

Neutrino Flavor Conversion in Dense Astrophysical Environments

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Presentation outline

The presentation is organized as follows:

- **Part I:** Introduction
- **Part II:** Matter-neutrino resonances*
 - Basic questions: What are they? Where do they occur? Consequences?
 - Interesting scenarios (numerical examples)
- **Part III:** Conclusions

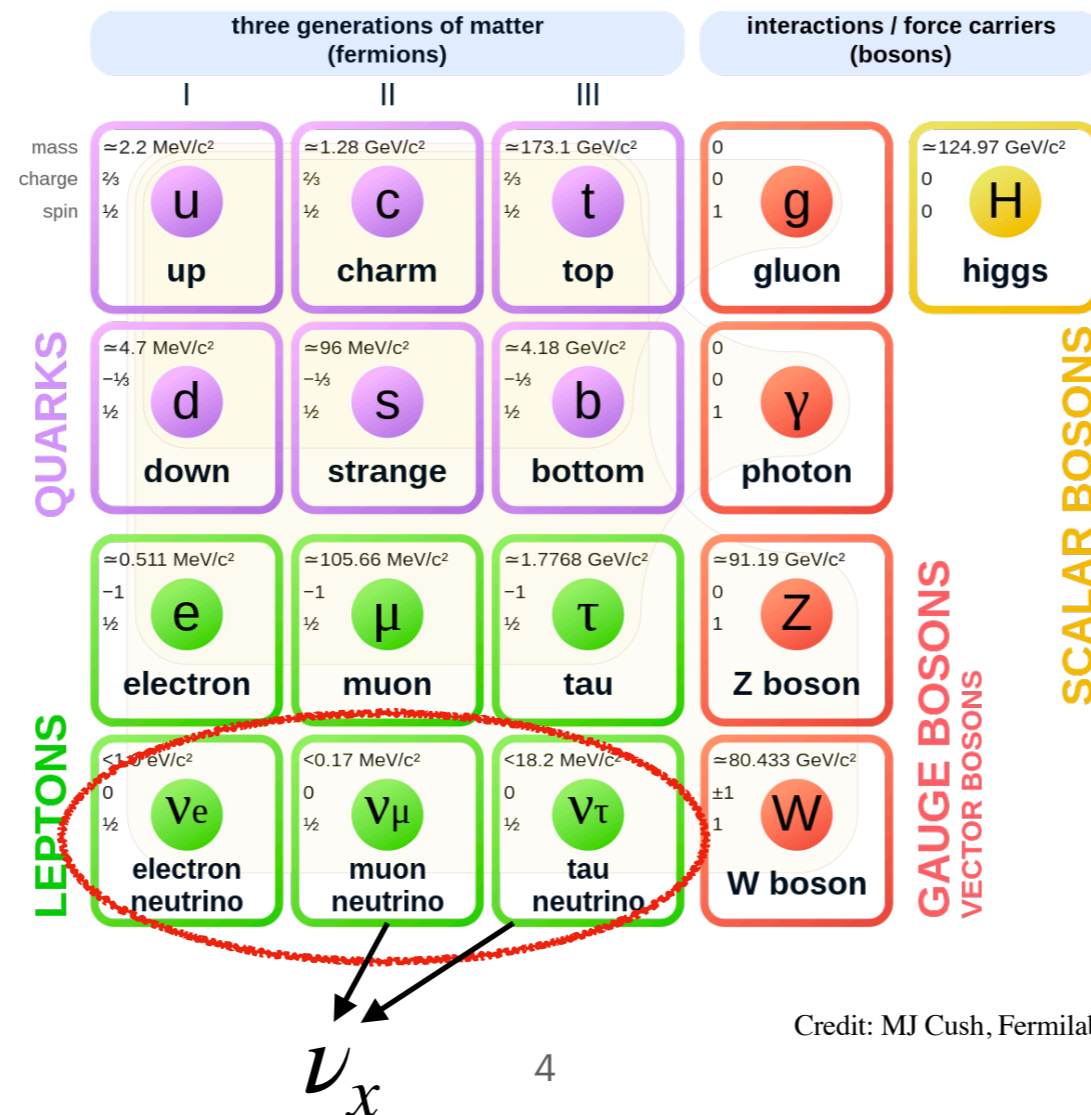
*Not to be confused with the MSW resonant effect

Part I

Introduction

Neutrinos are fun

- Neutrinos are neutral fermions (spin 1/2)
- Tiny masses and weak coupling to matter
- Three families of neutrinos



Credit: MJ Cush, Fermilab

Neutrino oscillations in vacuum

The diagram shows the equation $|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$ enclosed in a white box. A blue arrow points from the left side of the box to the label "Flavor eigenstate". A green arrow points from the middle of the box to the label "Lepton mixing matrix (PMNS)". A red arrow points from the right side of the box to the label "Mass eigenstate".

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$$

Flavor eigenstate

Lepton mixing matrix (PMNS)

Mass eigenstate

Mass eigenstates evolve with different phases \rightarrow neutrino oscillations

Neutrino oscillations in vacuum

$$|\nu_\alpha\rangle = \sum_j U_{\alpha j}^* |\nu_j\rangle$$

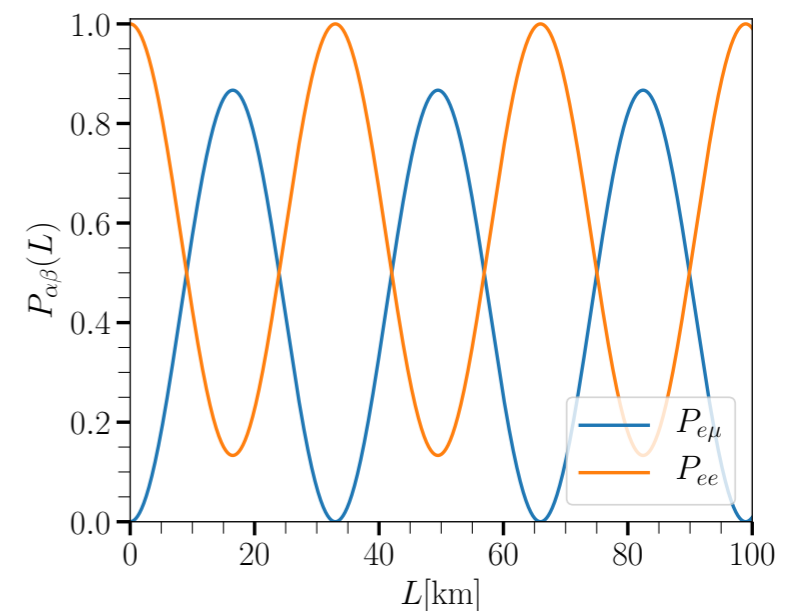
↪ Flavor eigenstate
 ↪ Lepton mixing matrix (PMNS)
 ↪ Mass eigenstate

