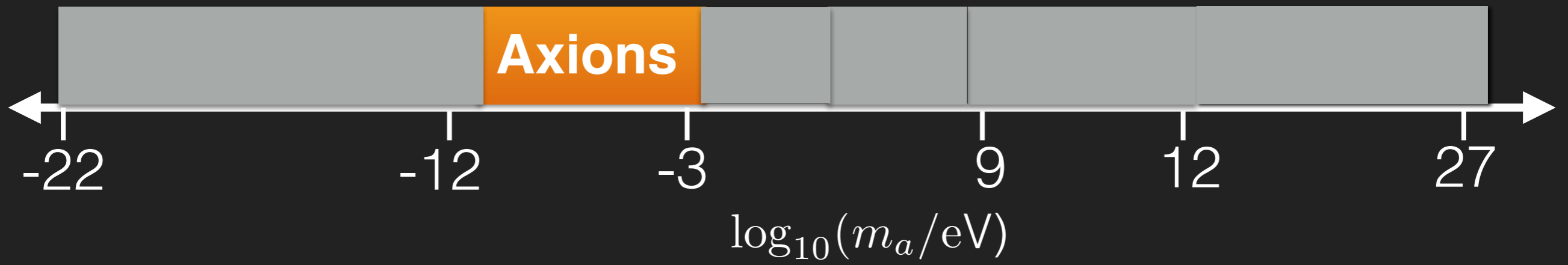


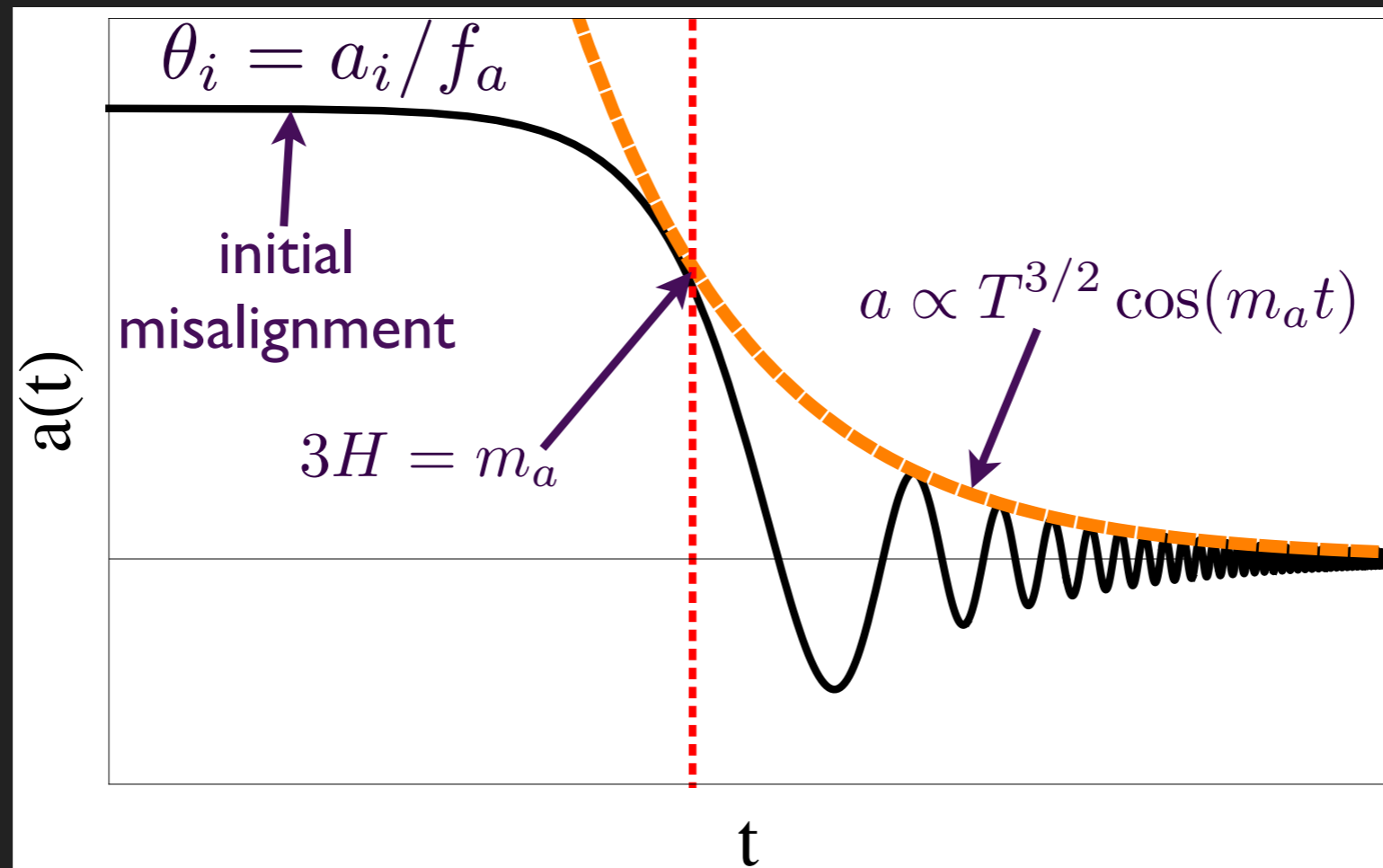
# THE QCD AXION MASS

**BEN SAFDI**

**BERKELEY CENTER FOR THEORETICAL PHYSICS  
UNIVERSITY OF CALIFORNIA, BERKELEY**



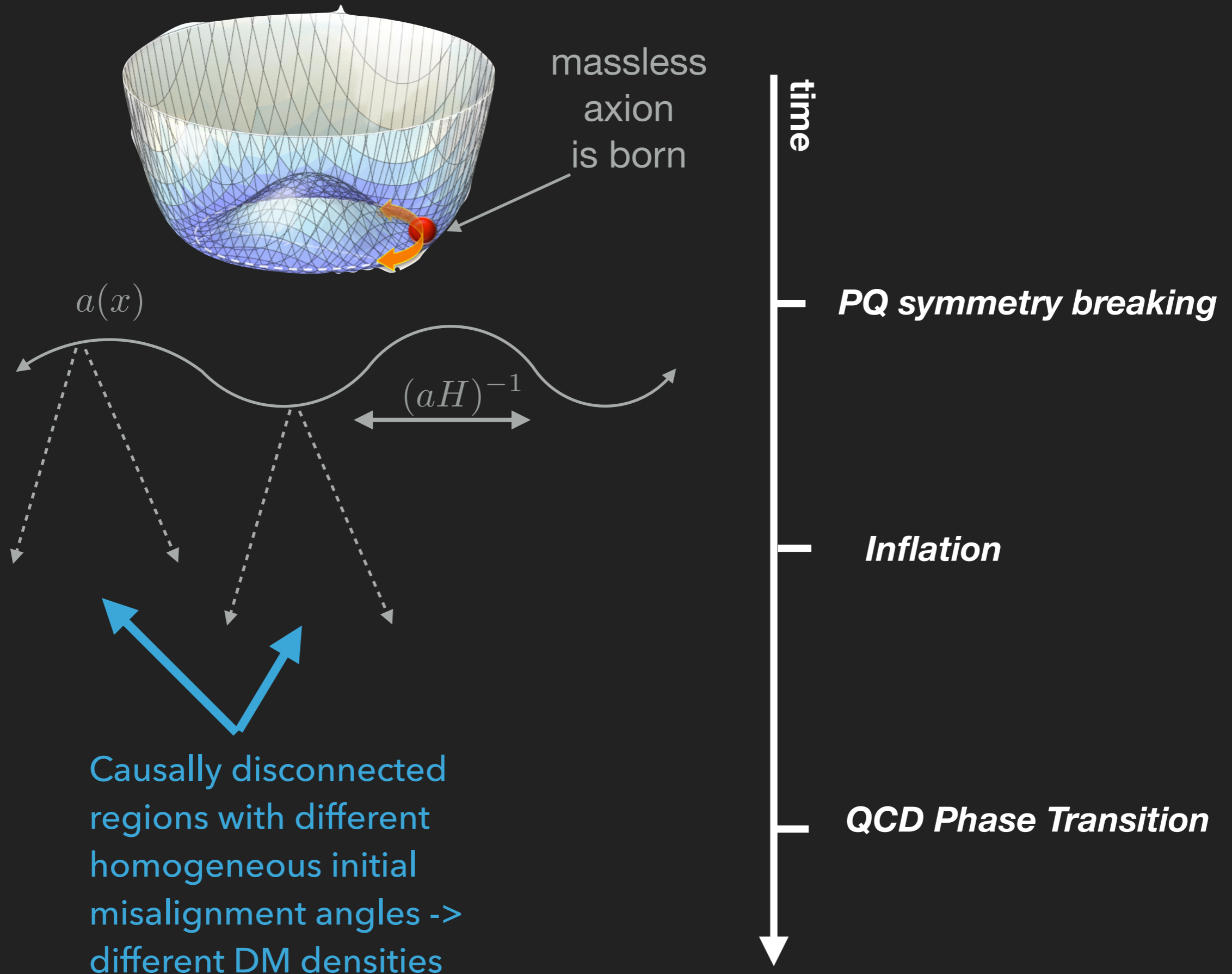
$$\sin a/f_a \sim a/f_a : \quad \ddot{a} + 3H\dot{a} + m_a^2 a = 0$$



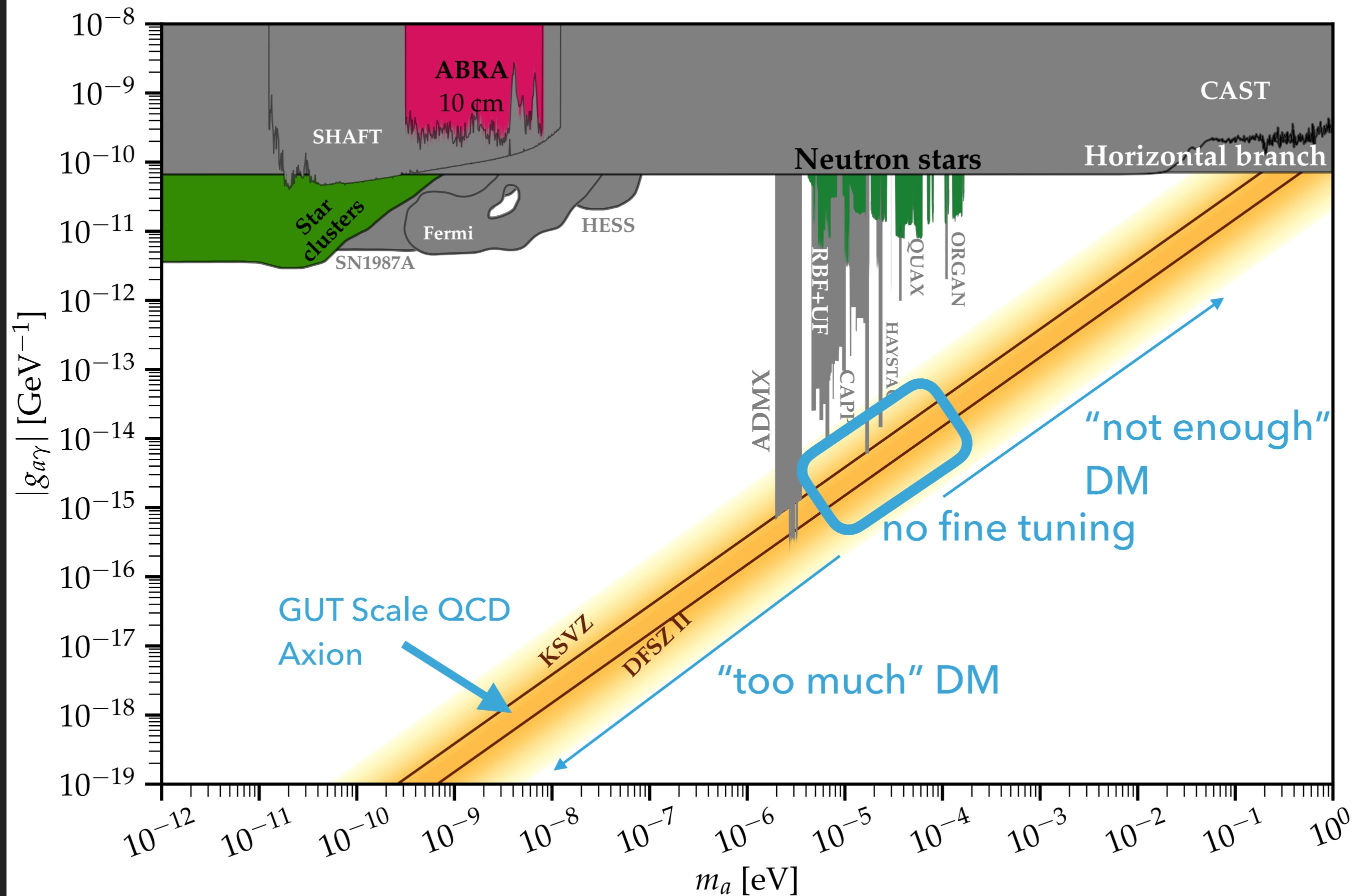
PQ broken  
before inflation!

$$\Omega_a h^2 \sim 0.1 \left( \frac{f_a}{10^{12} \text{ GeV}} \right)^{7/6} \theta_i^2$$

