philosophies are in strong conflict with both standard practices and key philosophies in the natural sciences.

My attempt at a cartoon summary:

What "exists"? What is "success"? Machine Learning Data Accurate Modeling

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An inspiring/infuriating paper!

Natural Sciences Latent Structures Understanding

[Hogg, Villar, PMLR 2024]

A Generative Model to Mimic the LHC?



What if you could generate synthetic LHC collisions that were indistinguishable from real LHC data? [extreme extrapolation of Butter, Diefenbacher, Kasieczka, Nachman, Plehn, Shih, Winterhalder, SciPost 2022]

According to Hogg/Villar, this conflicts with the epistemology of natural science...

What if you could generate synthetic LHC collisions based entirely on first-principles QFT calculations?

[aspirational goal in Campbell, Diefenthaler, Hobbs, Hoeche, Isaacson, Kling, Mrenna, Reuter, et al., Snowmass 2022]

Amazing if you had it! But we are nowhere near being able to do this...

Centaur Science:

Combine models of LHC data for the full phase space with first-principles predictions whenever available



Taking Inspiration from Boltzmann (Machines)



Boltzmann Machine: Generative model that samples according to a statistical distribution

$$P(\mathbf{s}) \propto e^{-E/T}$$
 $E = -\sum_{i < j} w_{ij} s_i s_j - \sum_i e^{-E/T}$

Boltzmann Factor: Maximum entropy solution subject to constraint on average energy







 $\theta_i S_i$

[Fahlman, Hinton, Sejnowski, AAAI 1983; Ackley, Hinton, Sejnowski, Cogn. Sci. 1985; Boltzmann 1877]

QCD Theory meets Information Theory

Plucking a random QCD calculation:

[e.g. Larkoski, Salam, JDT, IHEP 2013; based on Banfi, Salam, Zanderighi, IHEP 2005]

$$\Sigma(e^{-L}) = N \frac{e^{-\gamma_E R'}}{\Gamma(1+R')} e^{-R} \qquad R = \frac{\alpha_s}{\pi} \frac{C}{\beta} (L+B)^2 \qquad L \equiv \ln \frac{R_0^{\beta}}{C_1^{(\beta)}}$$

Sudakov Form Factor

To a QCD theorist, this is a (simplified) next-to-leading-logarithmic calculation To an ML practitioner, this is an opportunity for neurosymbolic learning

To a Centaur Scientist, the Sudakov form factor is a kind of Boltzmann factor, where the cusp anomalous dimension is like a Lagrange multiplier that enforces a constraint on the second logarithmic moment of the distribution

To my knowledge, logarithmic moments have never been measured or calculated before in QCD!



Proof-of-Concept Study with "Thrust"

First QCD Calculation of Thrust Logarithmic Moments!







see related moment construction in Desai, Nachman, JDT, PRD 2024]

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Priors from imperfect generators yield consistent results after moment reweighting!

[Assi, Lee, Höche, JDT, arXiv 2025; see Sudakov safety in Larkoski, Marzani, JDT, PRD 2015;









Centaur science continuing the tradition of relating properties of physical systems to concepts in computation/information theory

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Machine Learning 101: Likelihood Ratio Trick

Key example of simulation-based inference

Estimate p(x) / q(x)Goal: Finite samples P and Q Training Data: Learnable Function: f(x) parametrized by, e.g., neural networks

 $L = -\left\langle \log f(x) \right\rangle_{\mathbf{P}} + \left\langle f(x) - 1 \right\rangle_{\mathbf{Q}}$ Loss Function(al):

Many HEP problems can be expressed in this form!





[see e.g. Cranmer, Pavez, Louppe, arXiv 2015; D'Agnolo, Wulzer, PRD 2019; simulation-based inference in Cranmer, Brehmer, Louppe, PNAS 2020; relation to f-divergences in Nguyen, Wainwright, Jordan, AoS 2009; Nachman, JDT, PRD 2021]

Machine Learning 101: Likelihood Ratio Trick

Key example of simulation-based inference

Goal:Estimate p(x) / q(x)Training Data:Finite samples P and QLearnable Function:f(x) parametrized by, e.g., neural networks

Loss Function(al):
$$L = - \langle \log f(x) \rangle_{P} + \langle f(x) - dx \rangle_{P}$$

Asymptotically: $\begin{array}{ll} \operatorname{arg\,min} L = \frac{p(x)}{q(x)} \\ f(x) & f(x) \\ -\min_{f(x)} L = \int \mathrm{d}x \, p(x) \log \frac{p(x)}{q(x)} \end{array}$

Likelihood ratio

Kullback–Leibler divergence

[see e.g. Cranmer, Pavez, Louppe, <u>arXiv 2015</u>; D'Agnolo, Wulzer, <u>PRD 2019</u>; simulation-based inference in Cranmer, Brehmer, Louppe, <u>PNAS 2020</u>; relation to f-divergences in Nguyen, Wainwright, Jordan, <u>AoS 2009</u>; Nachman, JDT, <u>PRD 2021</u>]

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Many HEP problems can be expressed in this form!