Mass eigenstates evolve with different phases → neutrino oscillations

Transition probability
(two-flavor)

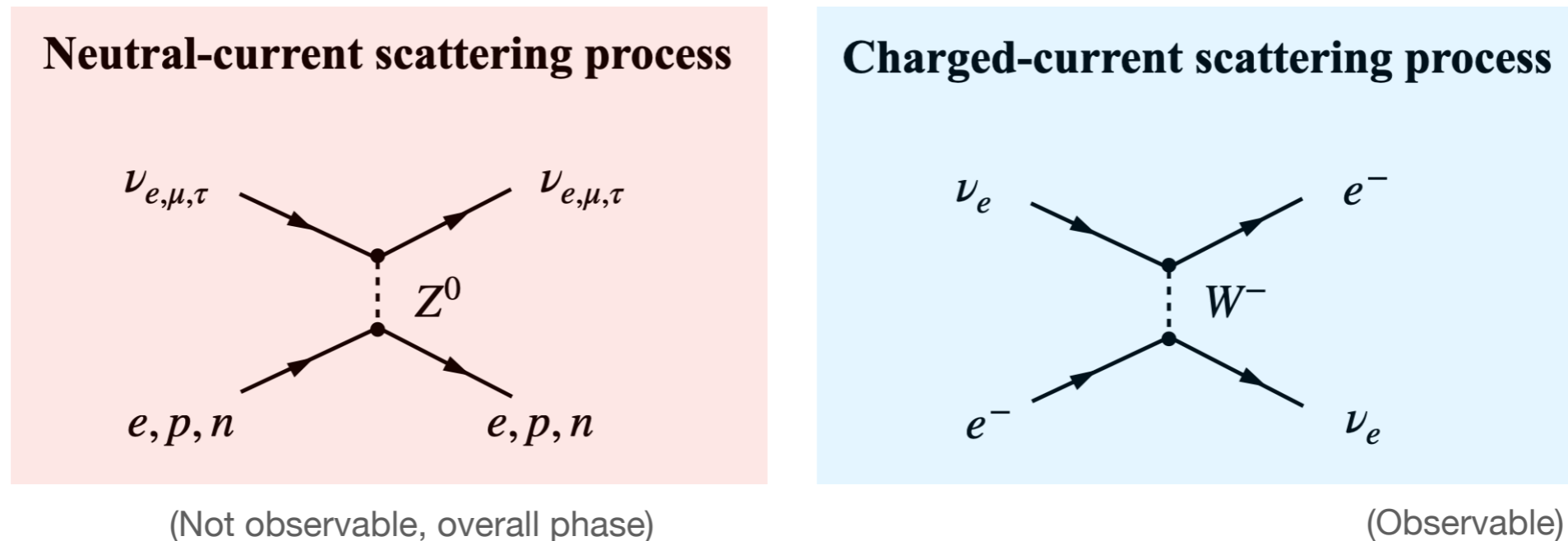
$$P_{e\mu}(L) = \sin^2 2\theta \sin^2\left(\frac{\Delta m^2}{4E} L\right)$$

↗ amplitude ↗ frequency



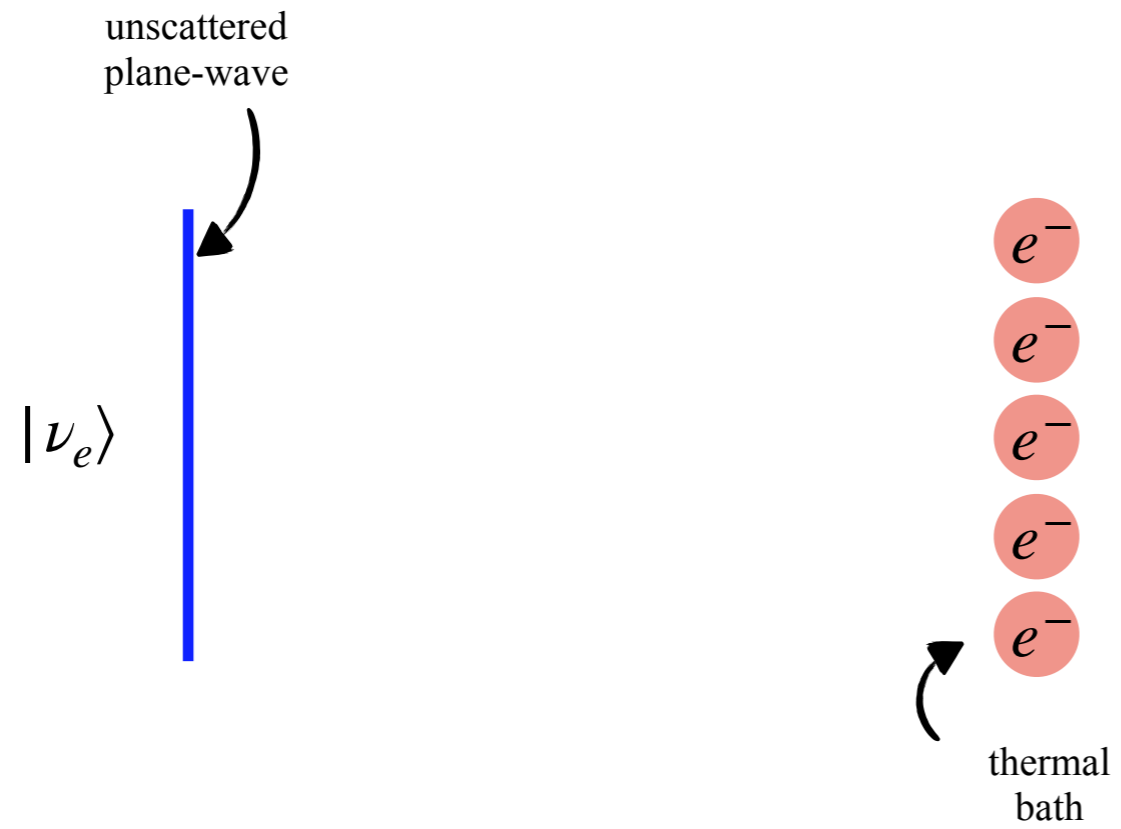
Neutrino oscillations in matter

- Matter background (e, p, n) modify how neutrinos oscillate inside the astrophysical source