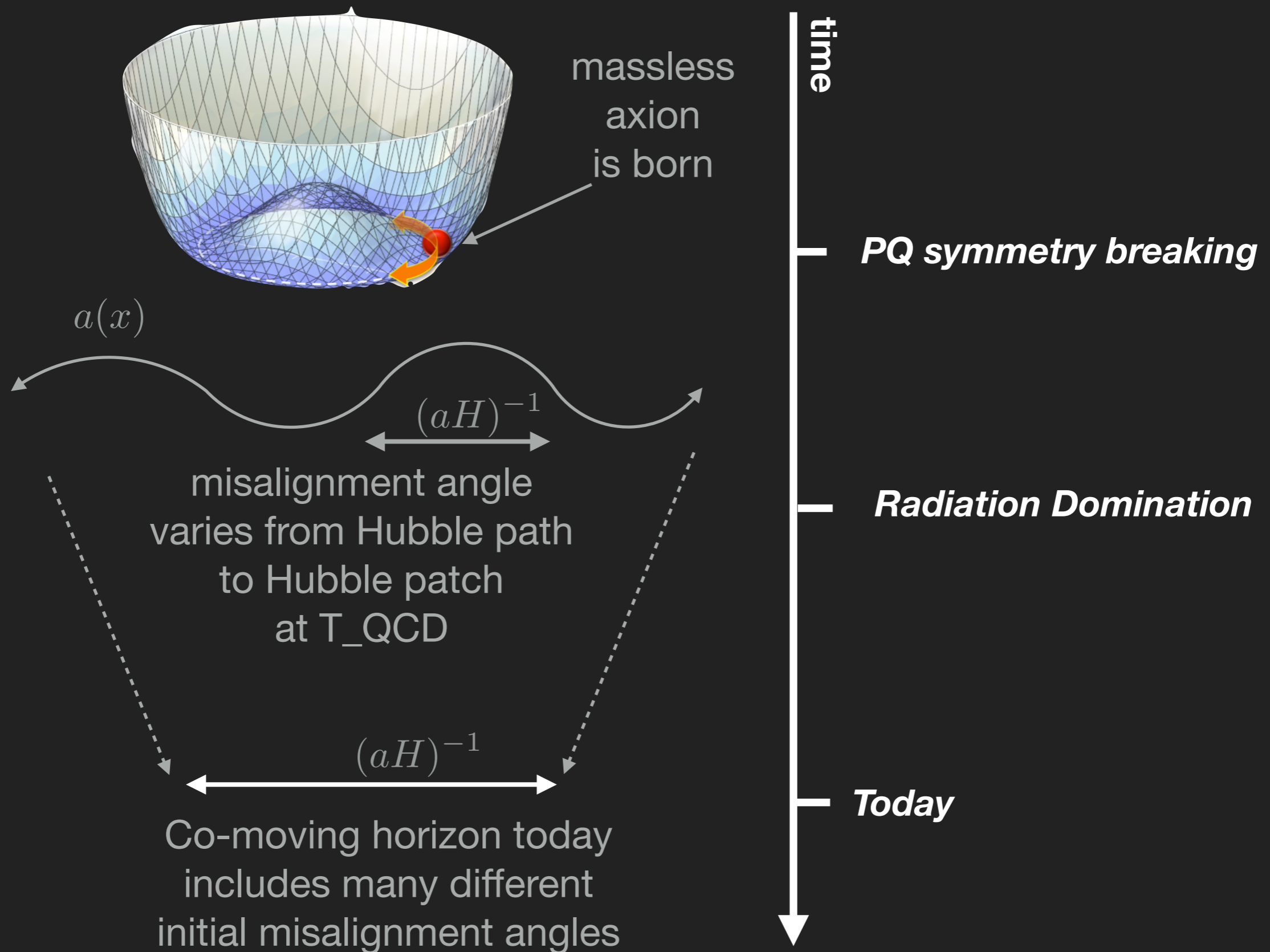
# Axion generated before inflation



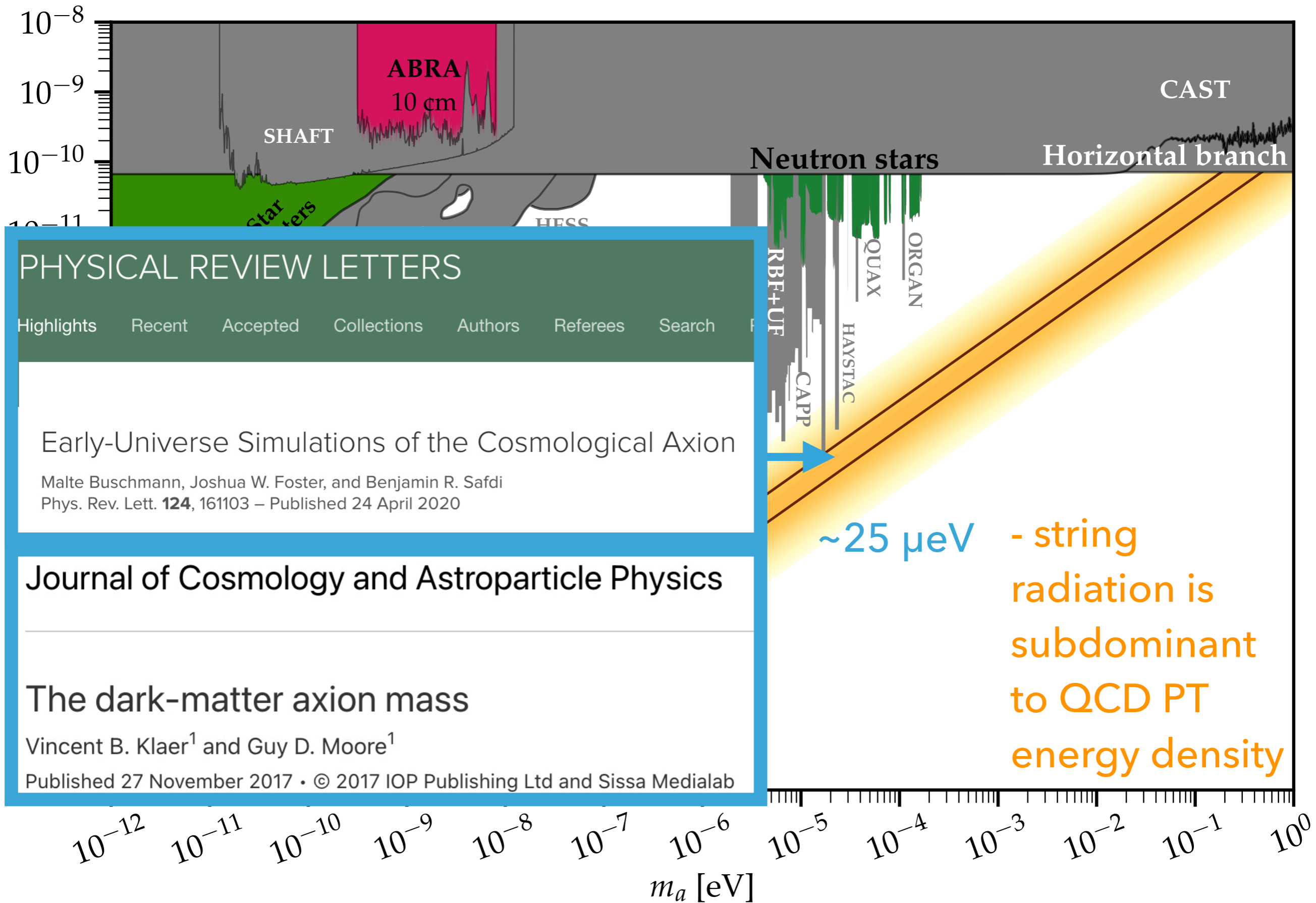
# PQ Broken Before Inflation



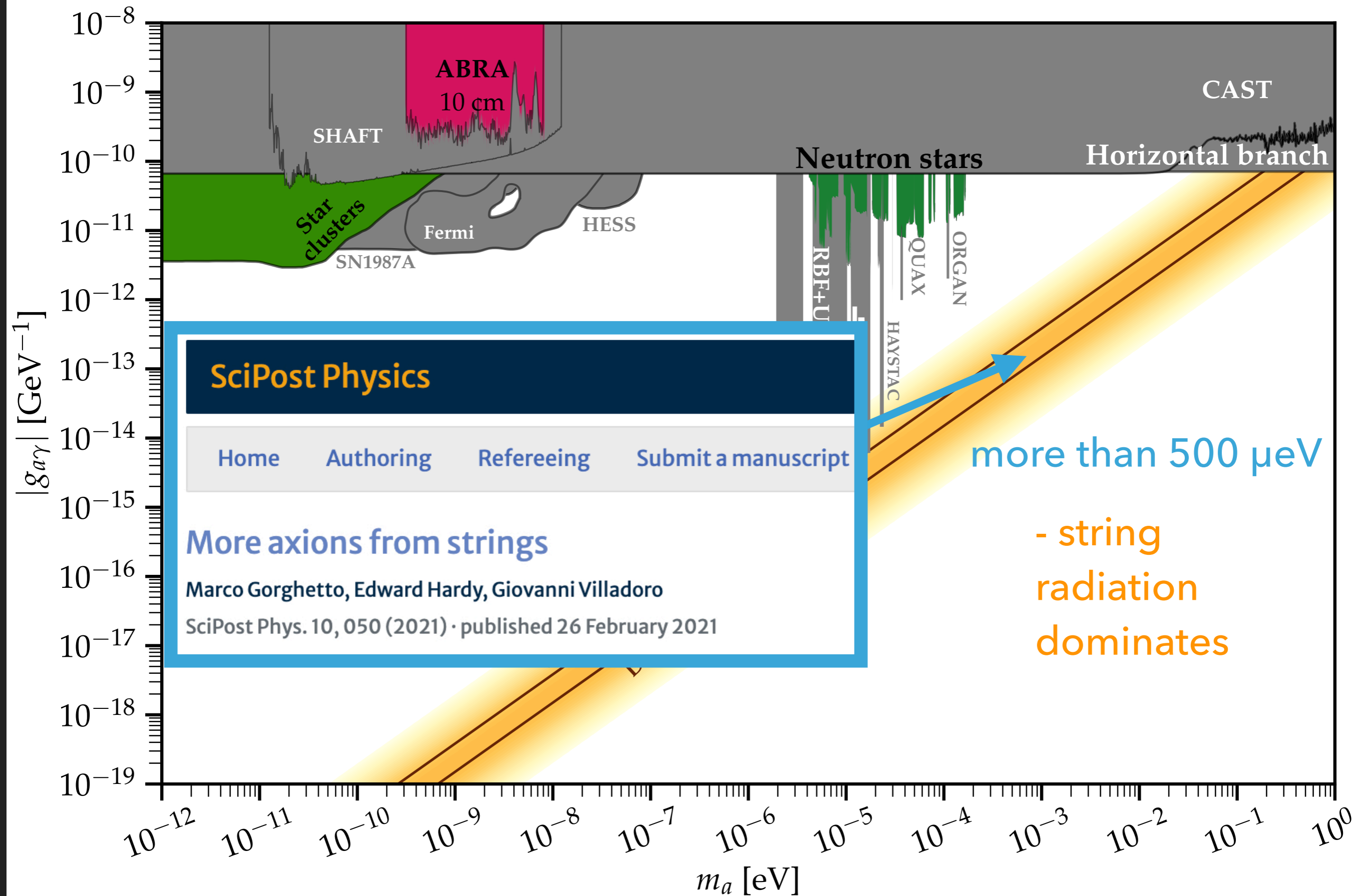
# Axion generated after inflation



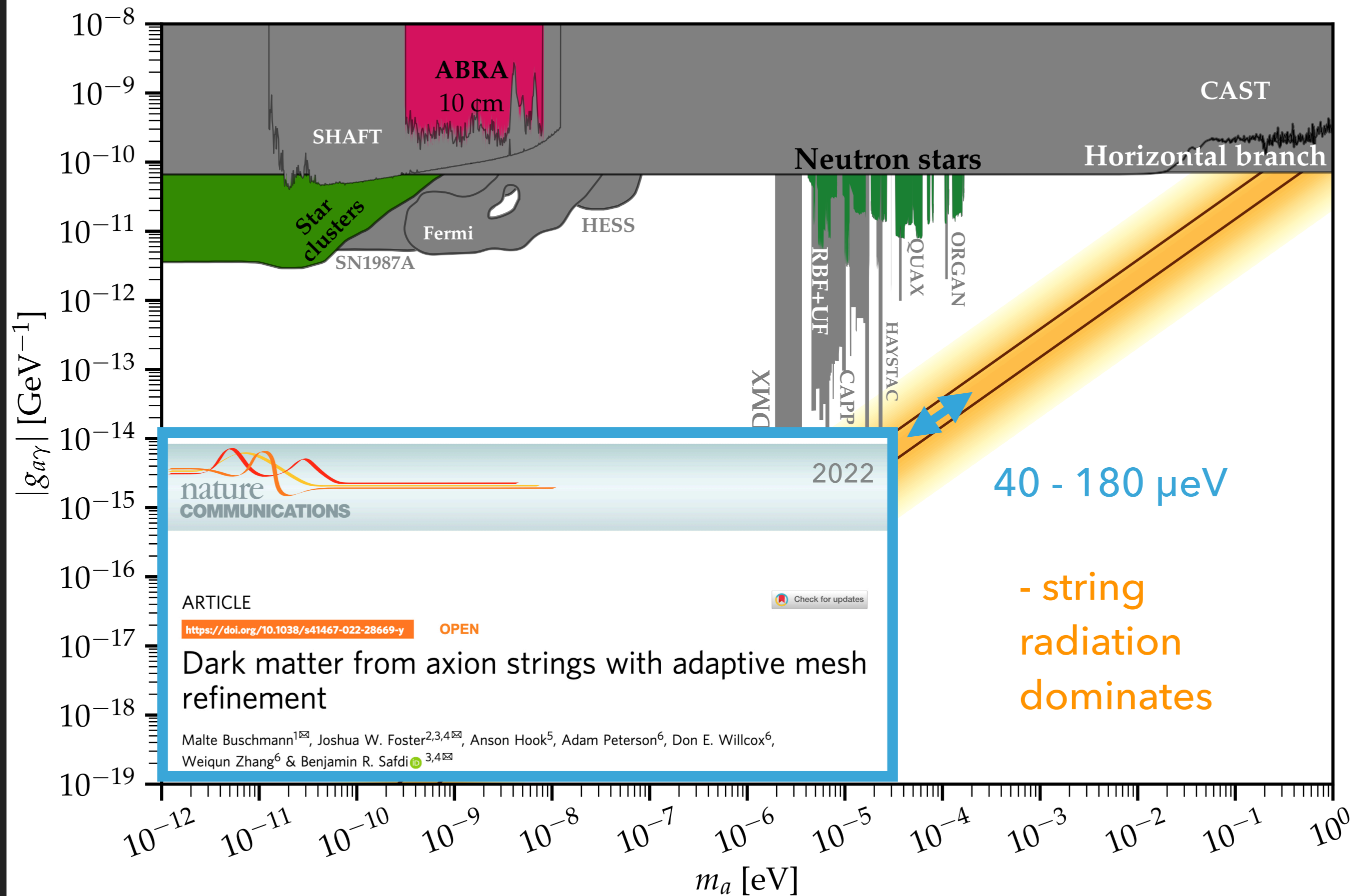
# What does the literature say?



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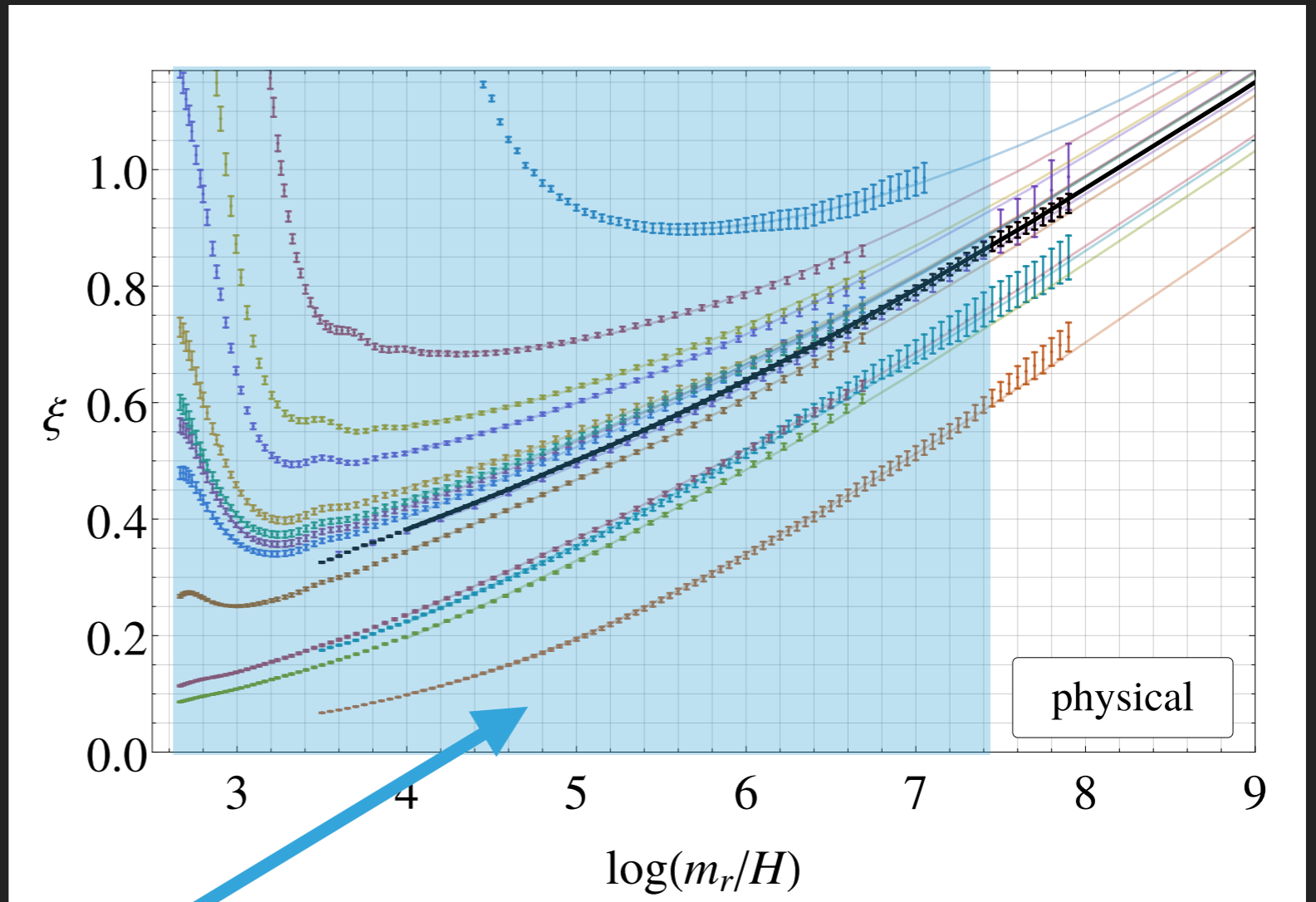


# Why? Two reasons

1. strings per Hubble increases logarithmically with time

A good point!

we can only simulate at small log



PHYSICAL REVIEW LETTERS

Highlights Recent Accepted Collections Authors Referees Search

Early-Universe Simulations of the Cosmological Axion

Malte Buschmann, Joshua W. Foster, and Benjamin R. Safdi  
Phys. Rev. Lett. **124**, 161103 – Published 24 April 2020

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More axions from strings

Marco Gorghetto, Edward Hardy, Giovanni Villadoro

SciPost Phys. 10, 050 (2021) · published 26 February 2021

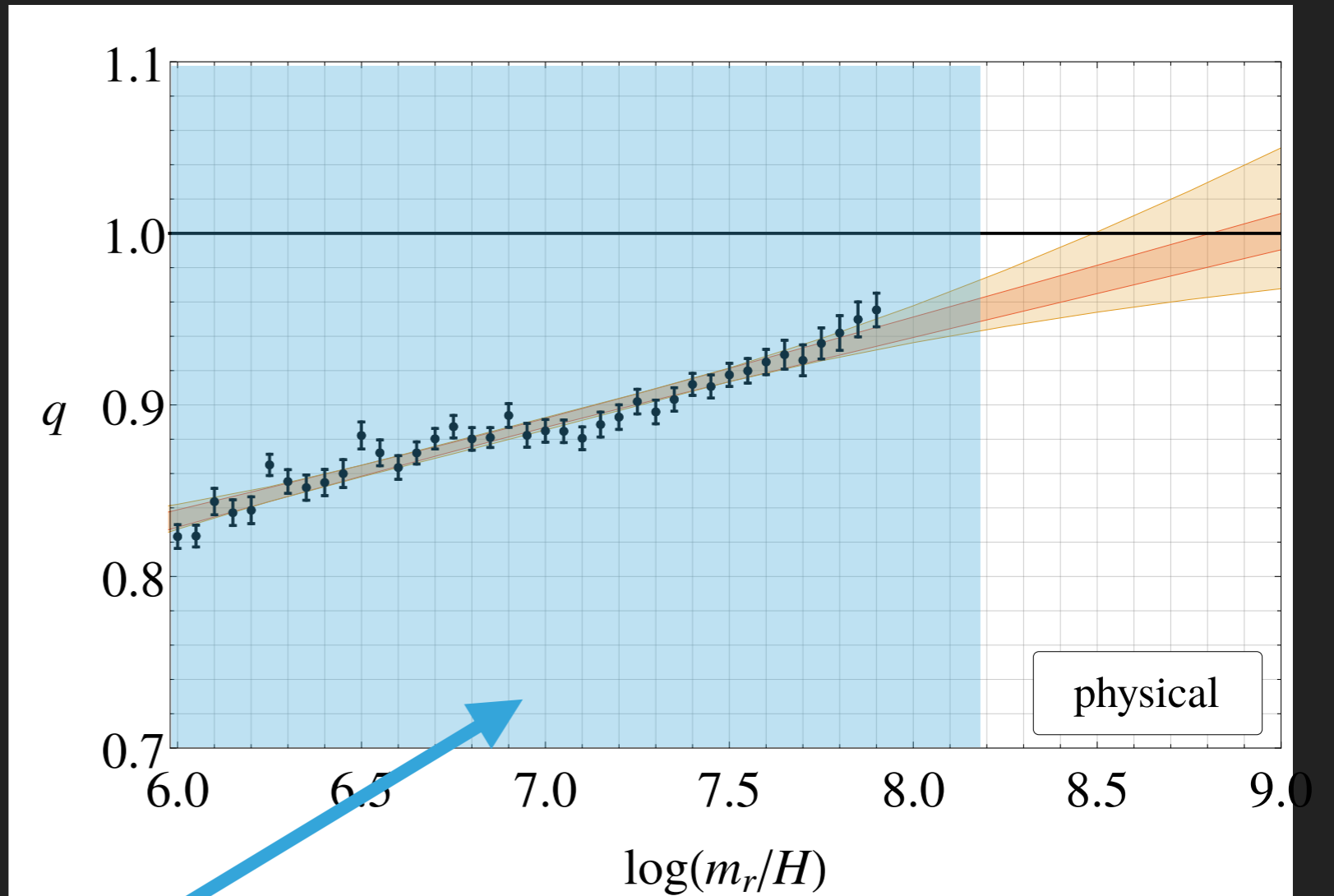
# Why? Two reasons

2. strings radiate more in the IR with time

$$\frac{\partial \rho}{\partial k} \sim \frac{1}{k^q}$$

We do not seem to confirm this! (but also only marginally rule it out)

we can only simulate at small log



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# Axion generated after inflation