Machine Learning 101: Likelihood Ratio Trick

Key example of simulation-based inference

Asymptotically, same structure as Lagrangian mechanics!

Action:
$$L = \int \mathrm{d}x \,\mathcal{L}(x)$$

Lagrangian:
$$\mathcal{L}(x) = -p(x)\log f(x) + q(x)(f(x)) -$$

Euler-Lagrange:
$$\frac{\partial \mathcal{L}}{\partial f} = 0$$
 Solution: $f(x) = \frac{p(x)}{q(x)}$

Requires shift in focus from solving problems to specifying problems

[see e.g. Cranmer, Pavez, Louppe, arXiv 2015; D'Agnolo, Wulzer, PRD 2019; simulation-based inference in Cranmer, Brehmer, Louppe, PNAS 2020; relation to f-divergences in Nguyen, Wainwright, Jordan, AoS 2009; Nachman, JDT, PRD 2021]

Many HEP problems can be expressed in this form!



Applications of Likelihood Ratio Trick

Detector Unfolding



[Andreassen, Komiske, Metodiev, Nachman, JDT, <u>PRL 2020;</u> + Suresh, <u>ICLR SimDL 2021</u>]

Monte Carlo Reweighting



[Nachman, JDT, <u>PRD 2020</u>; inspired by Andersen, Gutschow, Maier, Prestel, <u>EPJC 2020</u>]

Theme: Convert sampled data into usable function approximation

Important subtlety (not for this talk): How do you quantify the accuracy/uncertainty of your approximation?

Resolution Estimation



[Gambhir, Nachman, JDT, PRL 2022, PRD 2022]

Recent Example: Rediscovering the Upsilon (Y $\rightarrow \mu^+\mu^-$)

Classification of observed data in signal region versus background interpolation from sidebands



Leverage relation to likelihood ratio to enhance sensitivity beyond simple cuts

[Gambhir, Mastandrea, Nachman, IDT, arXiv 2025; using CATHODE in Hallin, Isaacson, Kasieczka, Krause, Nachman, Quadfasel, Schlaffer, Shih, Sommerhalder, PRD 2022







Information Theory and Optimization

"Predicting" a distribution by maximizing entropy

Shannon Entropy:
$$H(X) = \sum_{i=1}^{n} p(x_i) \log \frac{1}{p(x_i)}$$

Continuum Version

Relative Entropy:
$$-D_{\mathrm{KL}}(P\|Q) = \int dx \, p(x) \log rac{q(x)}{p(x)}$$
 - (KL divergence we saw before)

Extremum:
$$p(x) = e^{-\beta_0} q(x) \qquad \beta_0 = 0 \qquad \Longrightarrow$$

Maximizing (unconstrained) entropy is equivalent to choosing a prior

Maximum:
$$p(x_i) = rac{1}{n}$$

 $+ (\beta_0 - 1) \left(1 - \int dx \, p(x) \right)$

Lagrange Multiplier to enforce normalization

p(x) = q(x)

Information Theory and Constrained Optimization

"Predicting" a distribution by maximizing entropy with fixed moments

Relative Entropy:
$$-D_{ ext{KL}}(P\|Q) = \int dx \, p(x) \log rac{q(x)}{p(x)}$$
 -

Plus Moment Constraints:



Same manipulation as Boltzmann's approach to statistical mechanics! Lagrange multipliers set to values that satisfy constraints

 $+ (\beta_0 - 1) \left(1 - \int dx \, p(x) \right)$

 $+\sum_{j}\beta_{j}\left(c_{j}-\int dx\,p(x)f_{j}(x)\right)$

Information Theory and Numerical Constrained Optimization "Predicting" a distribution by maximizing entropy with fixed moments and auto-differentiation

Extremum:
$$p(x) = \exp\left[-\beta_0(x) - \sum_j \beta_j(x)\right]$$

Target Moment:

Loss Function:
$$\mathcal{L} = \sum_{j} \left(\frac{c_j - d_j}{c_j + d_j} \right)^2$$

Numerically minimize loss to estimate Lagrange multipliers As long as they aren't strictly incompatible, works for any set of basis functions

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 $(x) f_j(x) \mid q(x)$

 c_j Current Moment: $d_j = \int dx \, p(x) \, f_j(x)$

Alternative: Information Theory and Adversarial Networks



Reversing likelihood ratio trick, you can "integrate in" discriminator (d) to turn entropy minimization to adversarial optimization of weight function (g)





lesse Thaler (MIT, IAIFI) — QCD Theory meets Information Theory Iet Width: Particle Level Histograms





Machine learning provides a bridge between well-established statistical methodologies and sampled data in particle physics (and beyond)

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Returning to Proof-of-Concept Study with "Thrust"

First QCD Calculation of Thrust Logarithmic Moments!

Priors from imperfect generators yield consistent results after moment reweighting!





see related moment construction in Desai, Nachman, JDT, PRD 2024]

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[Assi, Lee, Höche, JDT, arXiv 2025; see Sudakov safety in Larkoski, Marzani, JDT, PRD 2015;







Pushing the Precision Frontier

Comparison to LEP Data

Impact on Complementary Observables



Broadening \simeq Thrust







Thrust moments improve predictions for dijet kinematics









Pushing the Precision Frontier

By pattern matching, we drew an analogy between Sudakov form factors and Boltzmann factors. which motivated calculation of logarithmic moments

How can we understand the importance of logarithmic moments directly from QCD perspective?