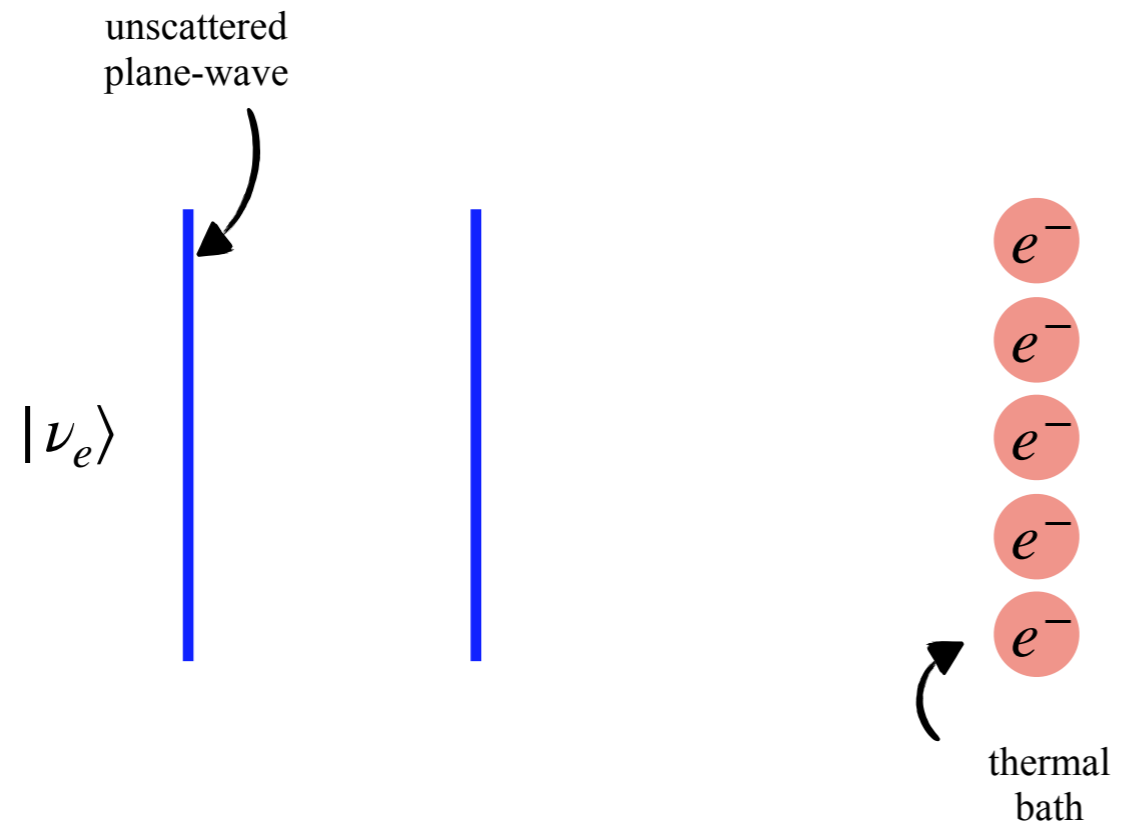


- Neutrinos undergo *coherent forward scattering* with particles in the background