M. Buschmann, J. Foster, **B.S.** PRL 2020

Simulate on static grid with  $\sim 10^{10}$  sites

Simulate from PQ phase transition to matter-radiation equality

M. Buschmann, J. Foster, **B.S.**, A. Hook, AMReX Collaboration,  
Nature Communications (Feb. 2022)

Simulate on adaptive grid equiv. to static grid with  $\sim 10^{15}$  sites



National Energy Research  
Scientific Computing Center



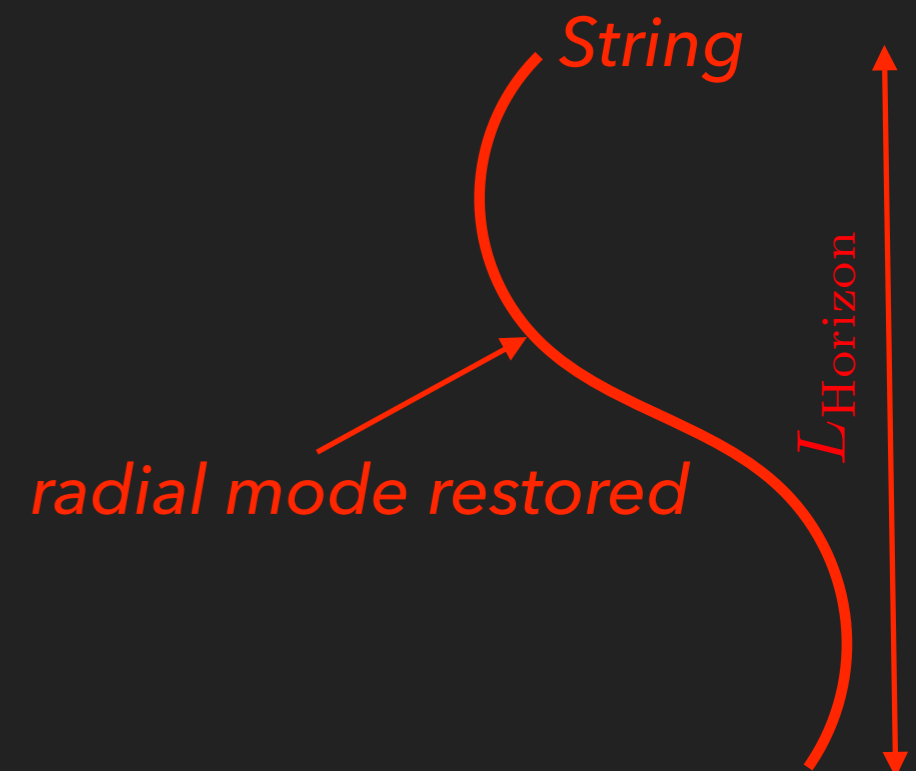
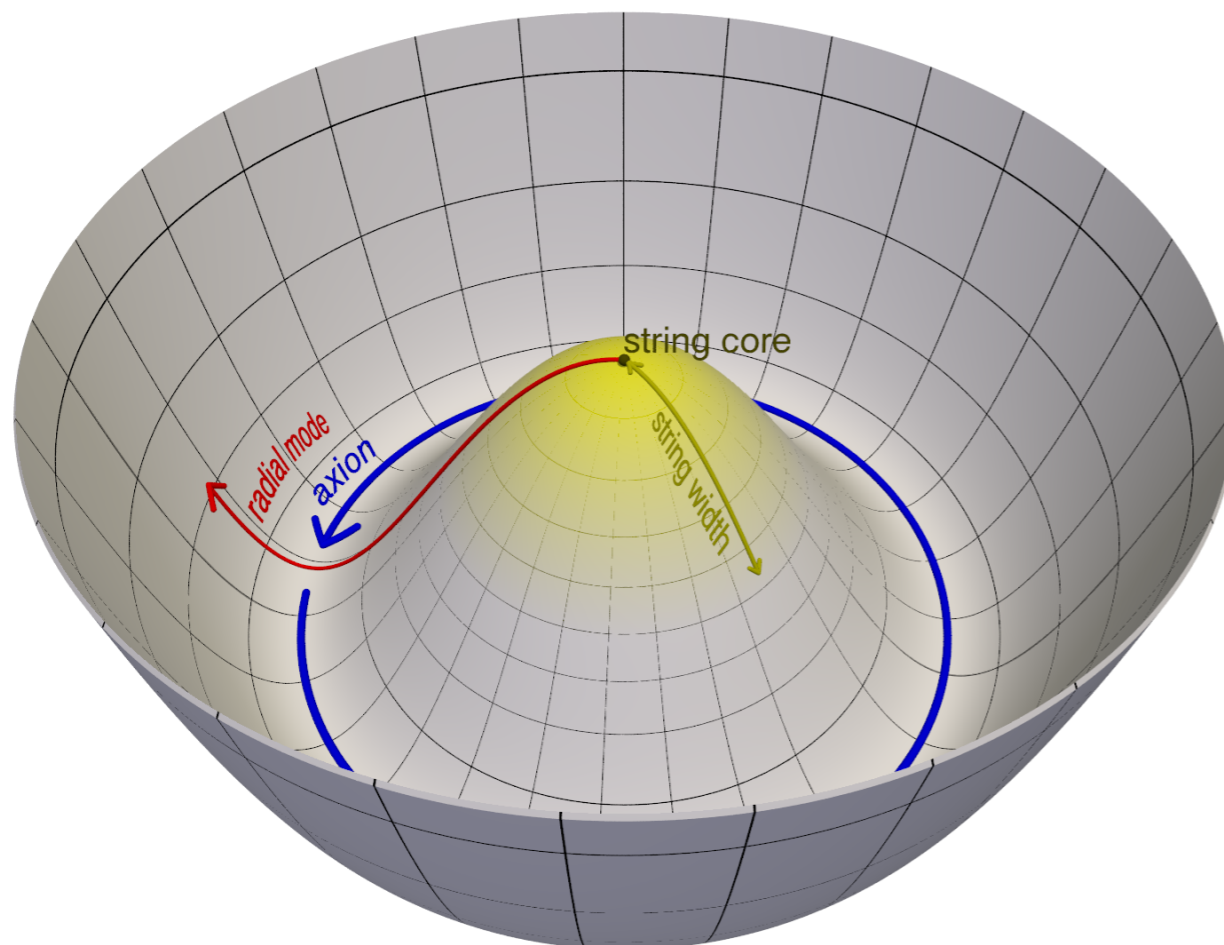
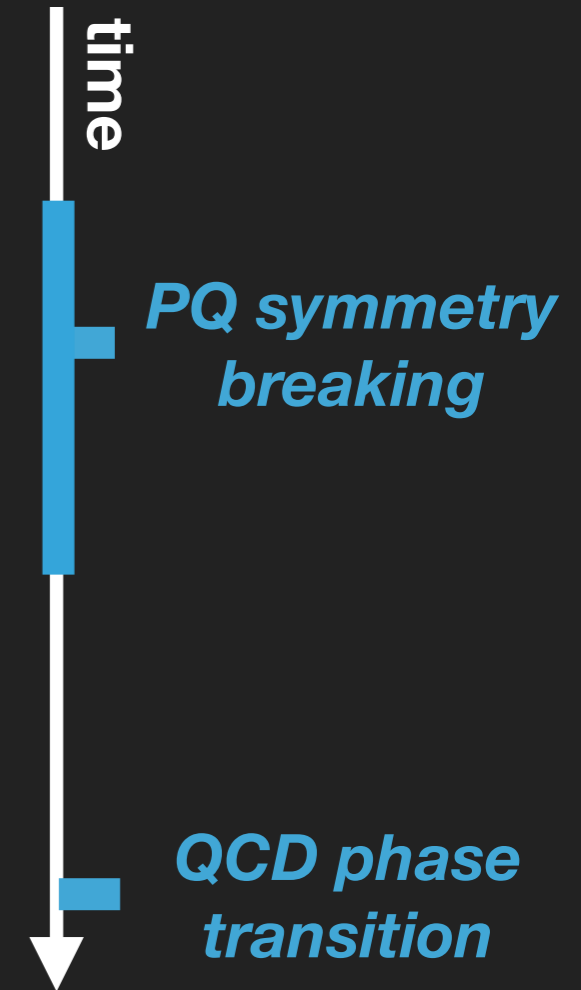
U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

# Axion dark matter primarily produced from strings

$$\mathcal{L}_{\text{PQ}} = \frac{1}{2} |\partial\Phi|^2 - \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2 - \frac{\lambda T^2}{6} |\Phi|^2$$

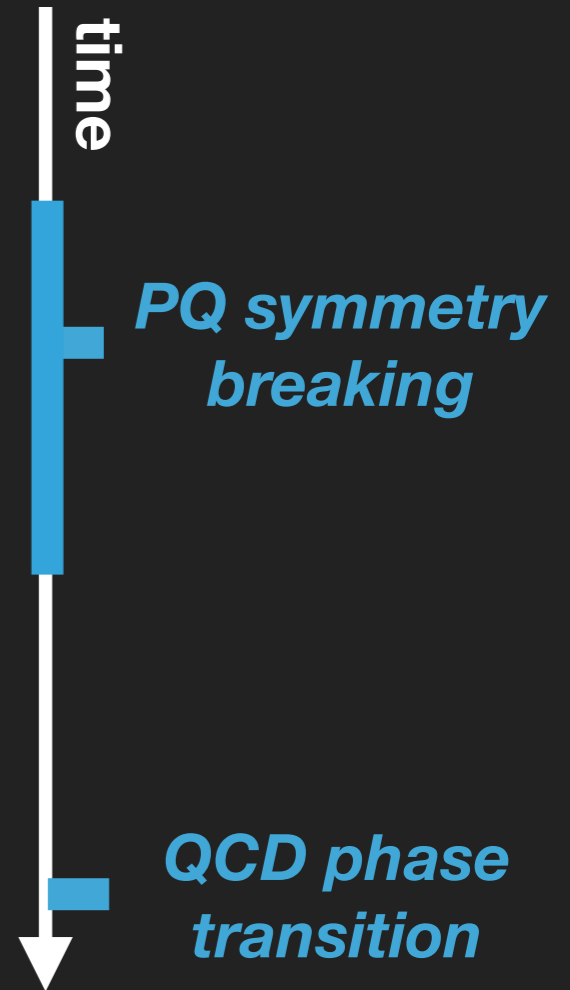
- symmetry broken for  $T \lesssim f_a$
- write  $\Phi(x) = \frac{r(x) + f_a}{\sqrt{2}} e^{ia(x)/f_a}$
- radial mode acquires mass:  $m_r \sim \sqrt{\lambda} f_a$  (take  $\lambda \sim 1$ )



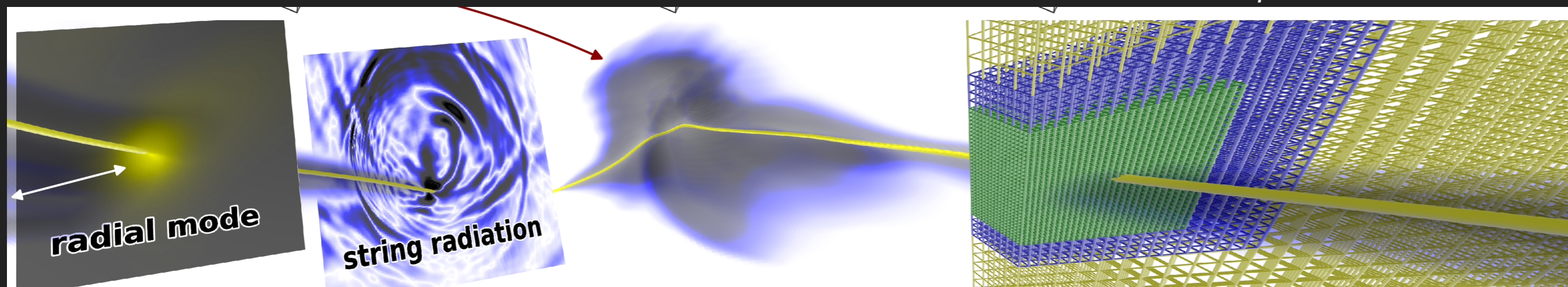
# Axion dark matter primarily produced from strings

$$\mathcal{L}_{\text{PQ}} = \frac{1}{2} |\partial\Phi|^2 - \frac{\lambda}{4} (|\Phi|^2 - f_a^2)^2 - \frac{\lambda T^2}{6} |\Phi|^2$$

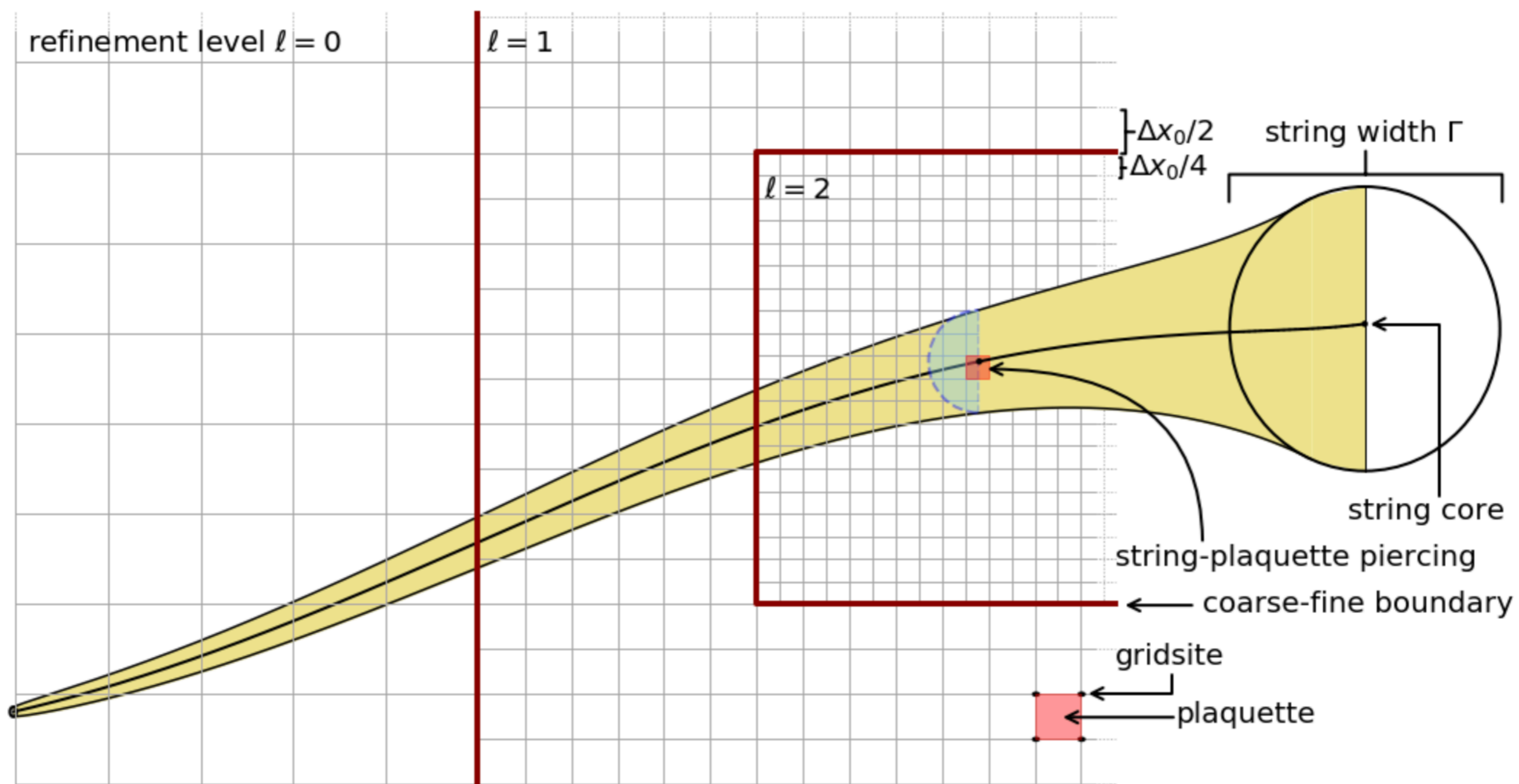
- ▶ symmetry broken for  $T \lesssim f_a$
- ▶ write  $\Phi(x) = \frac{r(x) + f_a}{\sqrt{2}} e^{ia(x)/f_a}$
- ▶ radial mode acquires mass:  $m_r \sim \sqrt{\lambda} f_a$  (take  $\lambda \sim 1$ )
- ▶ Adaptive mesh to maintain high resolution around strings
- ▶ 6e6 CPU-hours over ~100,000 CPUs and ~100 TB RAM
- ▶ Goal: measure axion radiation from strings to compute DM abundance



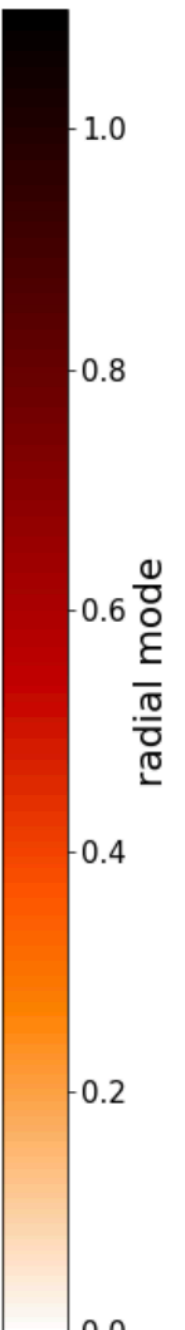
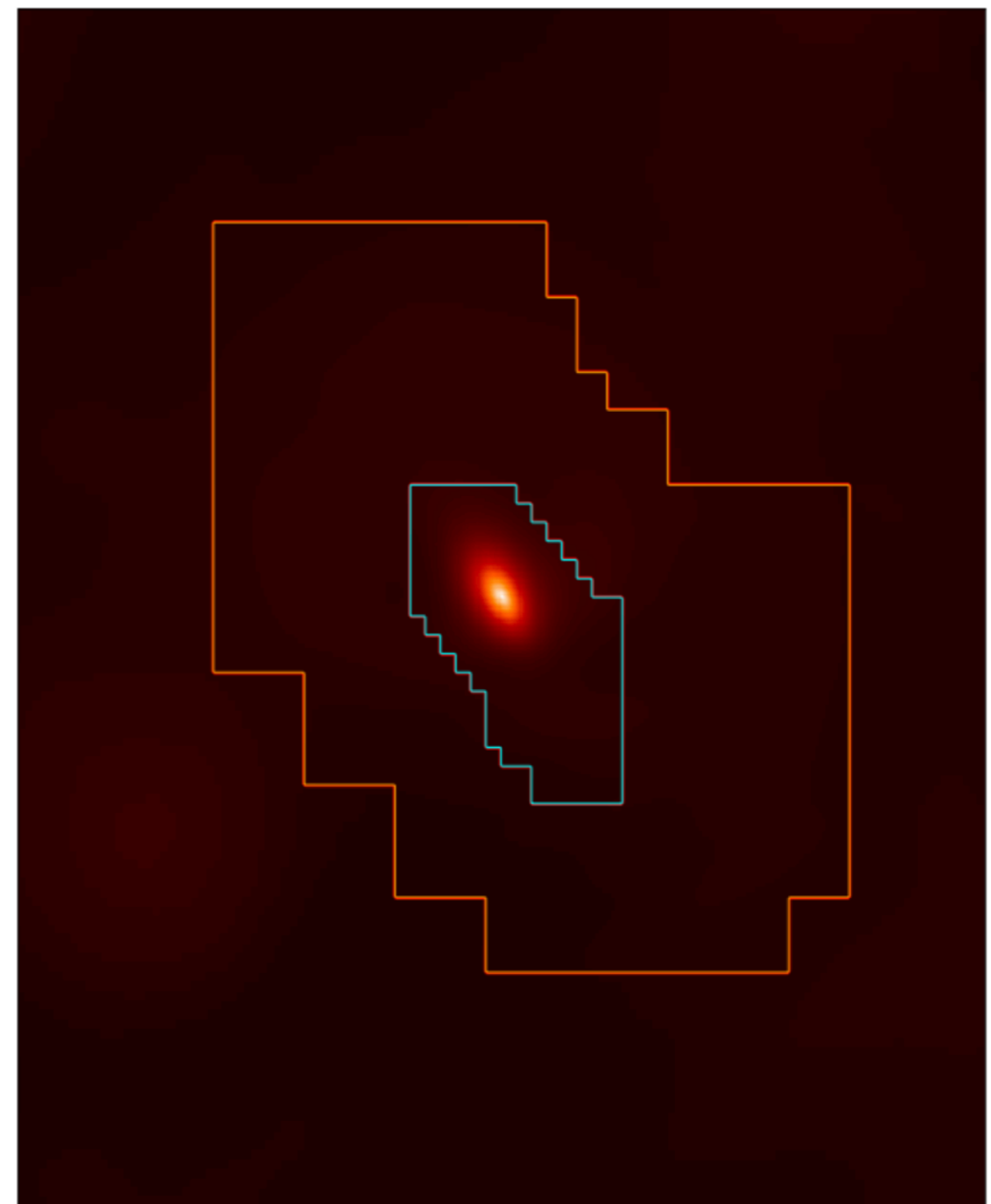
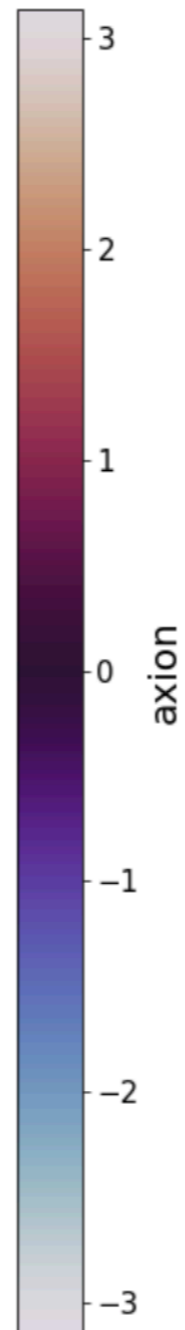
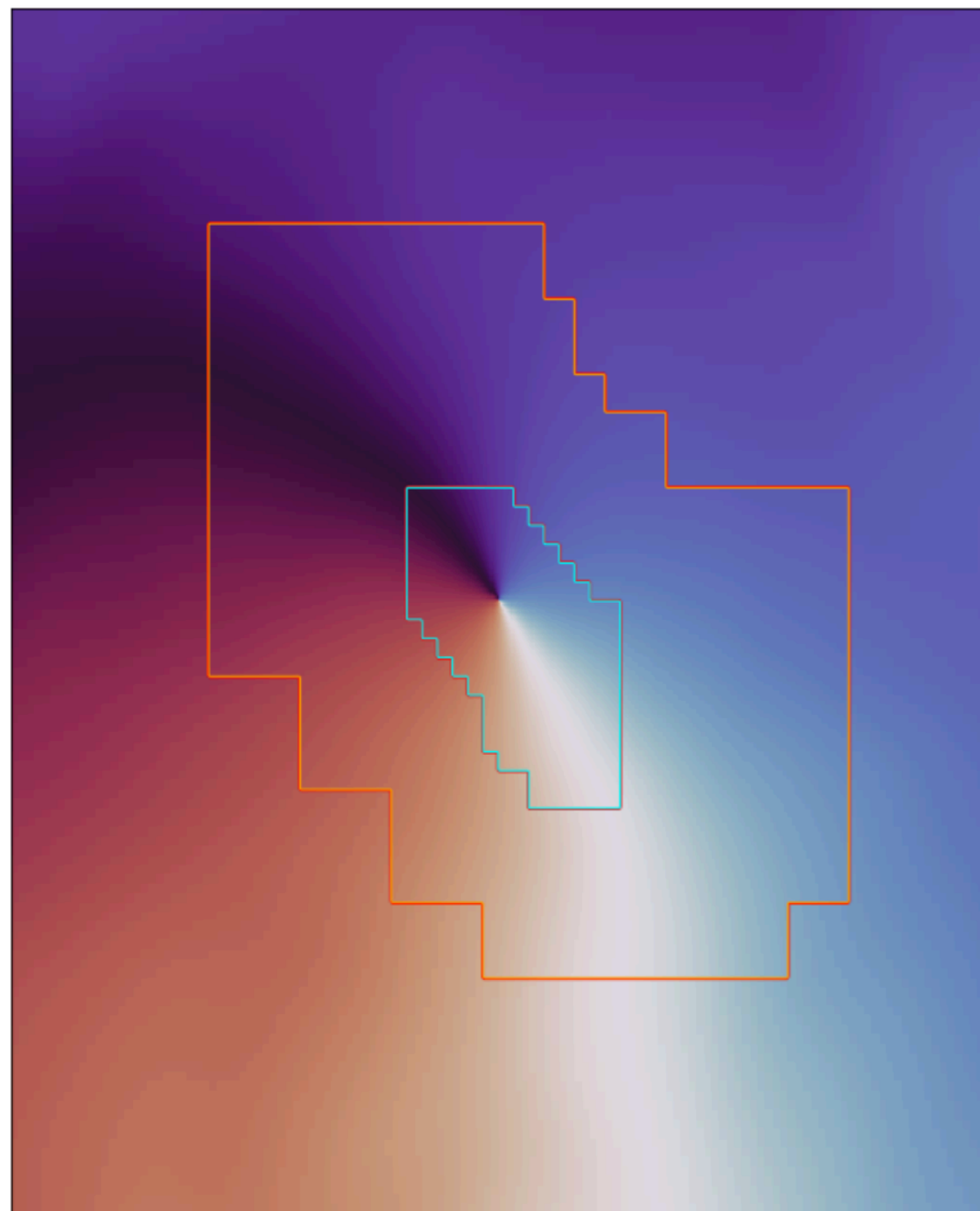
Adaptive mesh