[Assi, Lee, Höche, JDT, arXiv 2025









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Aside I: Computational Complexity as Muse



Jets with Anti-k_T: O(M log M) vs. O(M³) to cluster M particles

[Cacciari, Salam, Soyez, JHEP 2008]





[Figure from Buhmann, et al., <u>arXiv 2023;</u> based on Buhmann, Kasieczka, JDT, <u>SciPost 2023</u>] O(M) vs. $O(M^4)$ Jet Classification



When you are trying to make sub-microsecond decisions, polynomial speedups can open up new scientific vistas!

1000x Faster Optimal Transport



[Gambhir, Larkoski, JDT, JHEP 2024]

Faster Computation for Better Science

Example outside of ML: Energy correlators

Probing the QCD Phase Transition



Old method (dashed): $O(M^N)$ New method (solid): $O(M^2 \log M) \forall N$

[Alipour-fard, Budhraja, JDT, Waalewijn, arXiv 2024; [variant of Basham, Brown, Ellis, Love, PRL 1978; see also Komiske, Moult, JDT, Zhu, PRL 2022]

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Algorithmic Advances inspire **Enhanced Visualizations!**

Both are $O(M^3)$ but new method isolates distinct physics effects







AK5 Jets, $|\eta\rangle$

 $p_T^{\text{jet}} \in [500, 500]$

CMS Op

Aside 2: Collider Physics meets Optimal Transport

E.g. Thrust: how dijet-like is an event?



(using β =2 EMD variant)









[Cesarotti, JDT, JHEP 2020; ATLAS, JHEP 2023; see also Cesarotti, Reece, Strassler, JHEP 2021] [generalizations in Ba, Dogra, Gambhir, Tasissa, JDT, JHEP 2023; Gambhir, Larkoski, JDT, JHEP 2024]





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Lies, Damned Lies, and Statistics

Problem of Moments (in I-D): $d_j = \int dx \, p(x) \, x^j$ $j \in \{1, 2, 3, \ldots\}$

Given infinite set of moments, reconstruct the underlying distribution

For physics applications, this is rarely the right question to ask

E.g. Cauchy
$$p(x; x_0, \gamma) = \frac{1}{\pi} \frac{\gamma}{(x - x_0)^2 + \gamma^2}$$

Famously, this has no mean (or higher moments), even though it is "obvious" that $\langle x \rangle$ should be x_0



Lies, Damned Lies, and Statistics

More relevant question: Given a probability distribution, what summary statistics best capture the key physical properties?



Calculating Thrust

Extracting strong coupling constant from QCD event shapes



Simplified Thrust Calculation

Leading log at fixed coupling

Sudakov Form Factor

$$p(\tau) = \frac{-2\alpha_s C_F}{\pi} \frac{\ln \tau}{\tau} \exp\left[-\frac{\alpha_s C_F}{\pi} \ln^2 \tau\right]$$

Ordinary Moments

$$\langle \tau^m \rangle = \frac{2\alpha_s C_F}{\pi} \frac{1}{m^2} + \mathcal{O}(\alpha_s^2) \qquad \quad \langle \ln^n \tau \rangle = (-1)^n \left(\frac{\pi}{\alpha_s C_F}\right)^{n/2} \Gamma \left[1 + \frac{n}{2}\right]$$

Example of "Sudakov Safe" Observable

[Assi, Lee, Höche, JDT, <u>arXiv 2025;</u> Sudakov safety in Larkoski, Marzani, JDT, <u>PRD 2015]</u>

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Logarithmic Moments







Simplified Thrust Calculation

Leading log at fixed coupling

Sudakov Form Factor

$$p(\tau) = \frac{-2\alpha_s C_F}{\pi} \frac{\ln \tau}{\tau} \exp\left[-\frac{\alpha_s C}{\pi}\right]$$



 $\frac{F}{2} \ln^2 \tau$

Logarithmic Mean \Rightarrow Sudakov Peak

$$\rangle = -\frac{\pi}{2\sqrt{\alpha_s C_F}}$$

Characterizes Resummed Information

[Assi, Lee, Höche, JDT, arXiv 2025; Sudakov safety in Larkoski, Marzani, JDT, PRD 2015]







Many QCD Subtleties to Incorporate and Understand

For Thrust Specifically:

Sudakov Shoulder Resummation Three Jet Power Corrections Shape Function Parametrization

In General: **Choice of Priors Estimating Theory Uncertainties Non-Perturbative Corrections Treatment of Mixed Moments** Convergence of Moment Expansion

Future Directions: **Multi-differential Distributions Alternative Basis Functions**

Inclusive Observables (e.g. EECs)

- [see Tackmann, arXiv 2024]



Different summary statistics capture different physical effects, and logarithmic moments offer important insights into QCD resummation

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