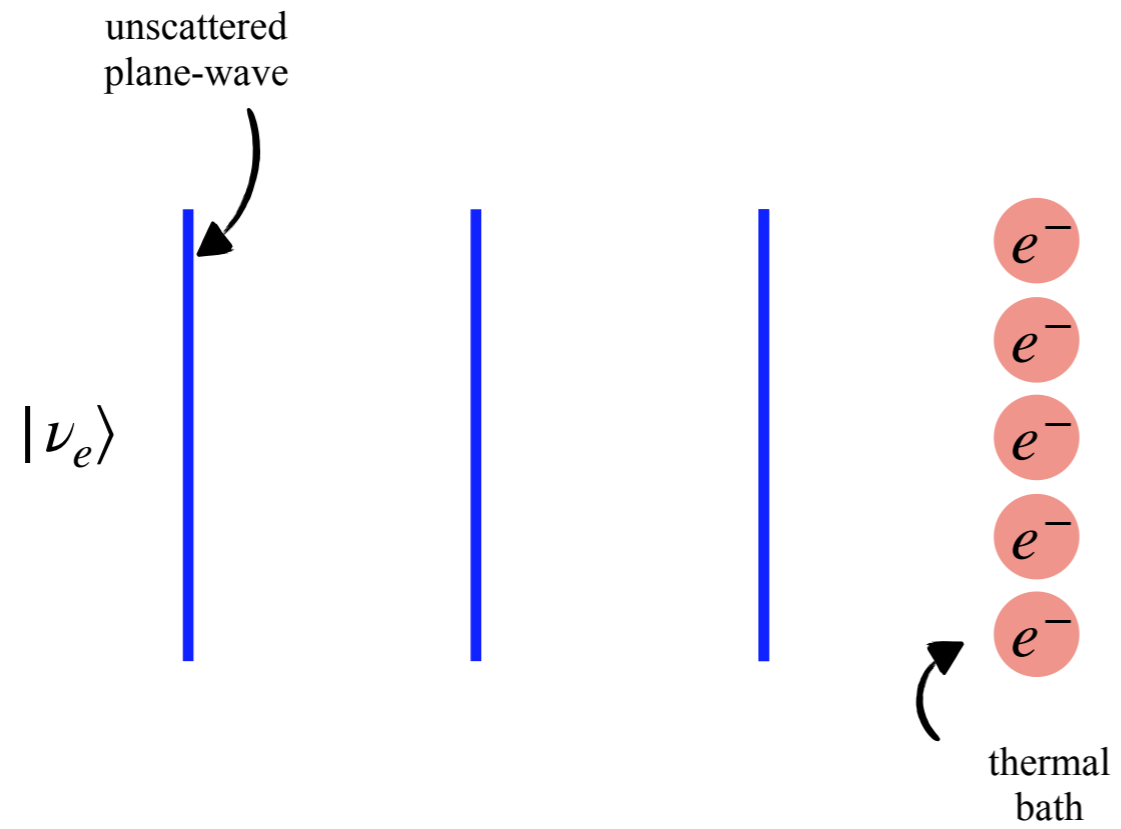
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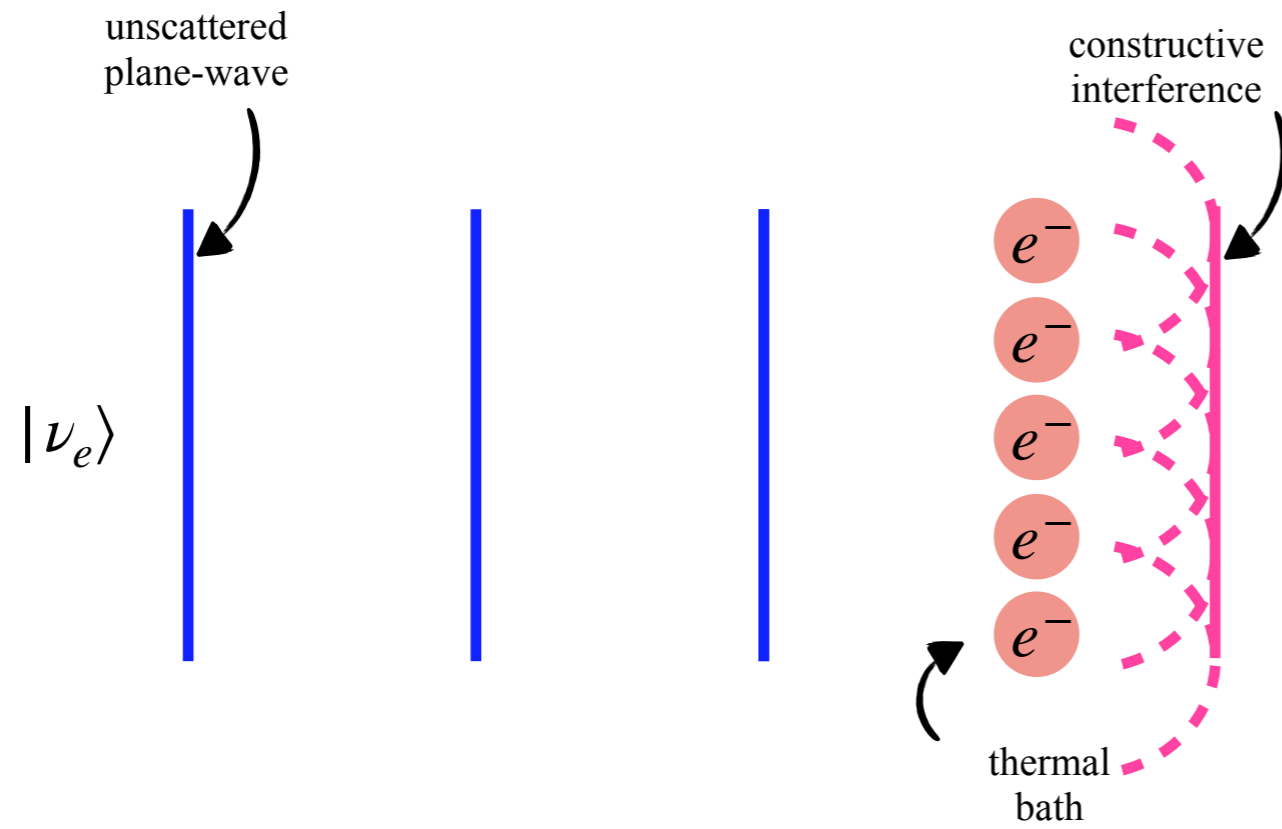
Neutrino oscillations in matter