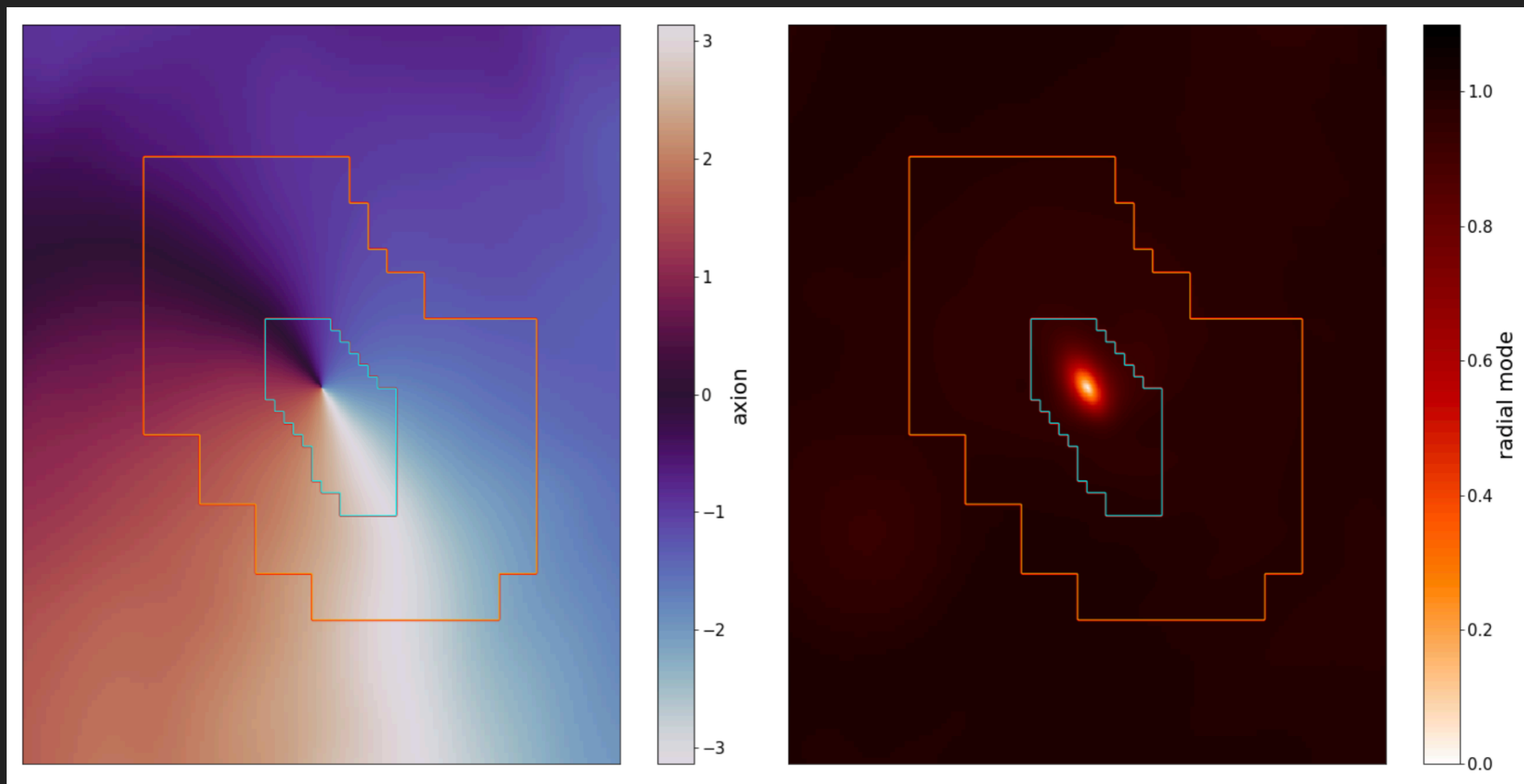
# Answer with Adaptive Mesh Refinement Simulations (AMReX)



# Answer with Adaptive Mesh Refinement Simulations (AMReX)



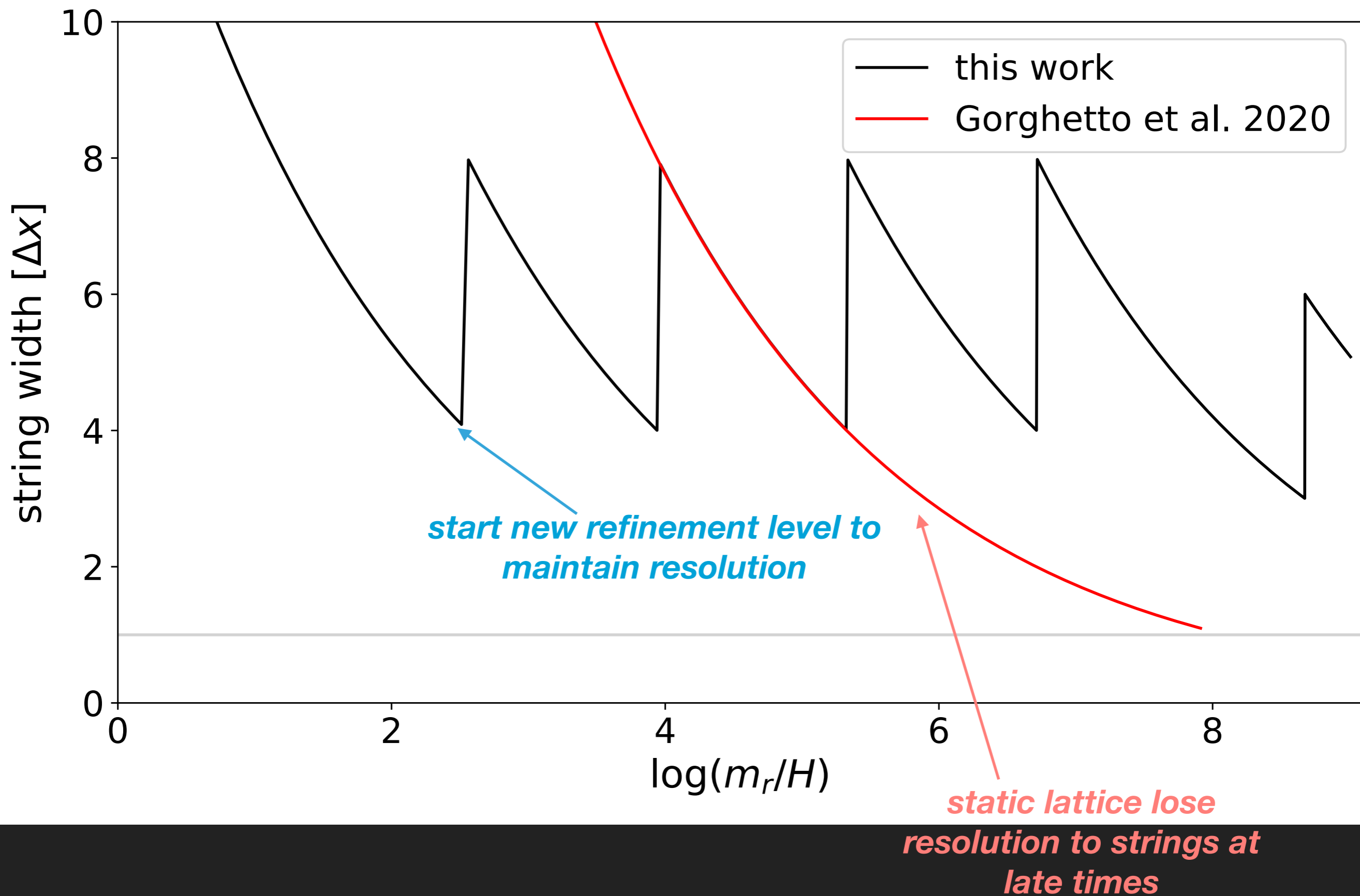
# Axions with AMReX

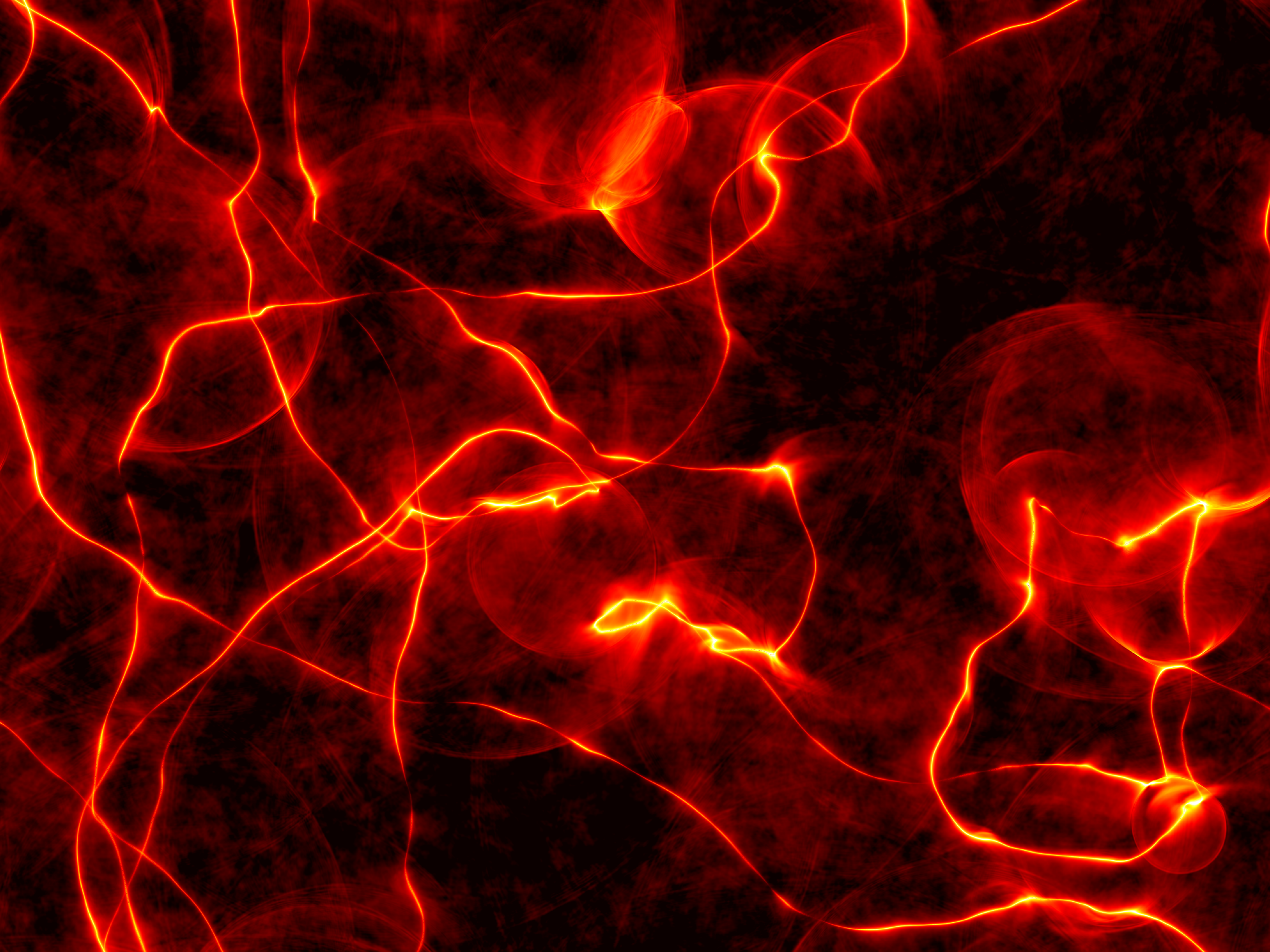


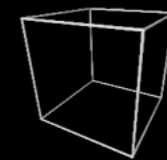
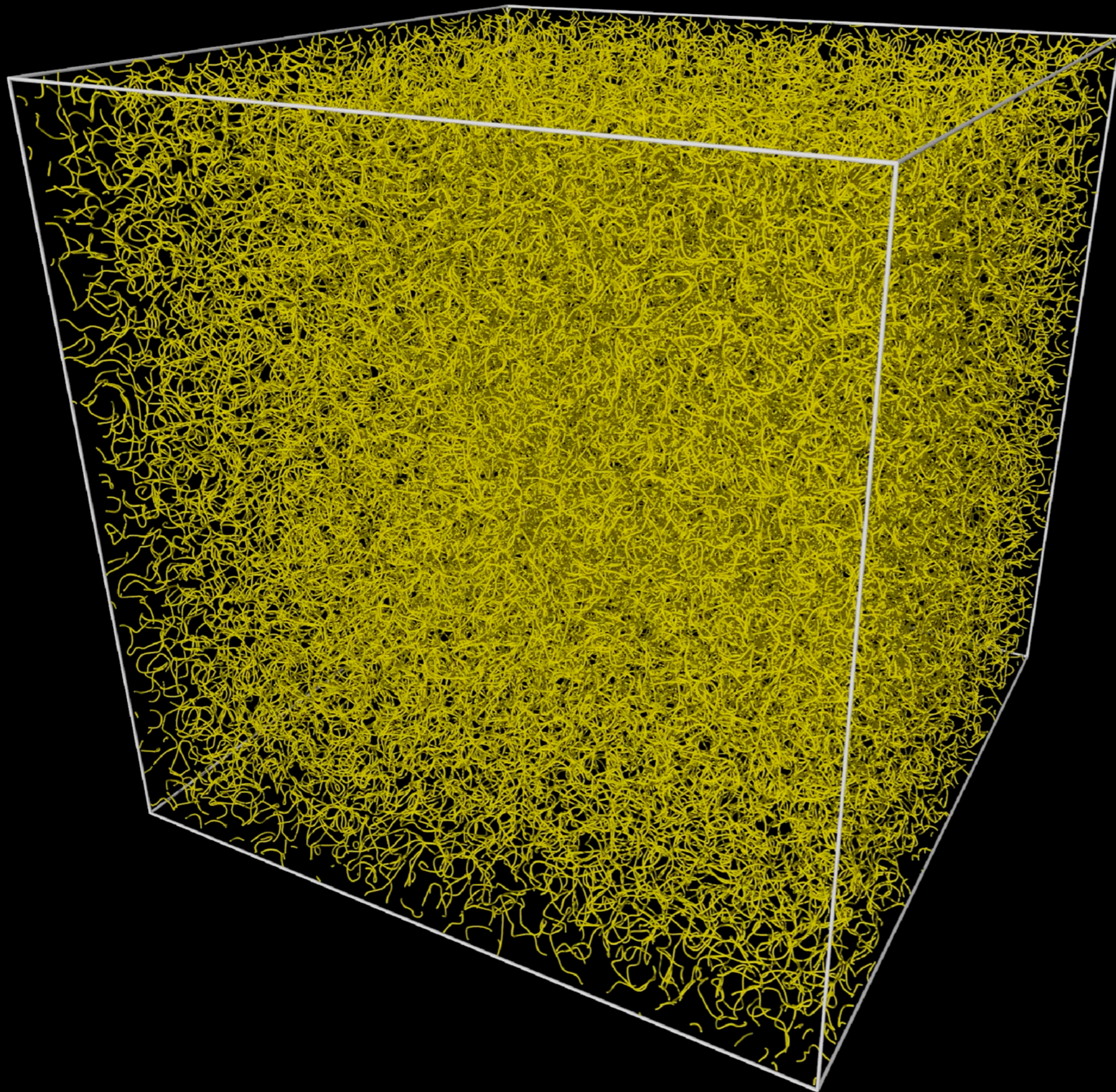
1. We use 6 refinement levels (up to  $131,072^3$  resolution)
2. 1,024 KNL nodes ( $\sim 70,000$  cores) on Cori (NERSC) – 100 TB memory
3. Refinement criteria: use radial mode to indicate presence of strings
4. Comparison: Buschmann et al. 2020 –  $\sim 2,000^3$  resolution



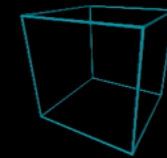
# Axions with AMReX







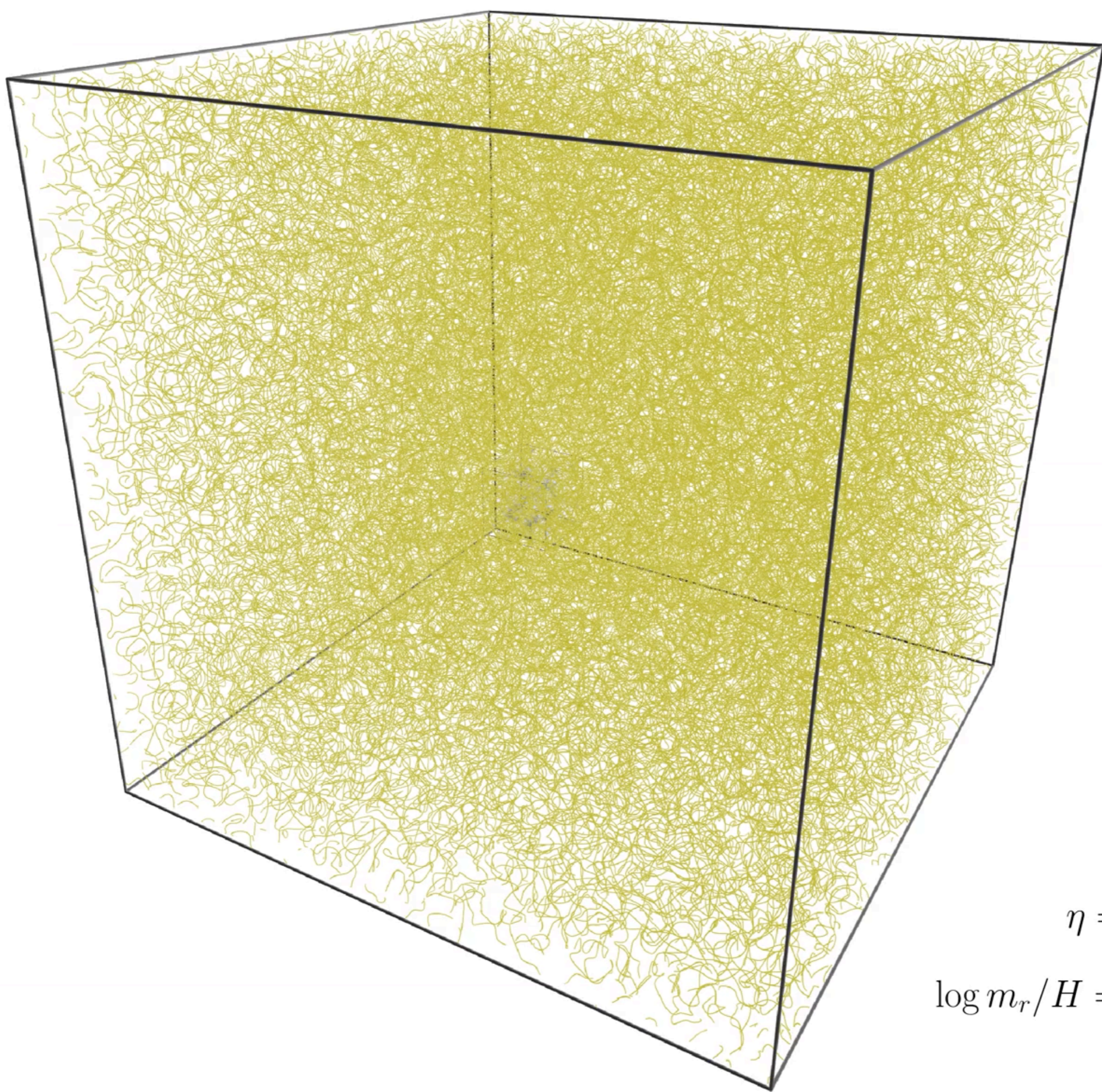
Simulation volume

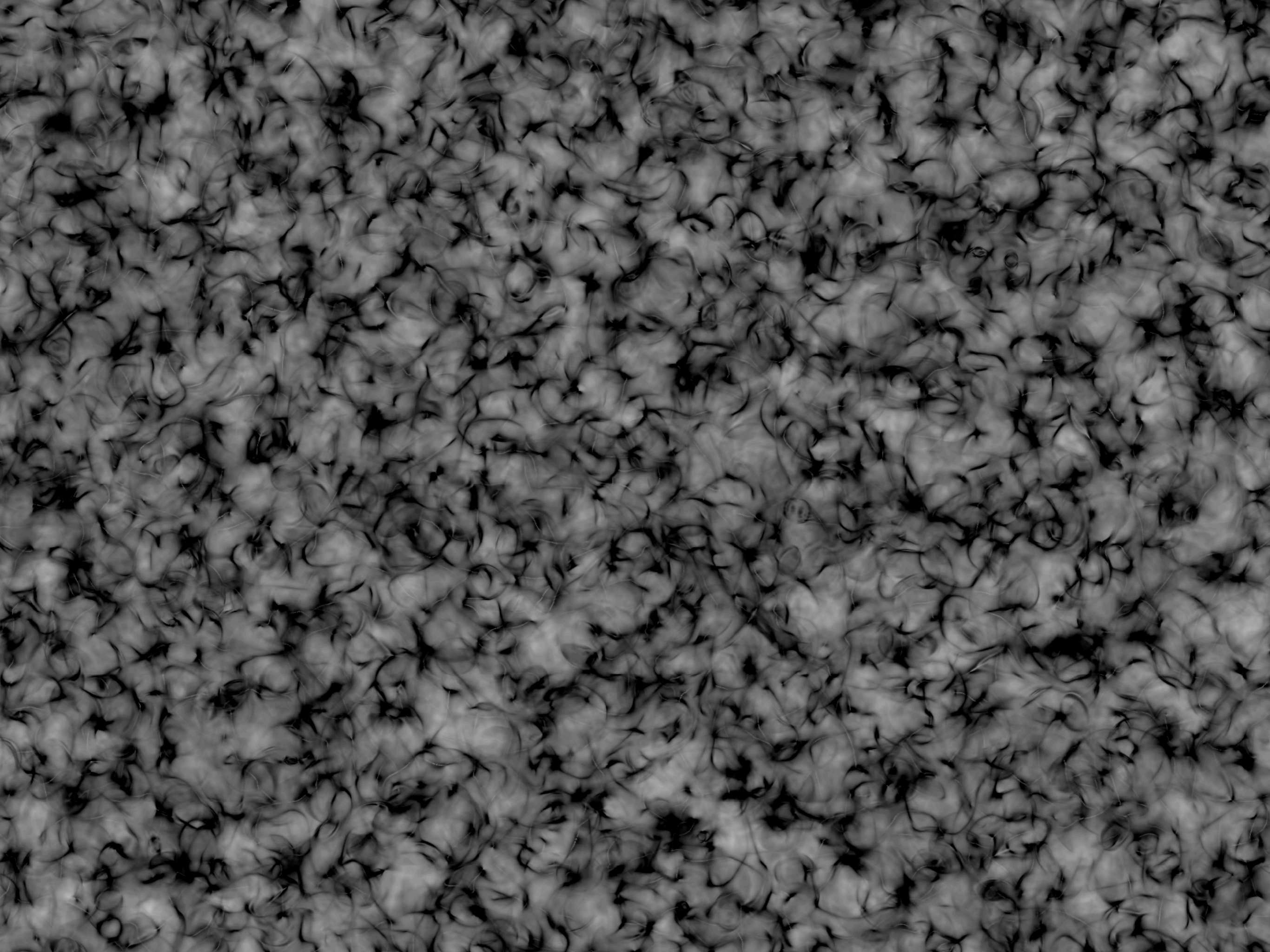


Hubble volume

$$\eta = 0.1$$

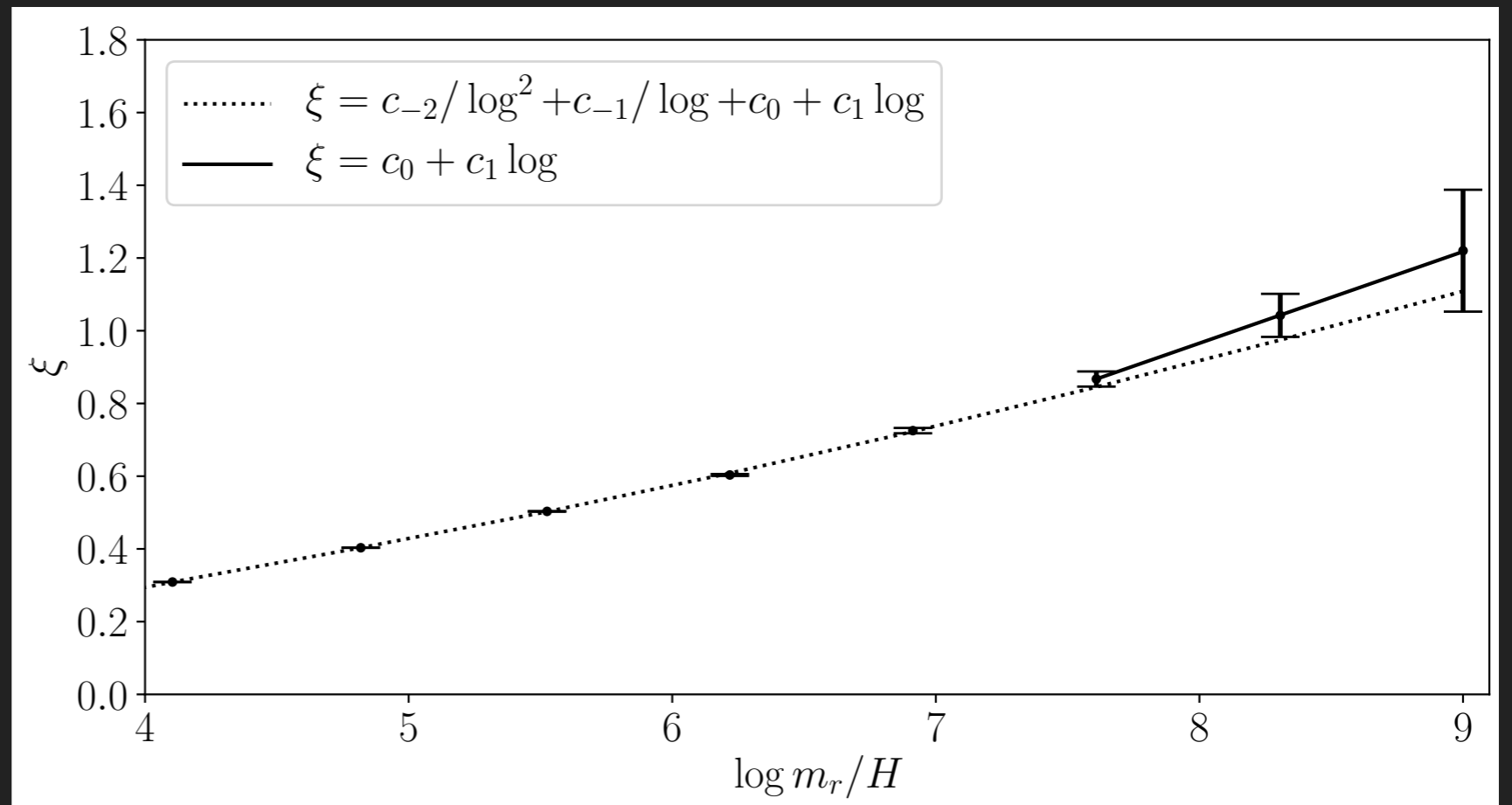
$$\log m_r/H = -3.58$$





# What do we find?

1. strings per Hubble increases logarithmically with time (and understand this analytically)



# What do we find?

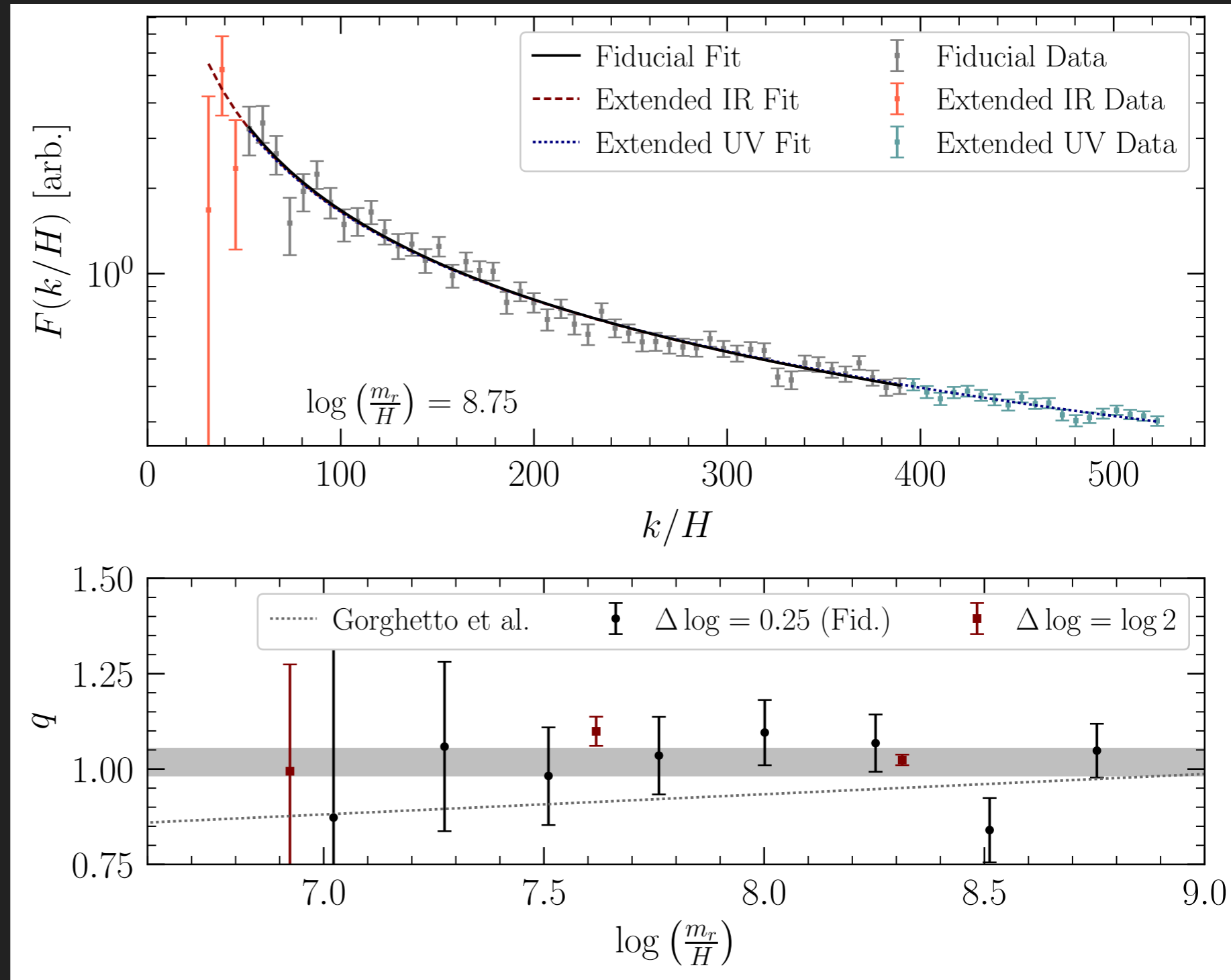
2. radiation does not become IR dominated – conformal to within few %