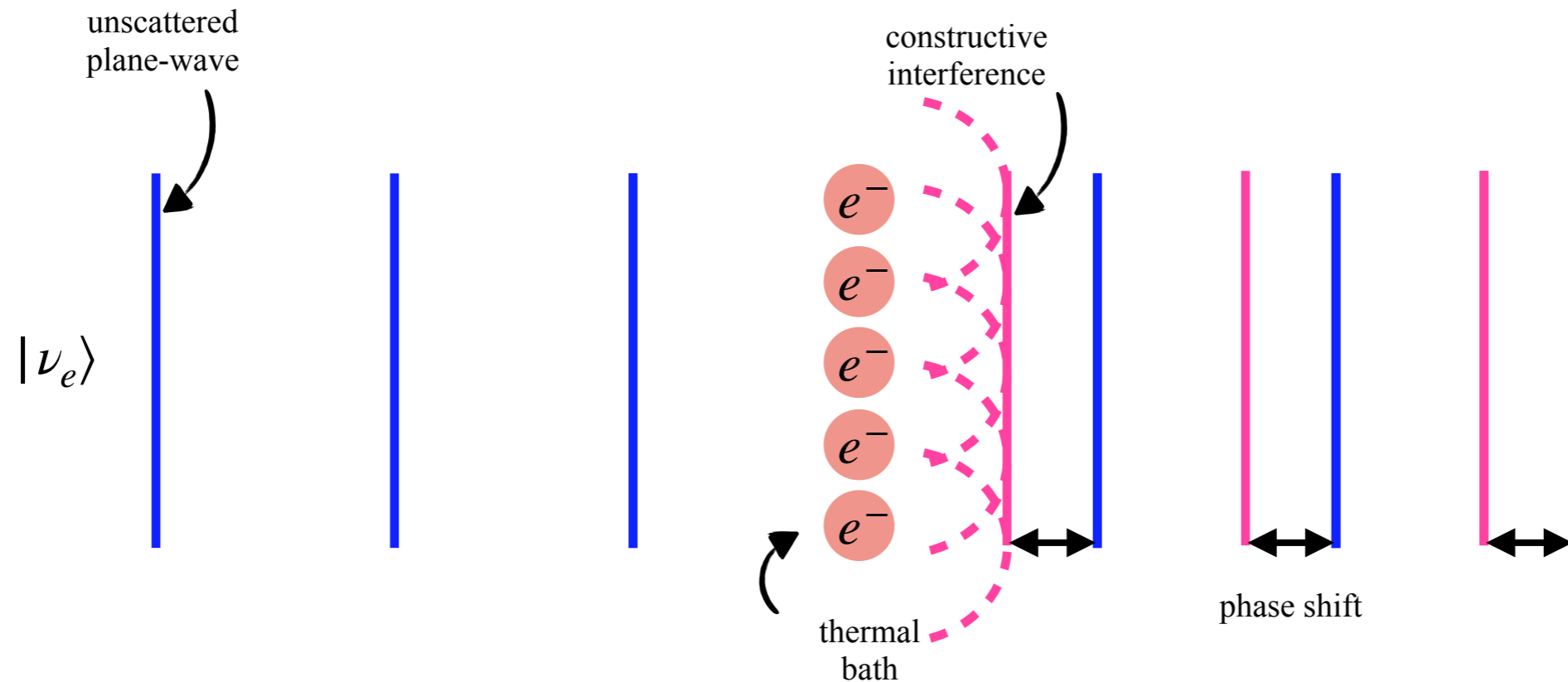
Neutrino oscillations in matter



Neutrino oscillations in matter



Neutrino oscillations in matter



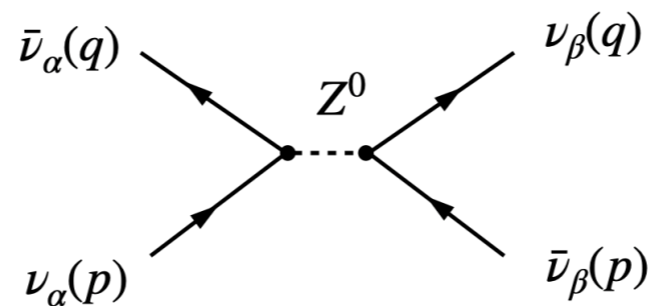
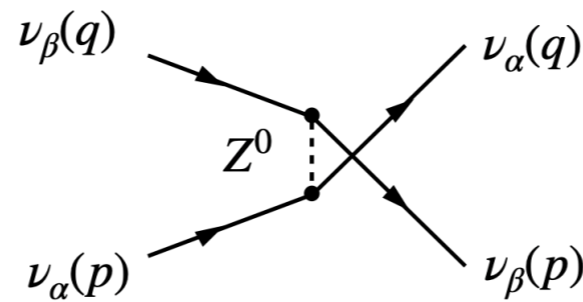
- Phase shift \rightarrow Mikheyev-Smirnov-Wolfenstein (MSW) resonant effect^{1,2}
- Neutrinos experience a potential $V_{CC} = \sqrt{2}G_F n_e$ (refraction)

¹Neutrino Oscillations in Matter, Wolfenstein, Phys. Rev. D 17, 2369 (1978)

²Resonant amplification of neutrino oscillations in matter and solar neutrino spectroscopy, Mikheev & Smirnov, Nuovo Cim.C 9 (1986) 17-26

Neutrino-neutrino interaction

- Neutrinos also constitute a background for other neutrinos
- Neutrino-neutrino interaction induces *collective oscillations*¹⁻⁵



¹Neutrino oscillations at high densities, Pantaleone, Physics Letters B 287 (1992) 128-132

²Collective Neutrino Oscillations, Duan et al, Ann. Rev. Nucl. Part. Sci. 60:569 (2010)

³Supernova Neutrinos: Production, Oscillations and Detection, Mirizzi et al, Rivista del Nuovo Cimento Vol. 39, N. 1-2 (2016)

⁴Collective neutrino flavor conversion: Recent developments, Chakraborty et al, 1602.02766

⁵New Developments in Flavor Evolution of a Dense Neutrino Gas, Tamborra et al, Ann. Rev. Nucl. Part. Sci. 71 (2021) 165-188

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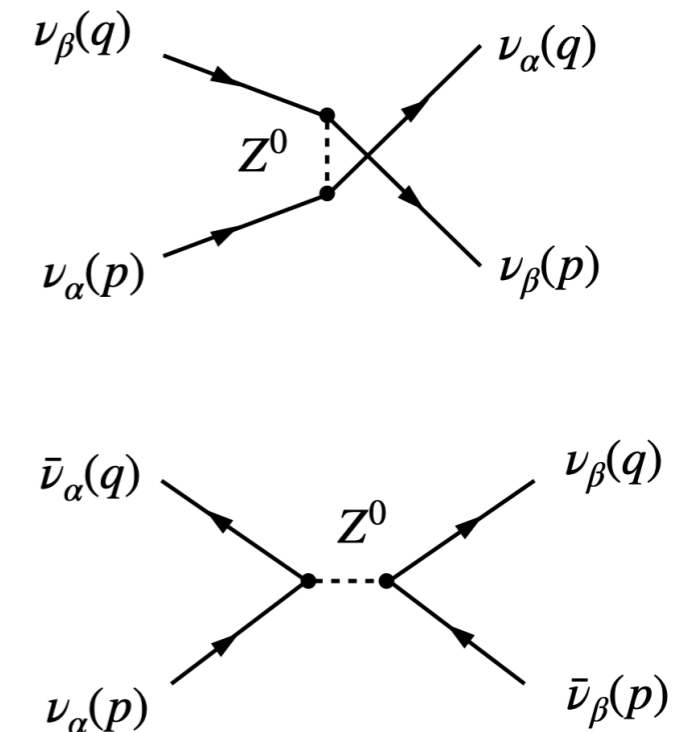
Momentum of test neutrino

$$H_{\nu\nu}(\vec{p}) = \sqrt{2}G_F n_\nu \int d\vec{q} [\rho(\vec{q}) - \bar{\rho}(\vec{q})] \left(1 - \frac{\vec{p} \cdot \vec{q}}{|\vec{p}| |\vec{q}|}\right)$$

Neutrino interaction strength ("μ")

Momentum of background neutrino

Density matrices for ν and $\bar{\nu}$



- *Non-linear* behavior of flavor evolution and *collective* conversion

¹Neutrino oscillations at high densities, Pantaleone, Physics Letters B 287 (1992) 128-132

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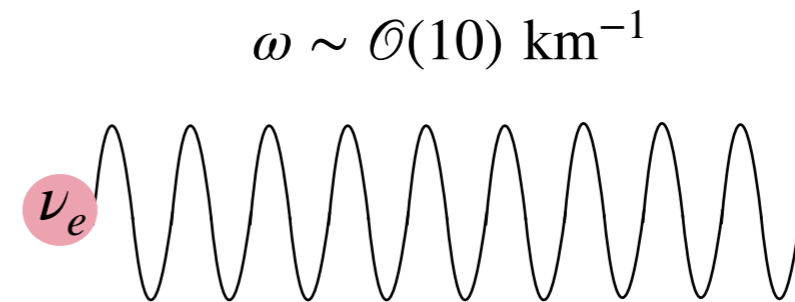
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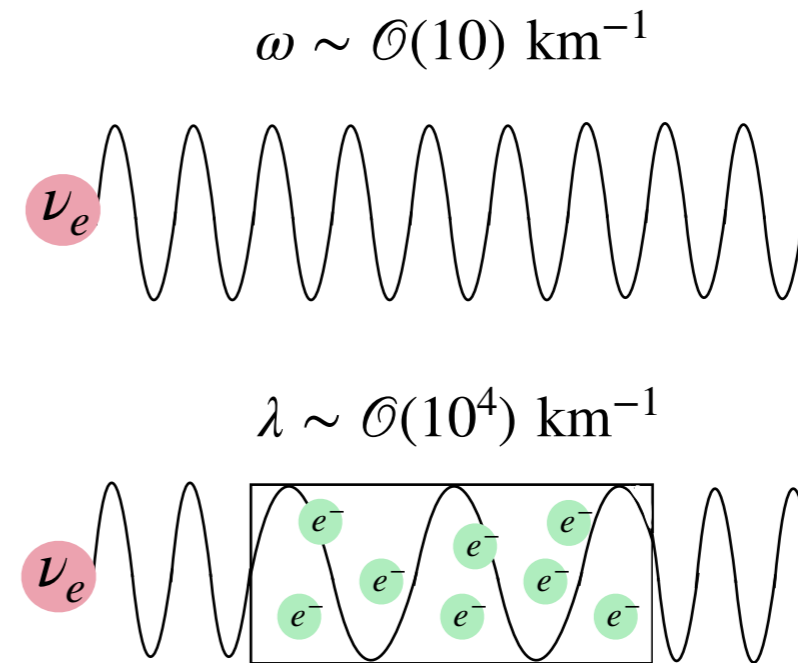
Neutrino flavor conversion

- **Vacuum oscillations** - driven by Δm^2



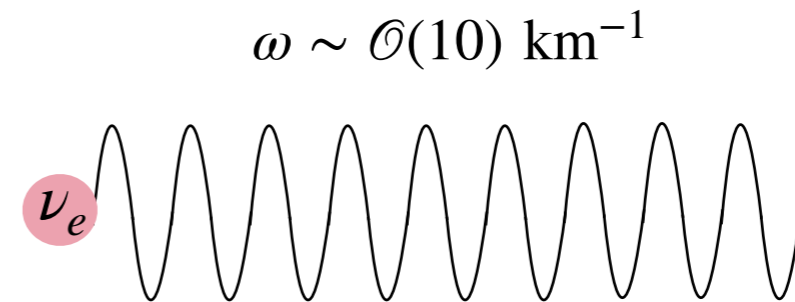
Neutrino flavor conversion

- **Vacuum oscillations** - driven by Δm^2
- **Neutrino-matter interaction** - coherent forward scattering with electrons (i.e. MSW effect)

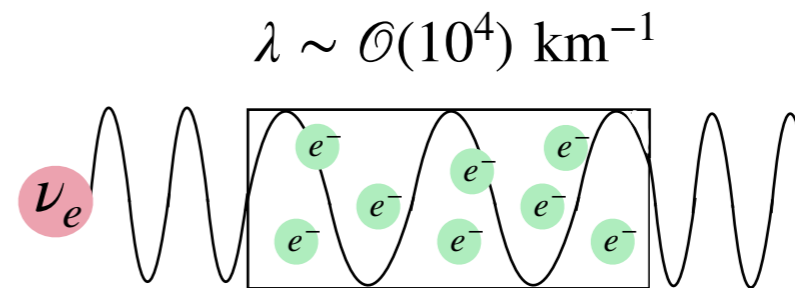


Neutrino flavor conversion

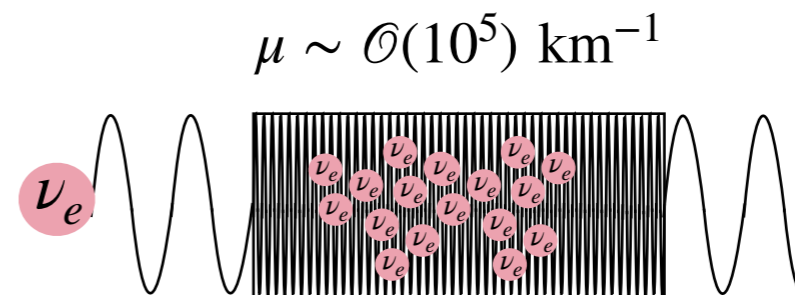
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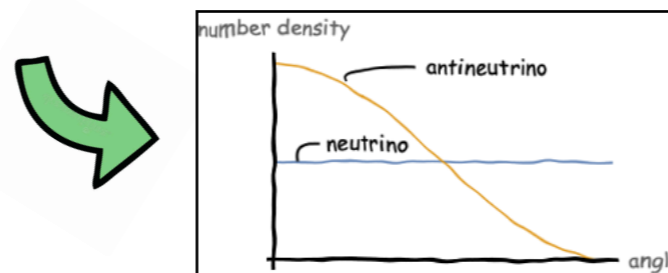
- **Neutrino-matter interaction** - coherent forward scattering with electrons (i.e. MSW effect)



- **Neutrino-neutrino interaction**— coherent forward scattering with background neutrinos \rightarrow *Collective flavor conversion*