$$\frac{\partial \rho}{\partial k} \sim \frac{1}{k^q}$$

$$q \in (0.98, 1.04)$$



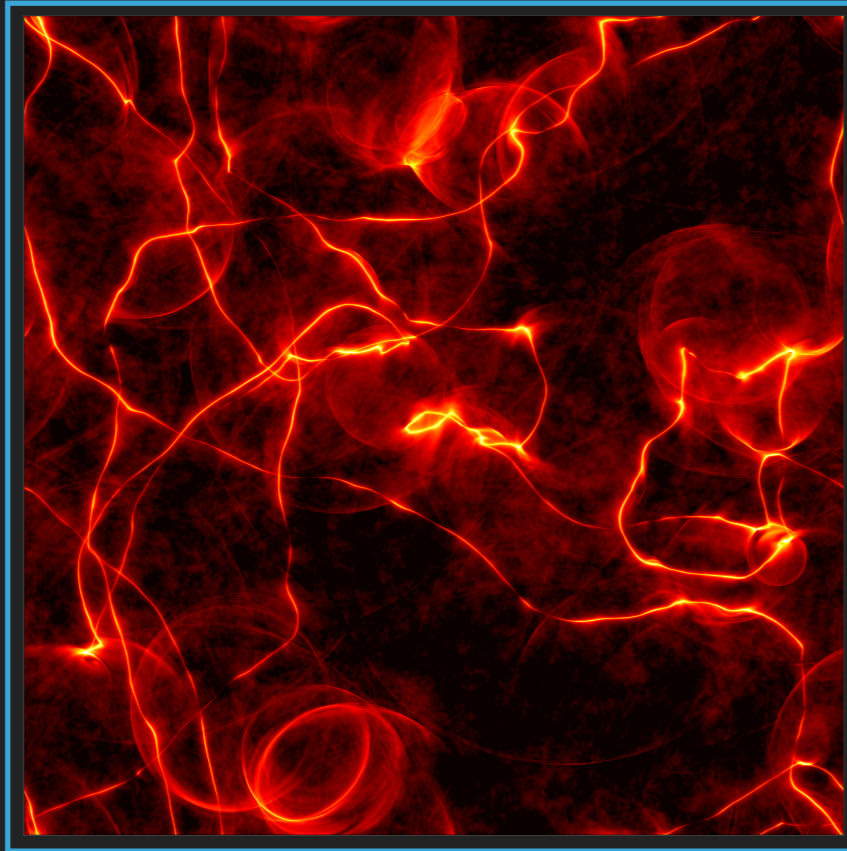
$$m_a \in (40, 180) \mu\text{eV}$$



$$m_a = 65 \pm 6 \mu\text{eV} \longleftarrow q = 1$$

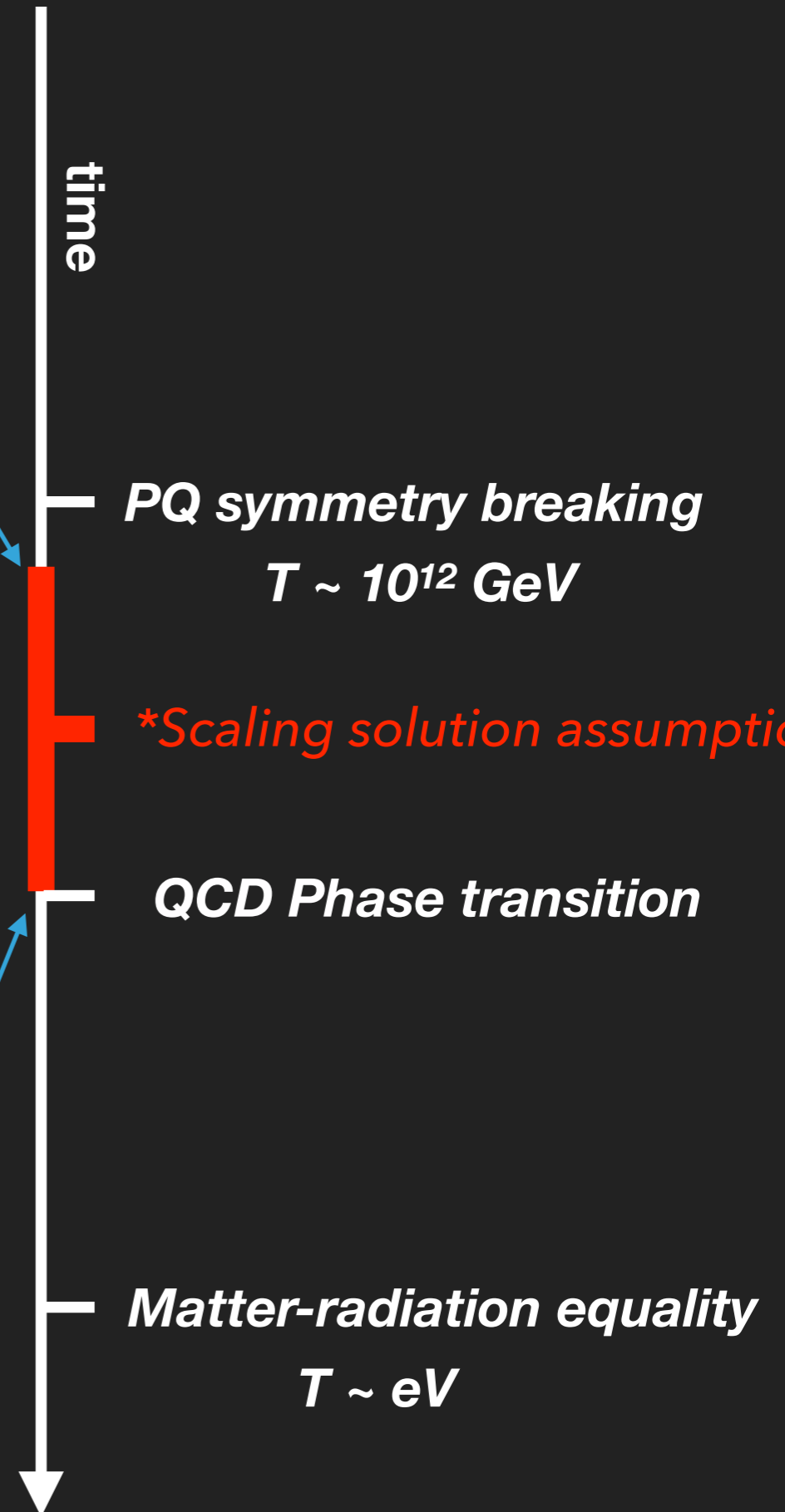
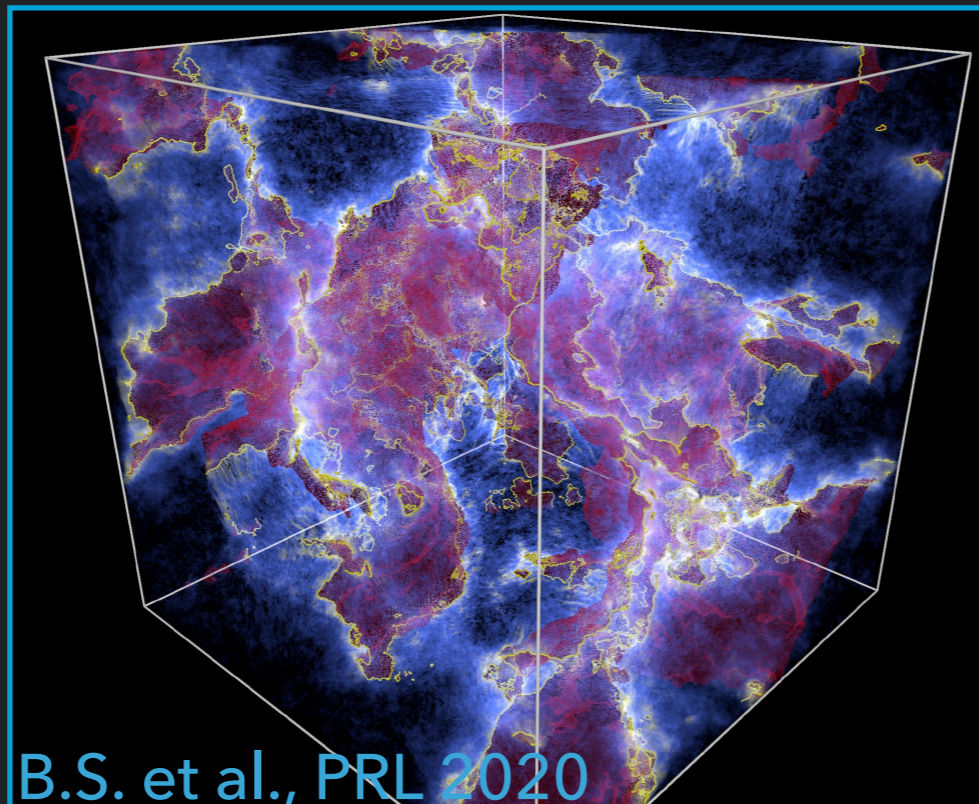
# Why does the spectrum matter?

1. Axions from string radiation non-relativistic at QCD phase transition



2. DM abundance determined by axion number density

3. For fixed energy density, spectral index determines number density





# How to calculate the DM relic abundance

$\Omega_a^{\text{str}} \propto$  axion number density at QCD phase transition

$$\Omega_a^{\text{str}} \propto \xi_* \times \left\langle \frac{H}{k} \right\rangle$$

← leaving off dependence on string tension

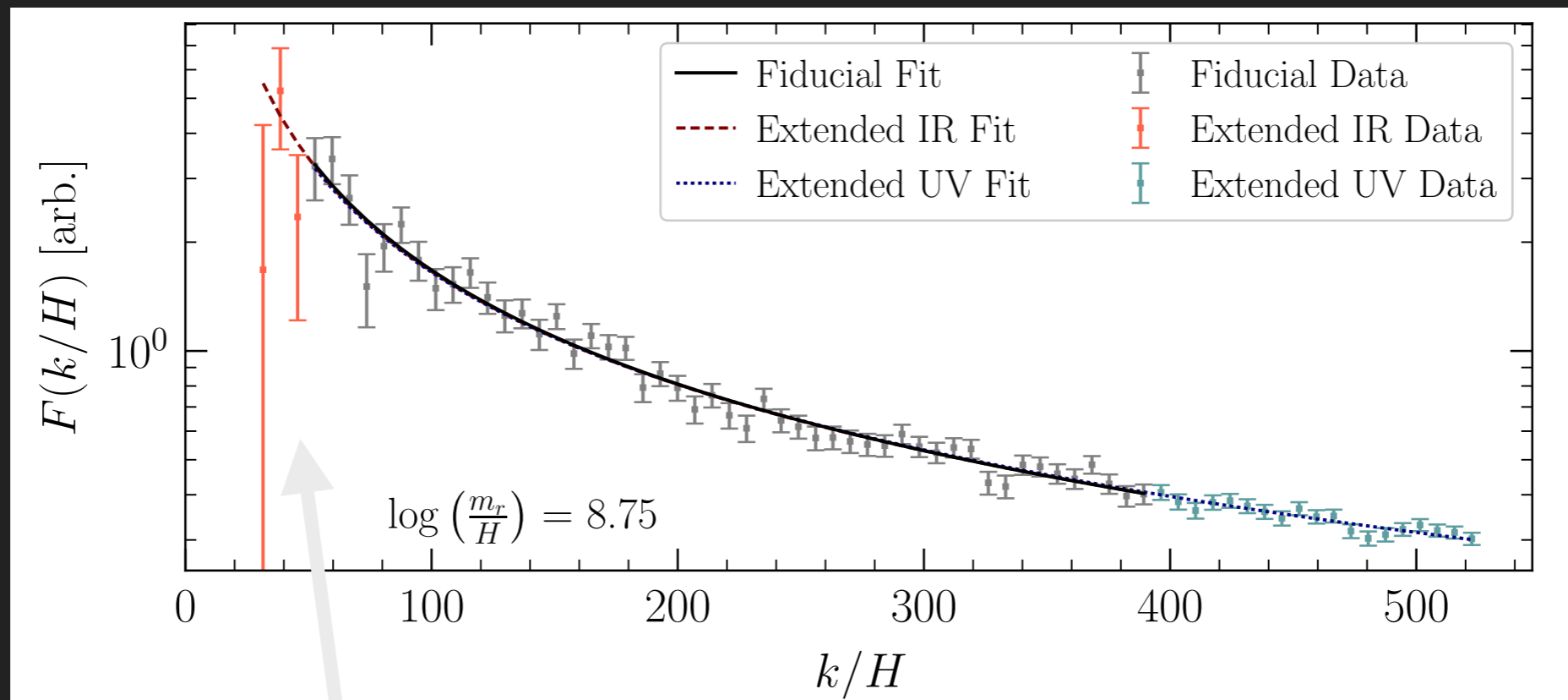
← inverse axion wavelength from string radiation at QCD

↑ number of strings per Hubble at QCD

# How to calculate the DM relic abundance

$$\Omega_a^{\text{str}} \propto \xi_* \times \left\langle \frac{H}{k} \right\rangle$$

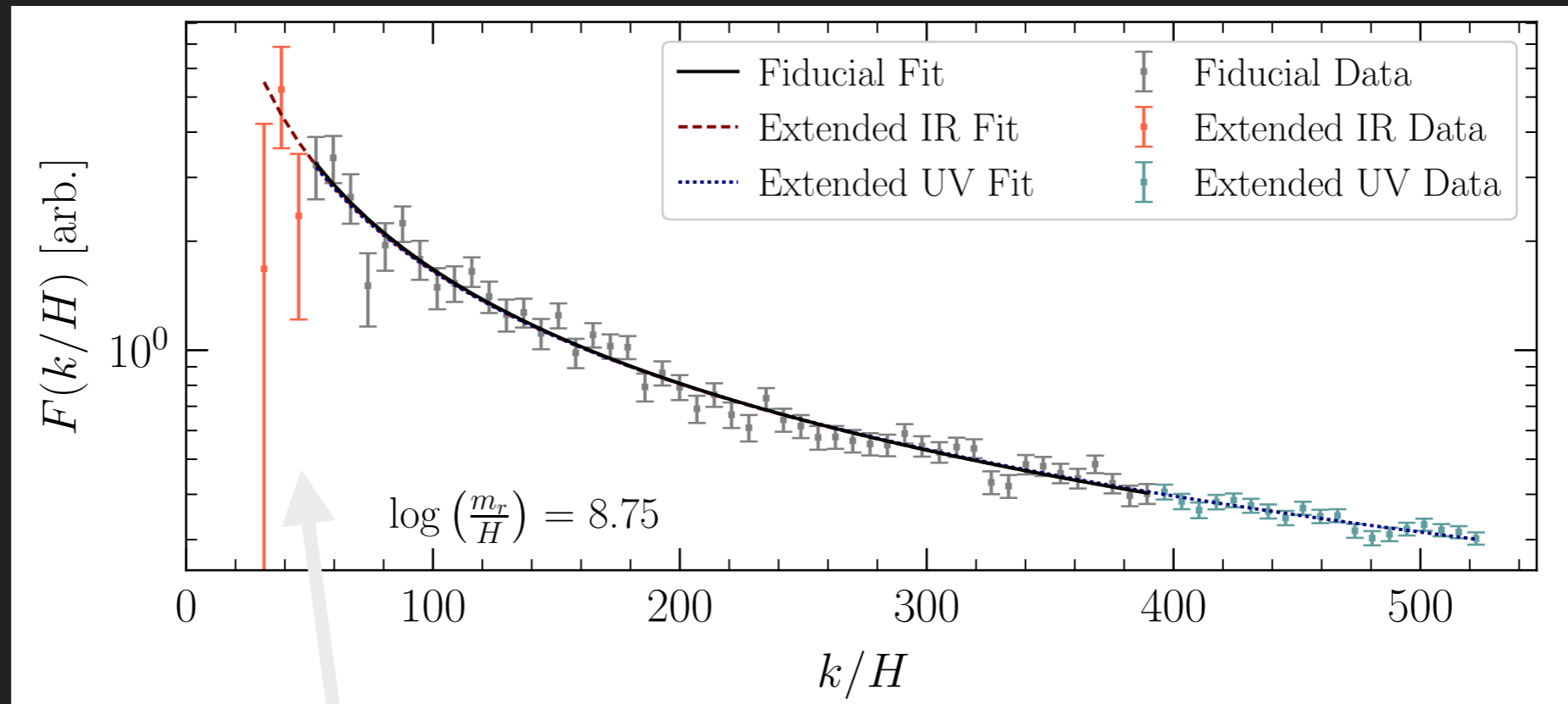
**How to compute  $\langle H/k \rangle$ :** Numerically integrate spectrum in IR, power-law fit in UV



**IR cut-off moves to UV like  $\sqrt{\xi}$  (maximum string curvature scale)**

# How to calculate the DM relic abundance

$$\Omega_a^{\text{str}} \propto \xi_* \times \left\langle \frac{H}{k} \right\rangle$$



**IR cut-off moves to UV like  $\sqrt{\xi}$  (maximum string curvature scale)**

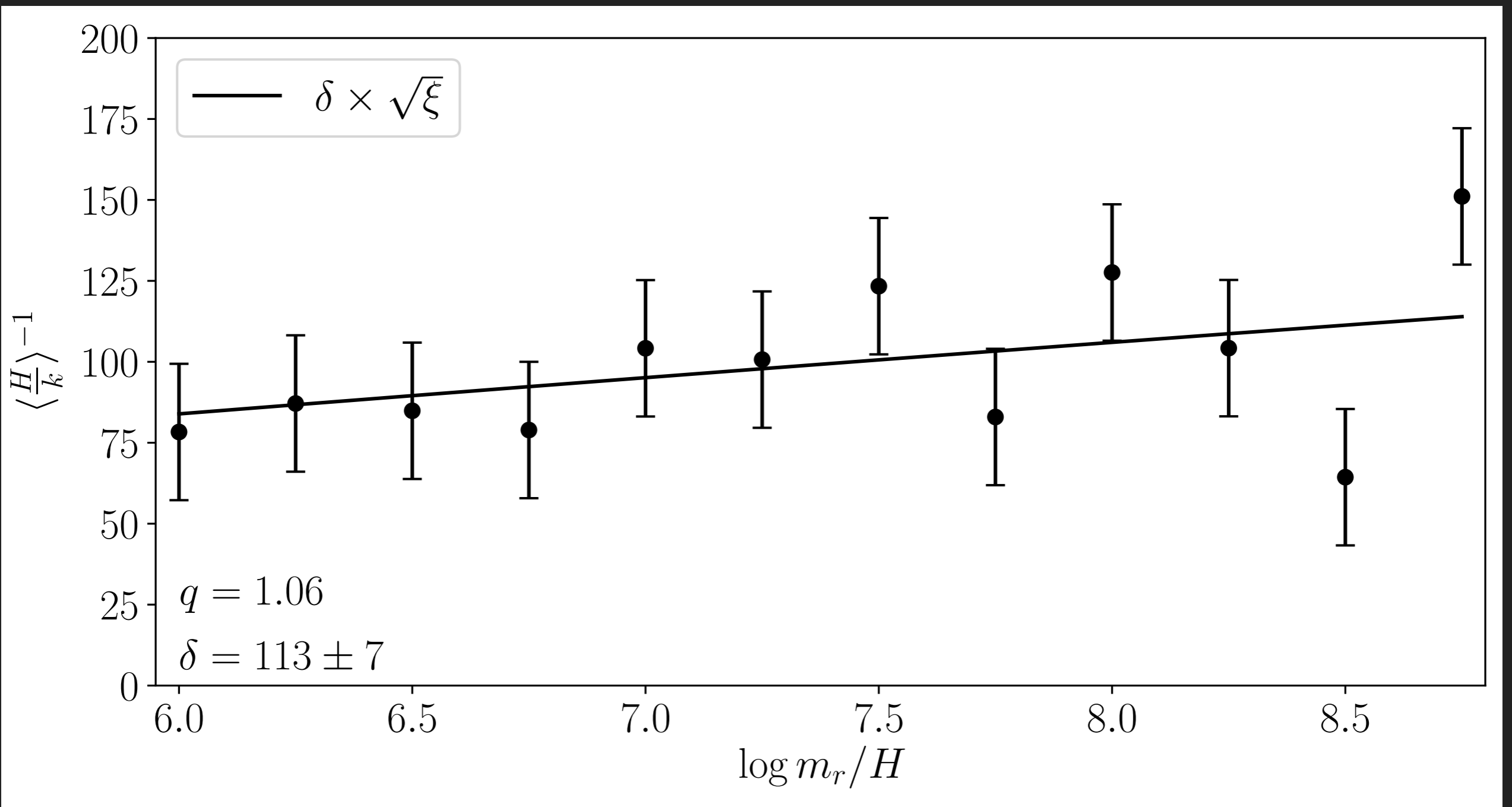
If  $q > 1$  (IR dominated), we expect  $\left\langle \frac{H}{k} \right\rangle^{-1} = \delta \times \sqrt{\xi}$

$$\Omega_a^{\text{str}} \propto \frac{\sqrt{\xi_*}}{\delta}$$

# How to calculate the DM relic abundance

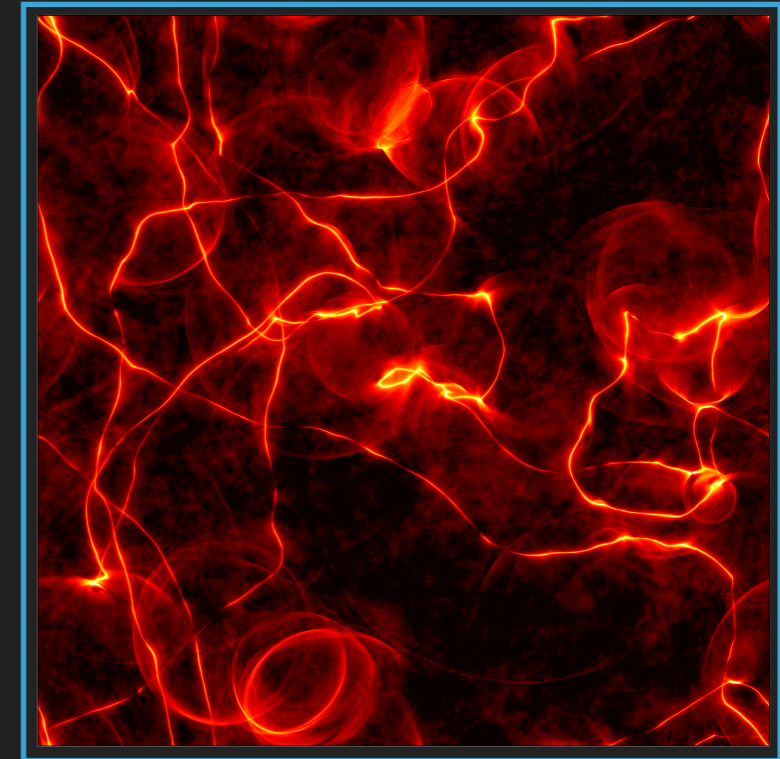
$$\Omega_a^{\text{str}} \propto \frac{\sqrt{\xi_*}}{\delta}$$

Numerically integrate spectrum in IR, power-law fit in UV



# The DM relic abundance

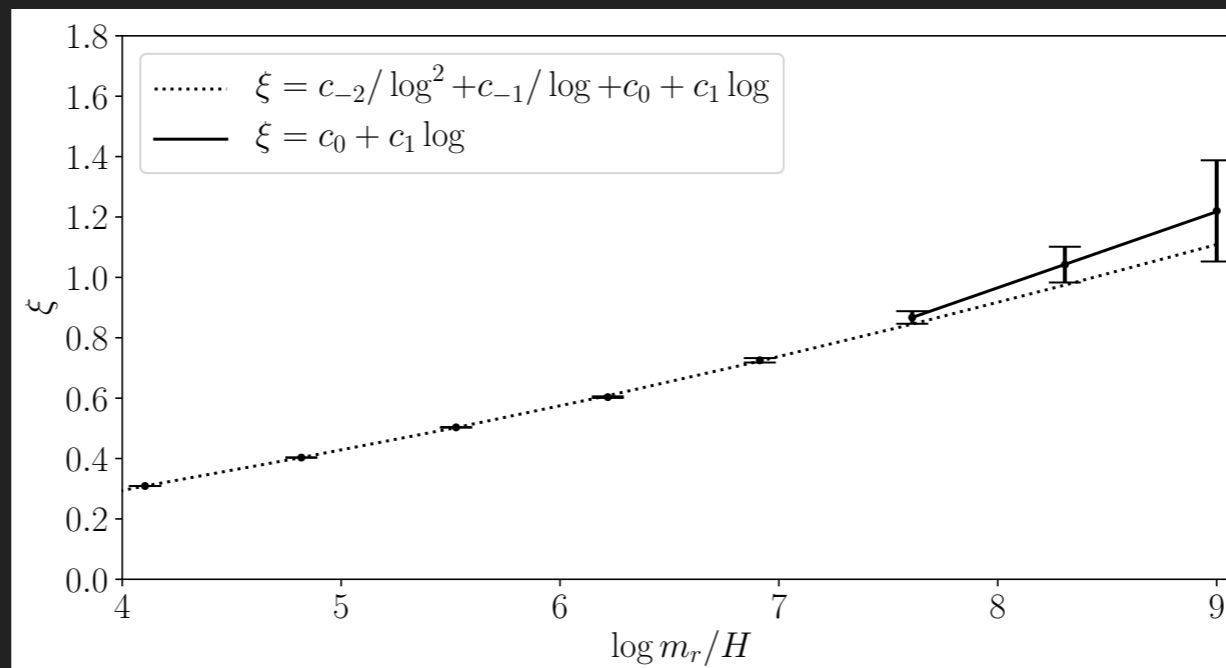
$$\Omega_a^{\text{str}} \approx 0.12 h^{-2} \left( \frac{f_a}{4.3 \cdot 10^{10} \text{GeV}} \right)^{1.17} \frac{107}{\delta} \sqrt{\frac{\xi_*}{17} \frac{\log_*}{70}}$$



String number density: dominant uncertainty from spectral index

strings per Hubble at QCD phase transition

log of Horizon scale versus PQ scale at QCD phase transition

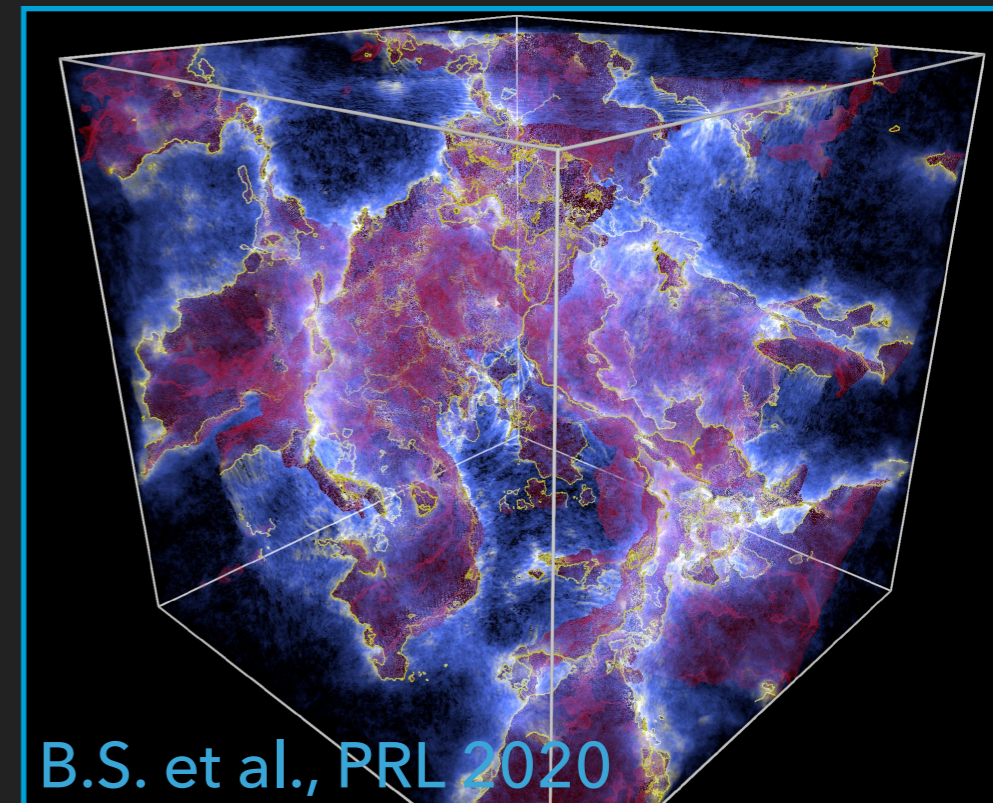
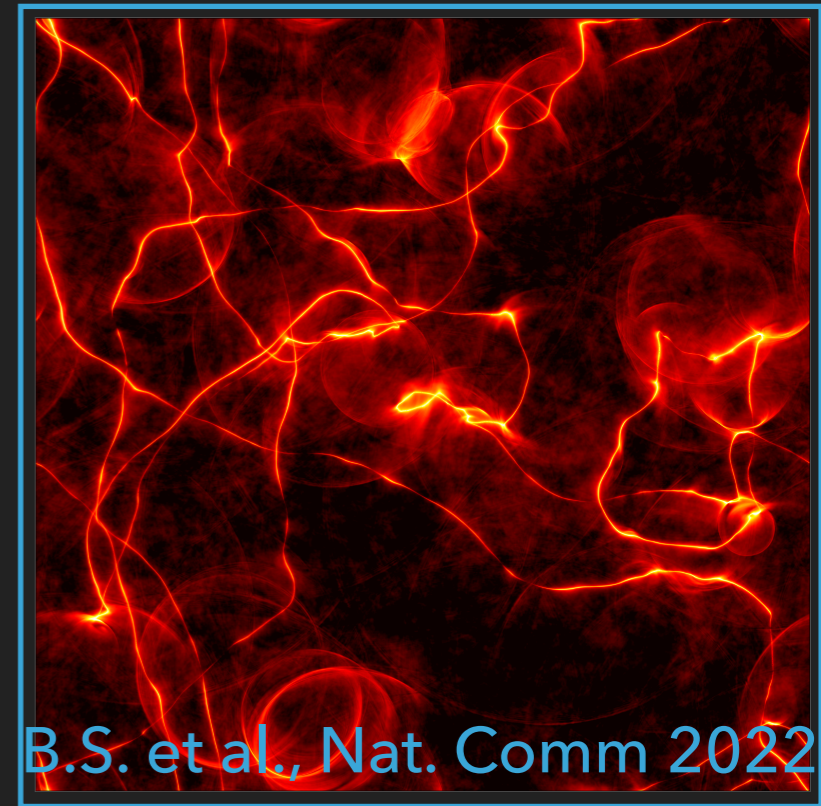


# The DM relic abundance

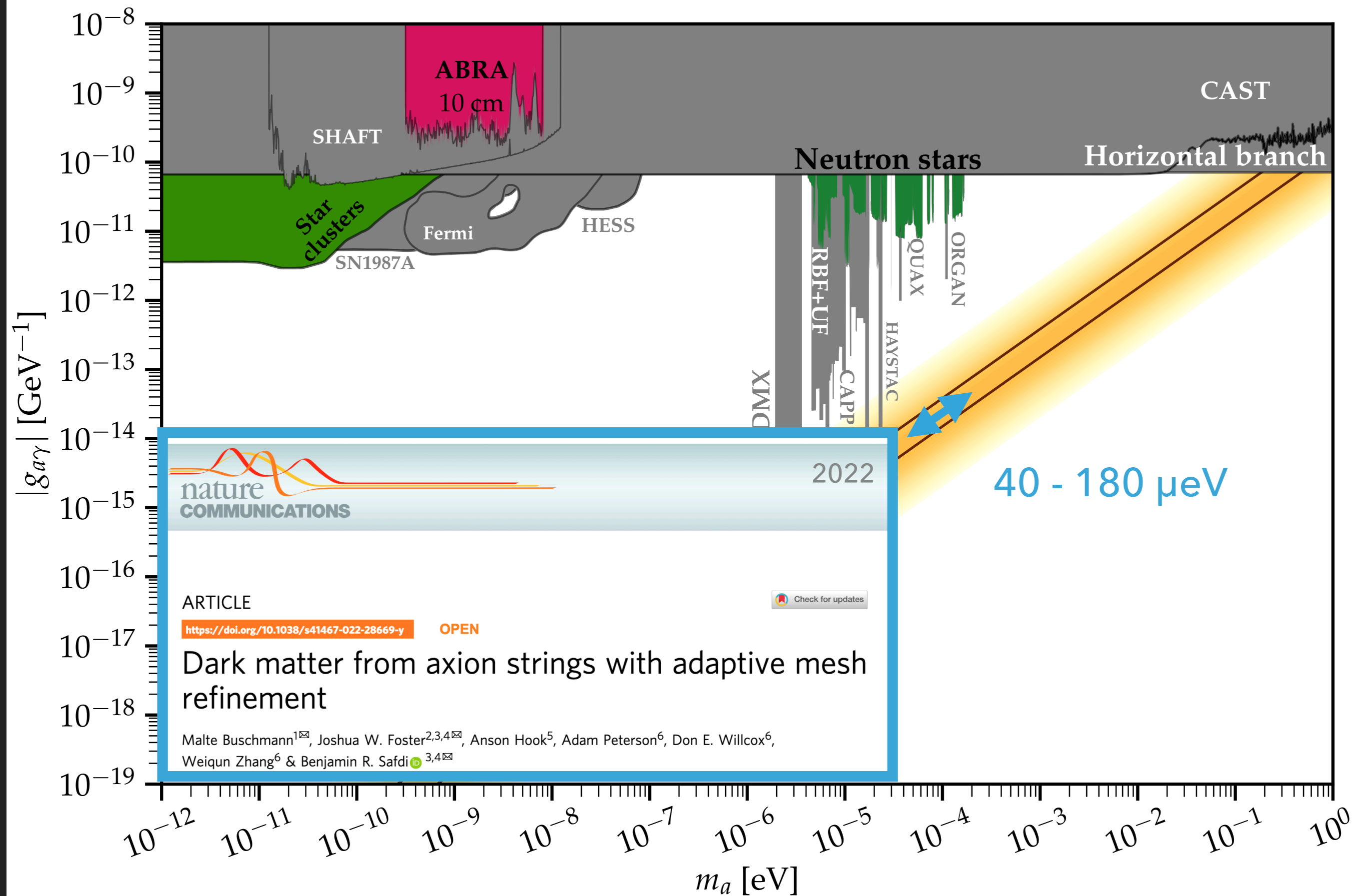
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String production prior to QCD phase transition dominates over contribution from QCD phase transition

$$\Omega_a^{\text{QCD}} \approx 0.017 h^{-2} (f_a / 4.3 \cdot 10^{10} \text{GeV})^{1.17}$$



# Our preferred mass range



## Caveats

1. Maybe we made a mistake (running larger sims now and more systematics, \*see next slide)
2. PQ symmetry broken before inflation
3. PQ symmetry broken after inflation by non-standard cosmology (e.g., early matter domination)
4. PQ symmetry broken after inflation but domain wall number great than one, domain walls stable, decay through explicit PQ breaking

Summary: should search over full possible mass range, but our work gives a special place to look



# What are we doing now?

## Perlmutter + GPU acceleration



1. GPU cluster being commission now. Already 5th most powerful supercomputer in world

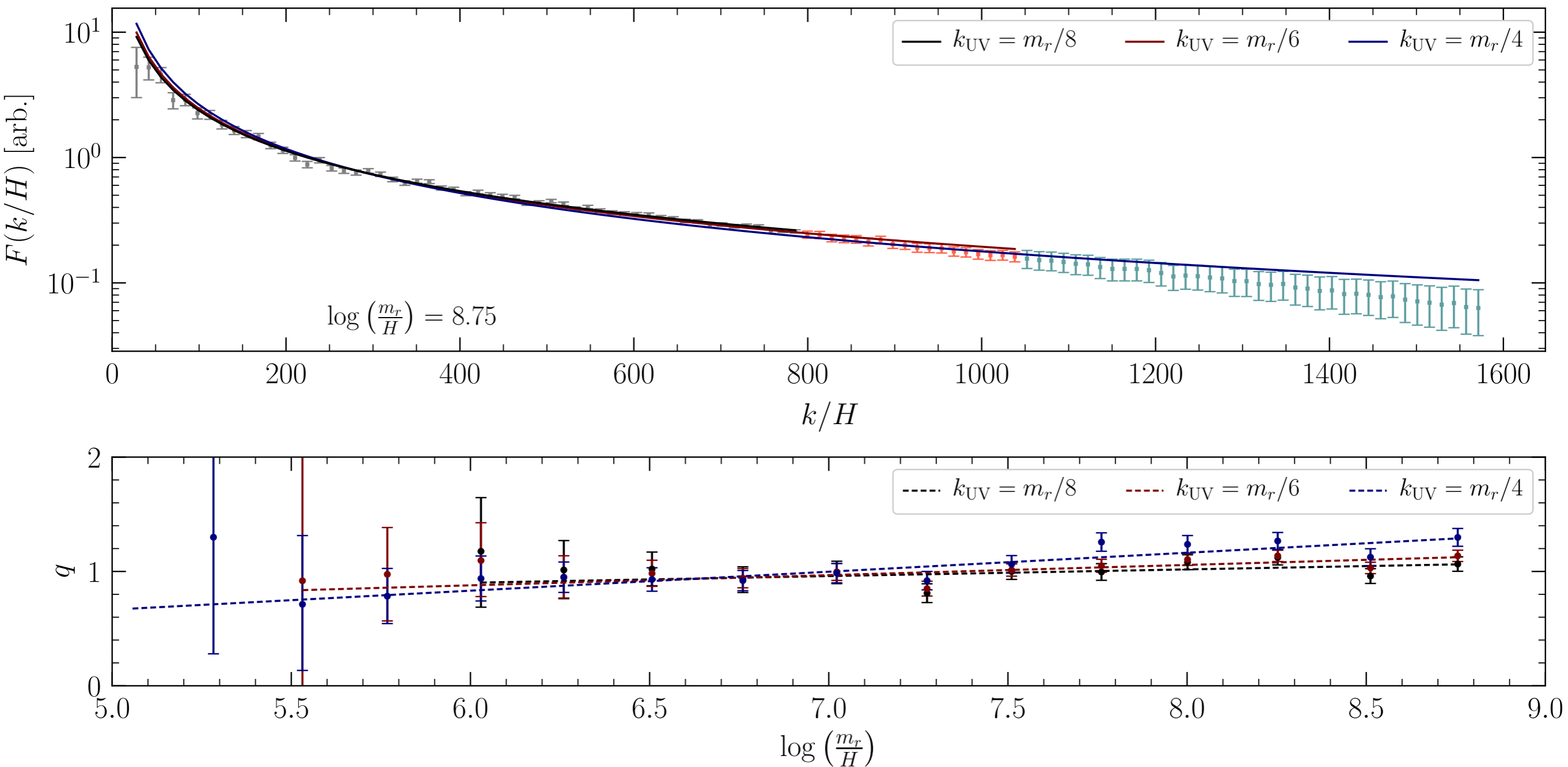
2. our plan: run on few thousand GPUs for increase in dynamic range

# QUESTIONS?

**\*SPECIAL THANKS TO LEAD AUTHORS  
MALTE BUSCHMANN AND JOSH FOSTER**

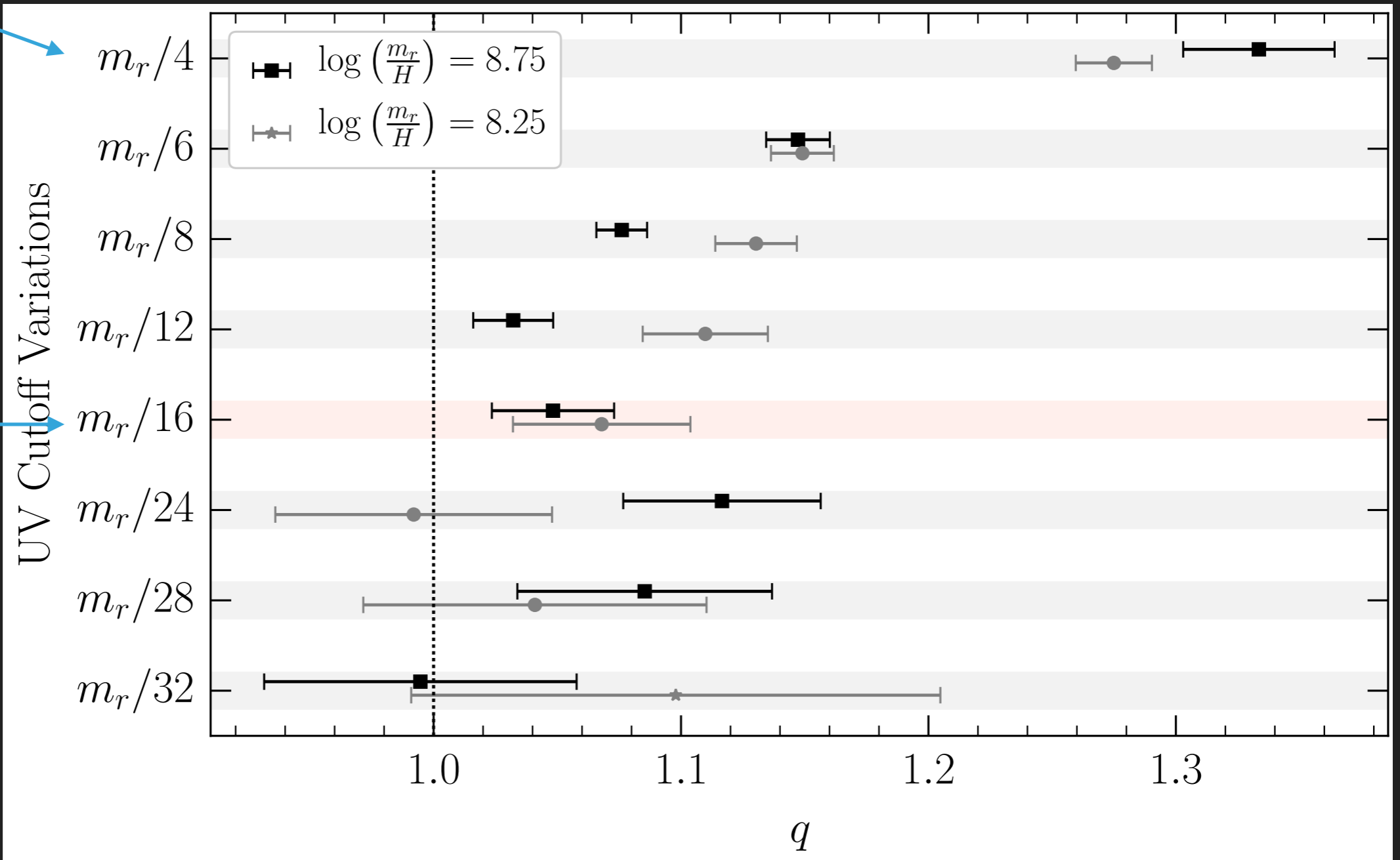
# Systematic Tests: UV cut-off in fitting $q$

Important to be far away from the UV cut-off when fitting power-law for  $q$



# Systematic Tests: UV cut-off in fitting $q$

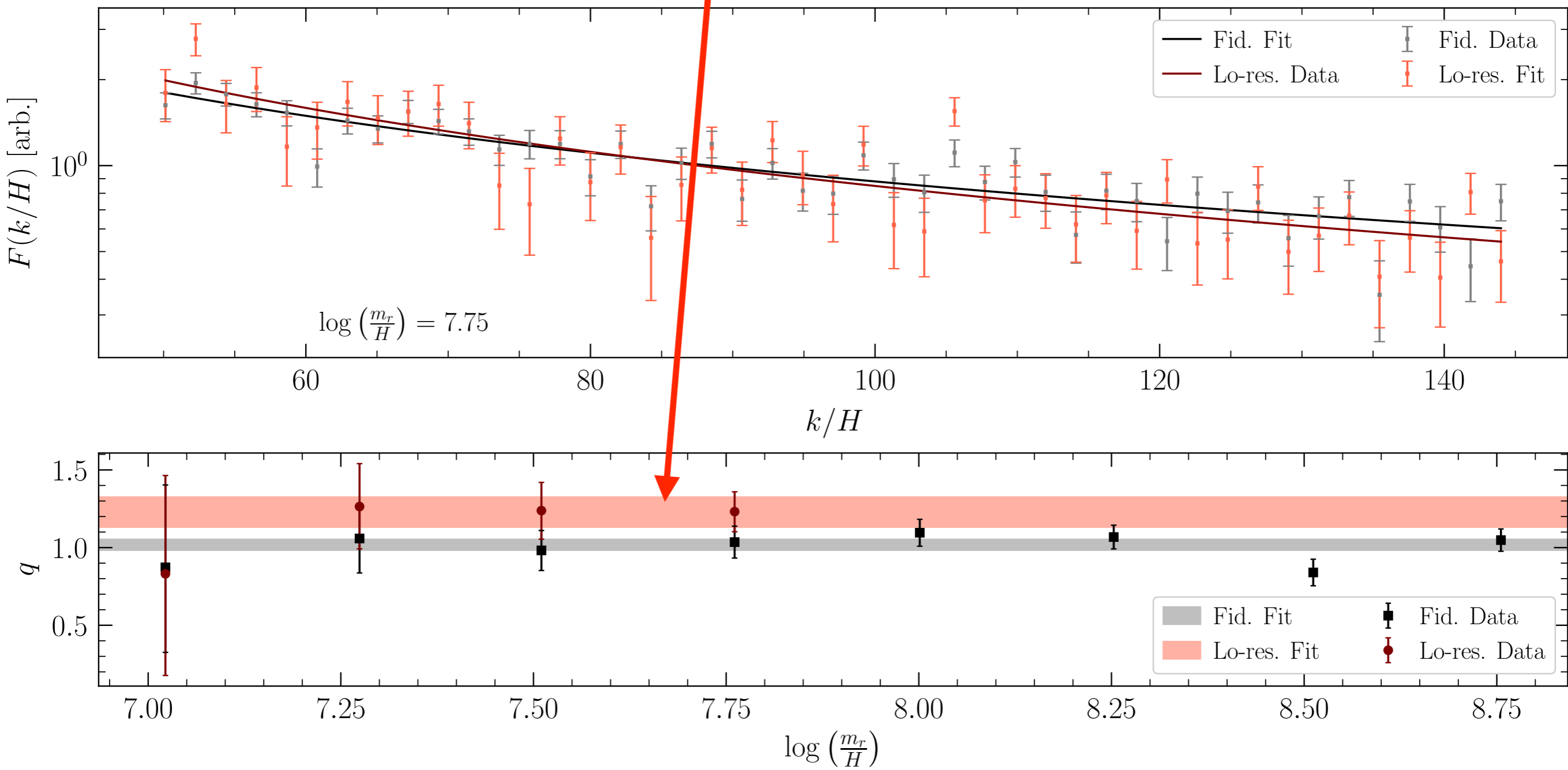
previous  
simulations



our work

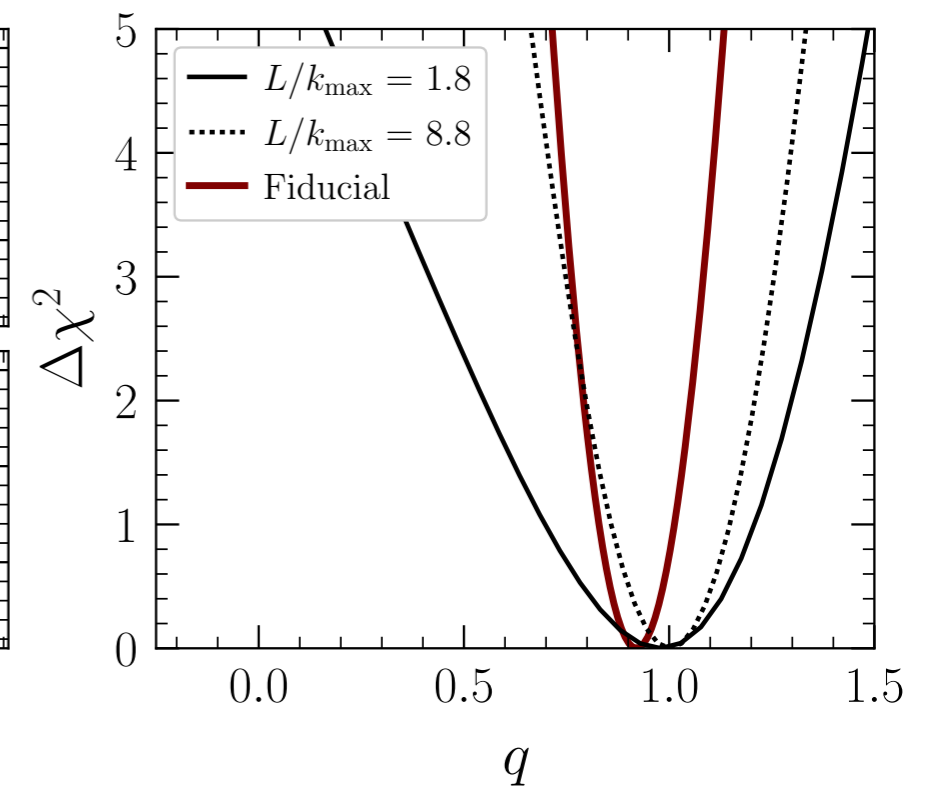
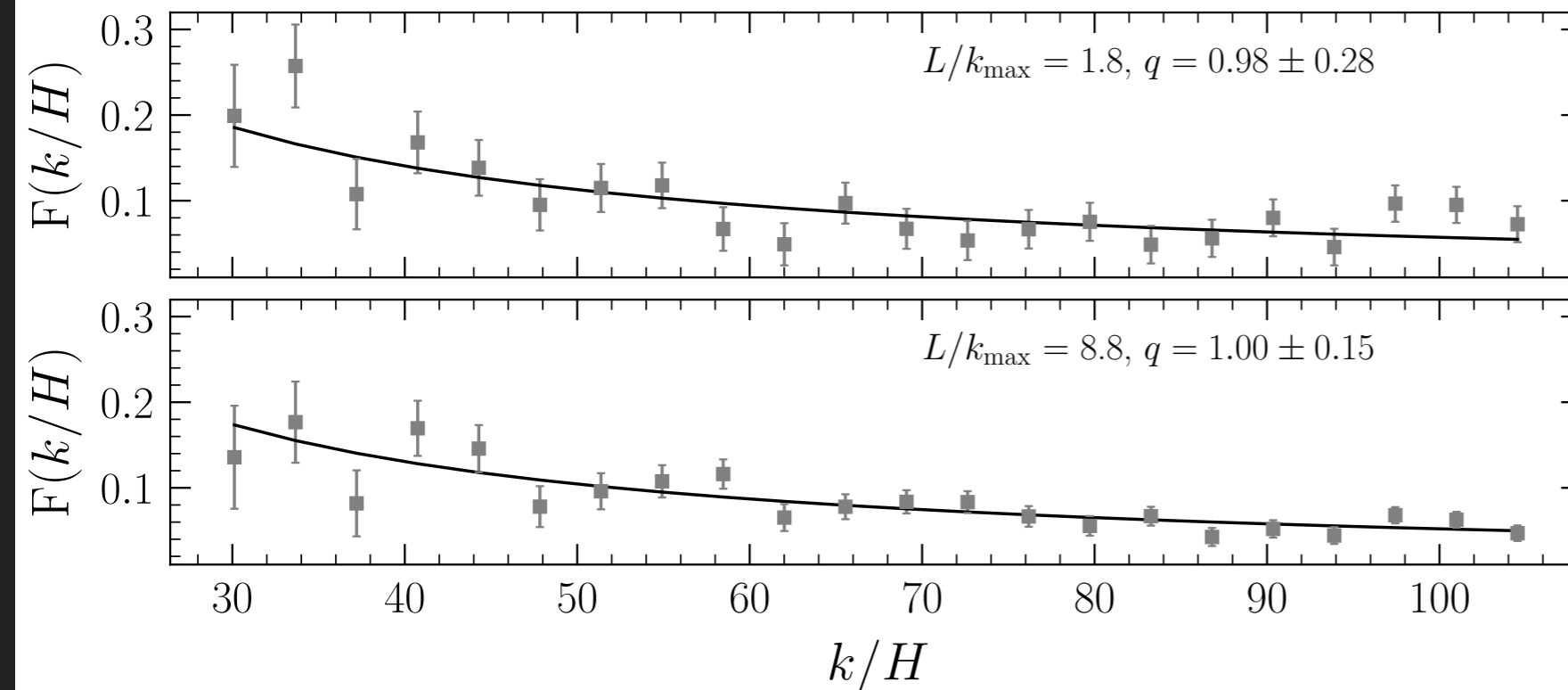
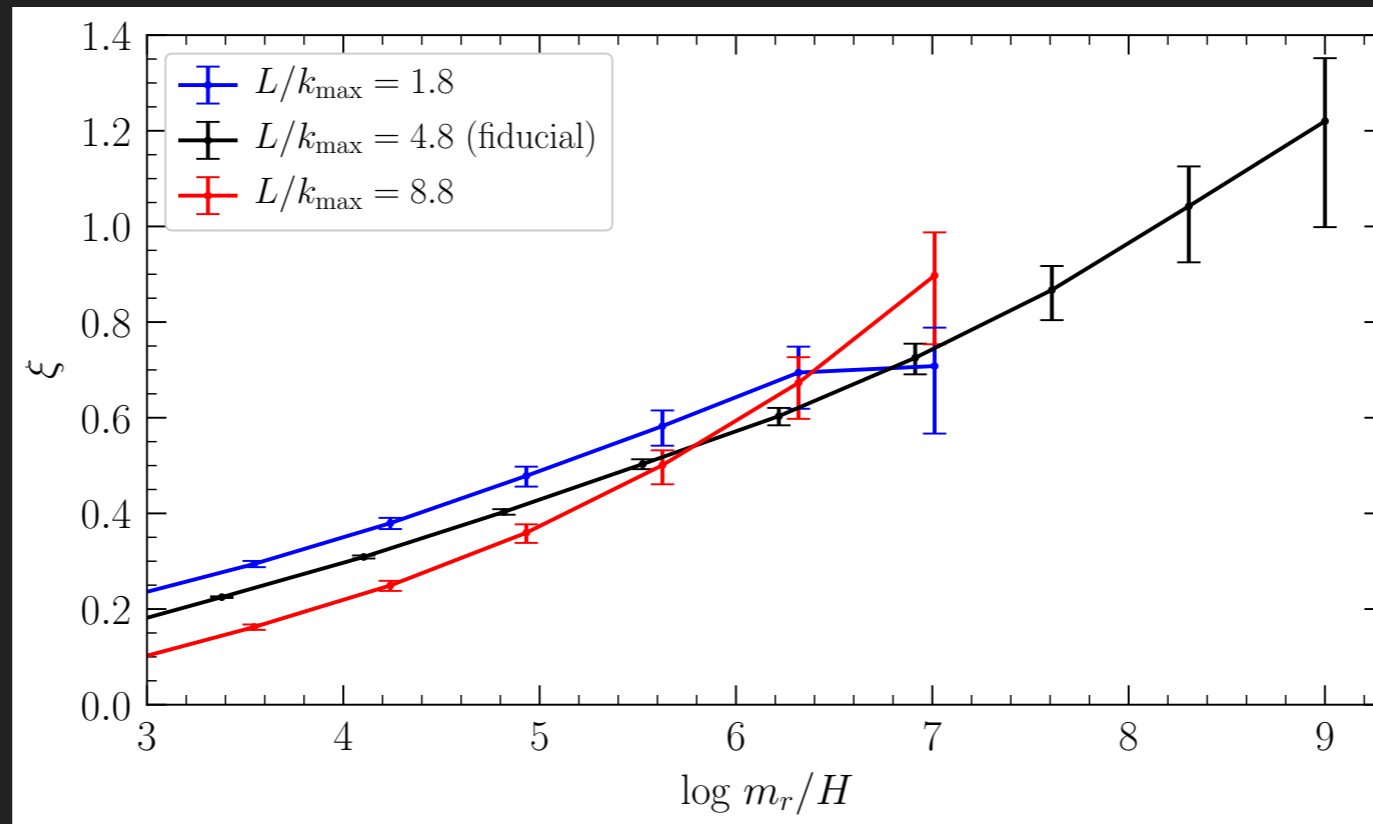
# Systematic Tests: resolving string cores

same simulation without refinement levels:  
resolve core by 1 grid site at the end

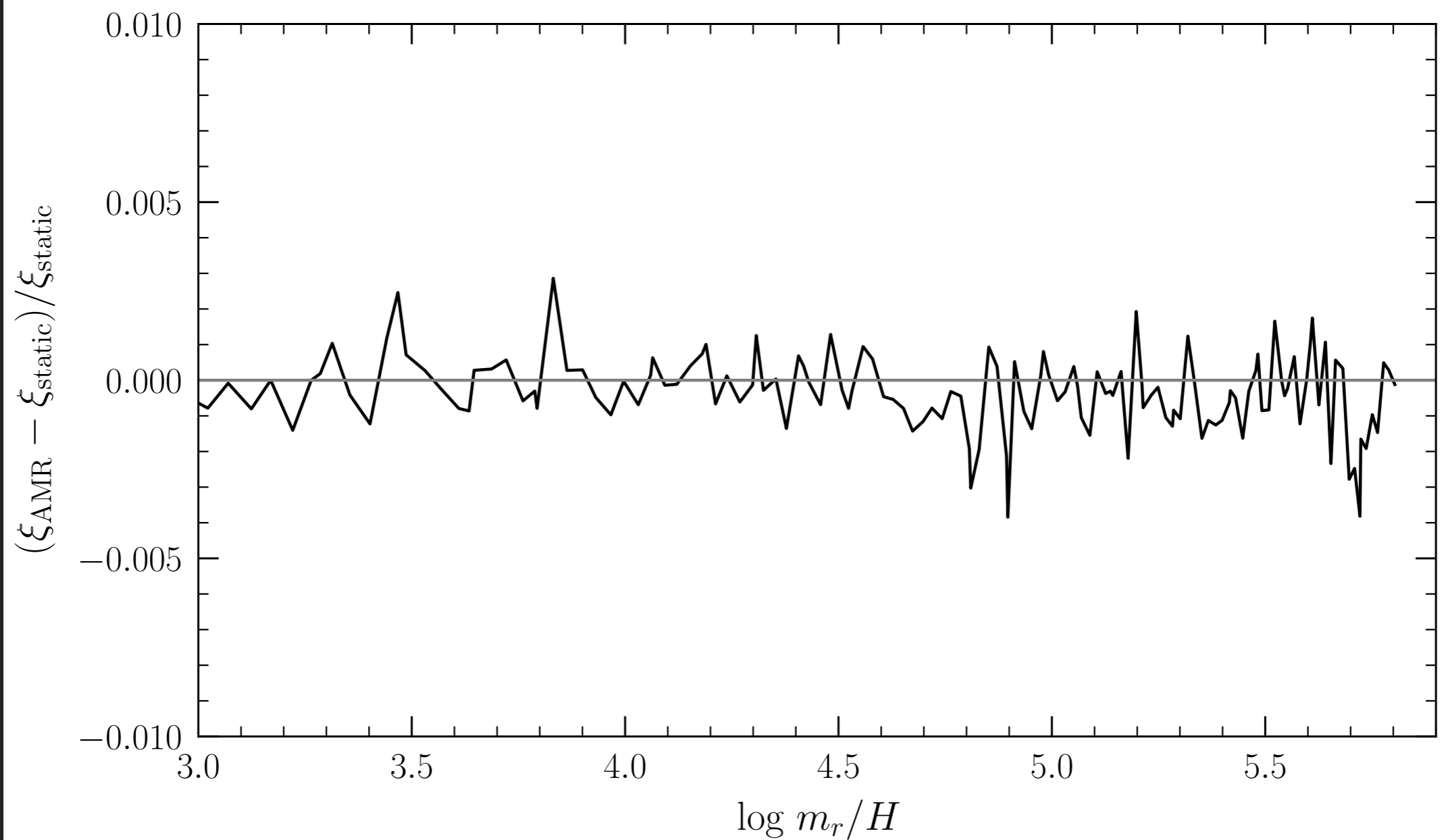


# Systematic Tests: results appear robust to initial conditions

\*performing more systematic tests now



# Systematic Tests: AMR and static lattice simulations give consistent results in range of validity



# Axion generated before inflation

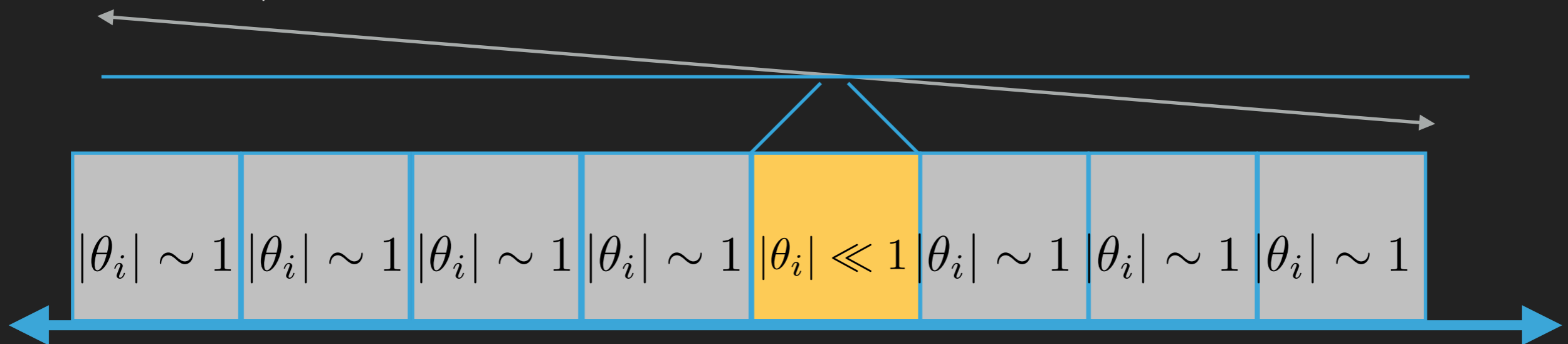
PHYSICAL REVIEW D 73, 023505 (2006)

## Dimensionless constants, cosmology, and other dark matters

Max Tegmark,<sup>1,2</sup> Anthony Aguirre,<sup>3</sup> Martin J. Rees,<sup>4</sup> and Frank Wilczek<sup>2,1</sup>

$f_a \sim 10^{15} - 10^{16}$  GeV produces too much DM for generic  $\theta_i$

$$\theta_i = a_i / f_a$$



Tegmark et al.: too much DM does not allow for life (and us!)

(Other solution high  $f_a$ : entropy dilution)