Key inputs: **angular distributions of ν_e and $\bar{\nu}_e$**

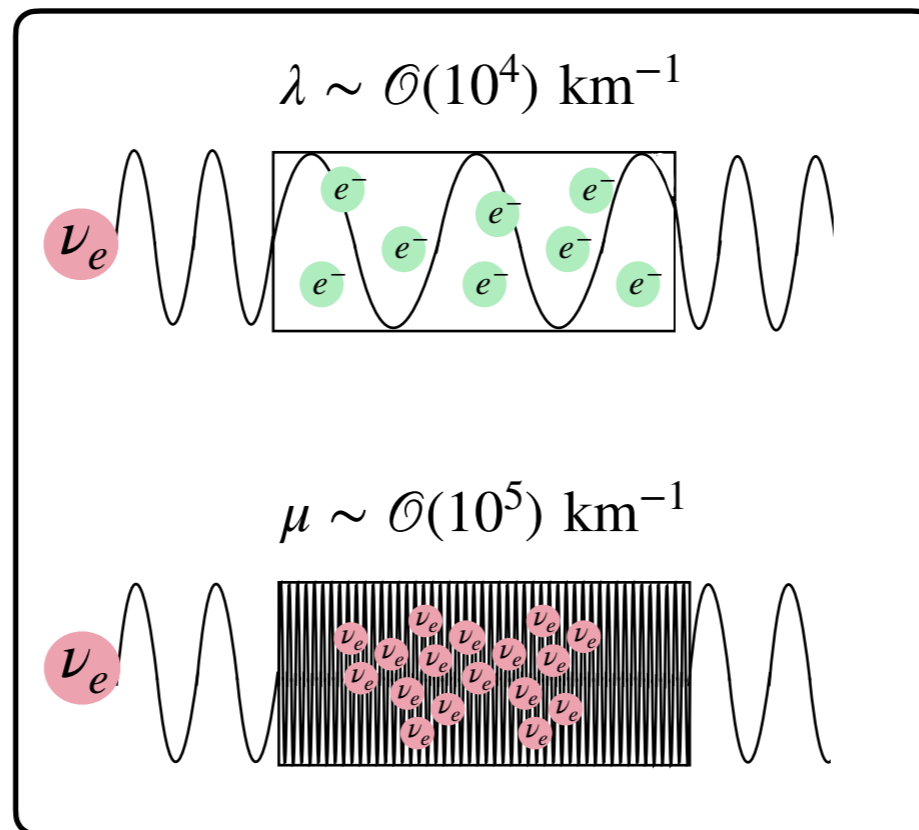


Determines the flavor dynamics

Neutrino flavor conversion

These two can interfere roughly when $\mu \sim \lambda$

Neutrino-matter interaction



Neutrino-neutrino interaction

(second part of the talk)

Collective neutrino conversion

- Neutrinos with different momenta evolve collectively
- The (mean-field) equations of motion describing neutrino flavor conversion are:

$$\left(\frac{\partial}{\partial t} + \vec{v} \cdot \vec{\nabla}_x \right) \rho(\vec{x}, \vec{p}, t) =$$

$$\left(\frac{\partial}{\partial t} + \underbrace{\vec{v} \cdot \vec{\nabla}_x}_{\text{advection}} \right) \bar{\rho}(\vec{x}, \vec{p}, t) =$$

Spatial variations¹

¹Neutrino propagation hinders fast pairwise flavor conversions, Shalgar, **Padilla-Gay** & Tamborra, *JCAP* 06 (2020) 048

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Coherent forward scattering²

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²Neutrino Flavor Pendulum Reloaded: The Case of Fast Pairwise Conversion, **Padilla-Gay**, Tamborra & Raffelt, *Phys.Rev.Lett.* 128 (2022)

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Spatial variations¹

Coherent forward scattering²

Non-forward scattering^{3,4}

¹Neutrino propagation hinders fast pairwise flavor conversions, Shalgar, **Padilla-Gay** & Tamborra, *JCAP* 06 (2020) 048

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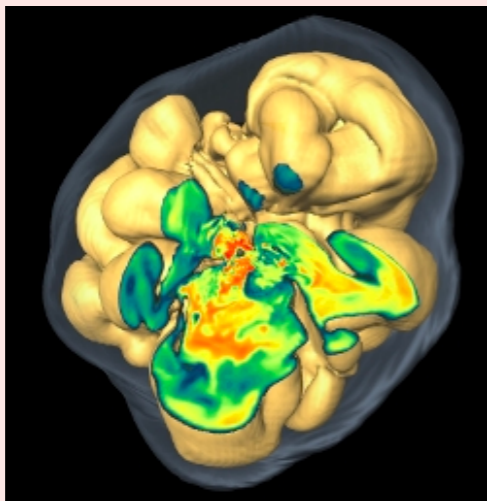
³Neutrino fast flavor pendulum. II. Collisional damping, **Padilla-Gay**, Tamborra & Raffelt, *Phys.Rev.D* 106 (2022) 10, 103031

⁴Collisions and collective flavor conversion: Integrating out the fast dynamics, Fiorillo, **Padilla-Gay** & Raffelt, 2312.07612

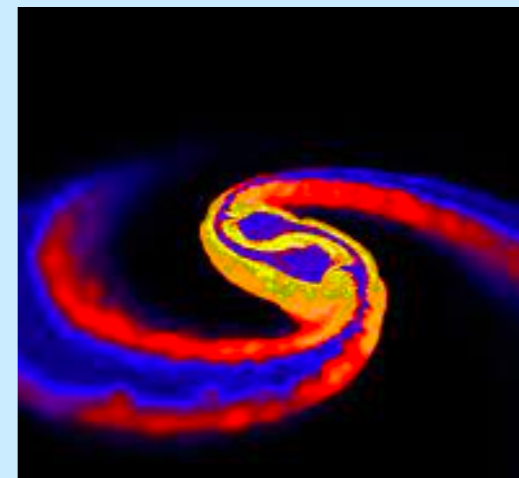
Neutrinos in dense astrophysical environments

Copiously produced $\sim 10^{58}$ neutrinos (MeV)

In core-collapse supernovae:



In compact binary mergers:

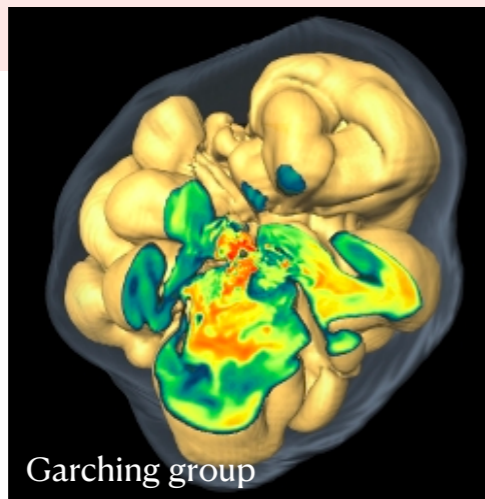


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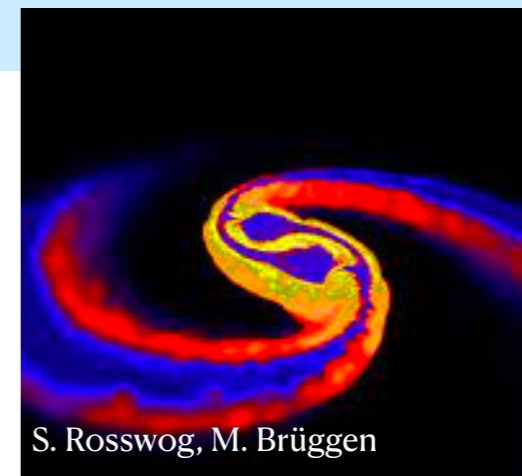
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In core-collapse supernovae:

- Neutrinos carry 99% of the grav. energy
- Neutrinos can revive the stalled shock¹
- More ν_e than $\bar{\nu}_e$ (neutronization burst)²



In compact binary mergers:



¹Revival of a stalled supernova shock by neutrino heating, Bethe & Wilson, Astrophysical Journal, 1985, p. 14-23.

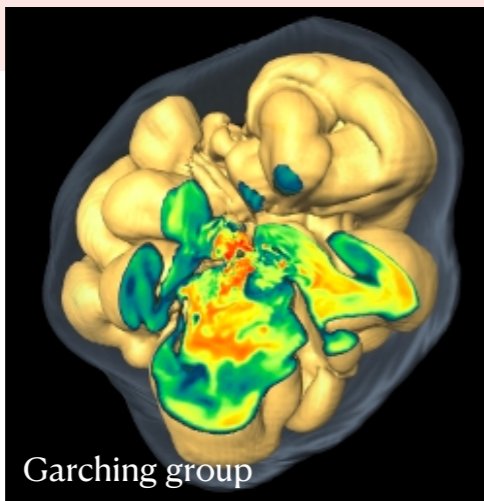
²Theory of Core-Collapse Supernovae, Janka et al, Phys.Rept.442:38-74, 2007

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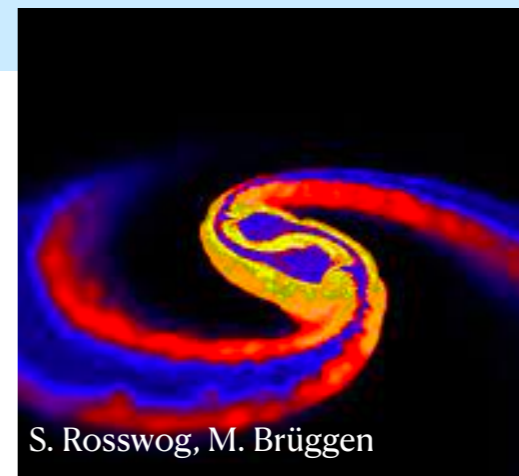
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- Neutrinos cool the disk
- Neutrinos dominate the ejecta in polar region
- More $\bar{\nu}_e$ than ν_e (n-rich, merger protonizes)³



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³Coalescing neutron stars, Ruffert, Janka & Takahashi, Astronomy and Astrophysics, v.319, p.122-153

Neutrinos in dense astrophysical environments

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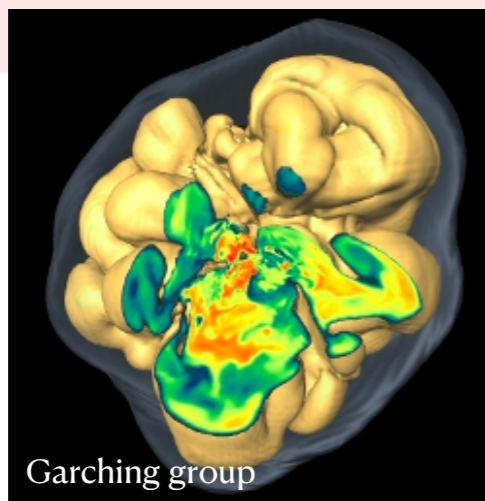
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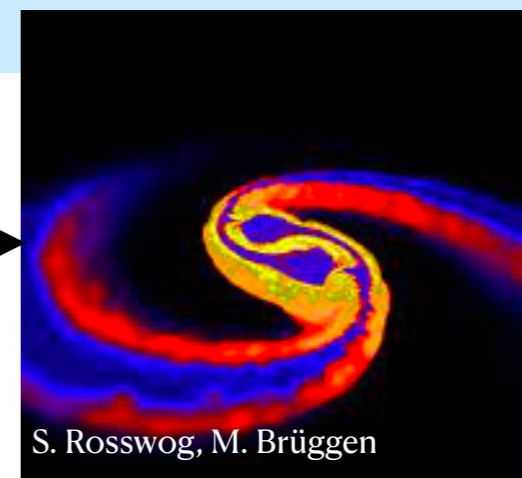
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○ ν 's affect nucleosynthesis⁴⁻⁷
(set Y_e)



Flavor dependent
processes



¹Revival of a stalled supernova shock by neutrino heating, Bethe & Wilson, *Astrophysical Journal*, 1985, p. 14-23.

²Theory of Core-Collapse Supernovae, Janka et al, *Phys.Rept.*442:38-74, 2007

³Coalescing neutron stars, Ruffert, Janka & Takahashi, *Astronomy and Astrophysics*, v.319, p.122-153

⁴Nucleosynthesis in Supernovae, Hoyle & Fowler (1960), *Astrophysical Journal*, vol. 132, p.565

⁵r-Process in Neutron Star Mergers, Freiburghaus, Rosswog & Thielemann, C. Freiburghaus et al 1999 *ApJ* **525** L121

⁶Enhanced triple- α reaction reduces proton-rich nucleosynthesis in supernovae, Jin, Roberts, Austin & Schatz, *Nature* volume 588, (2020)

⁷Successful vp-process in neutrino-driven outflows in core-collapse supernovae, A. Friedland, P. Mukhopadhyay, A. Patwardhan, 2312.03208

What are we missing?

- Full solution of quantum neutrino transport
- Implementation of neutrino conversion in hydrodynamical simulations
- Self-consistent treatment of neutrino conversion within nucleosynthesis networks



Part II

Matter-neutrino Resonances (MNR)

Ian Padilla-Gay, Shashank Shalgar, Irene Tamborra, *Symmetry breaking due to multi-angle matter-neutrino resonance in neutron star merger remnants*, [arXiv:24XX.XXXXX](#)

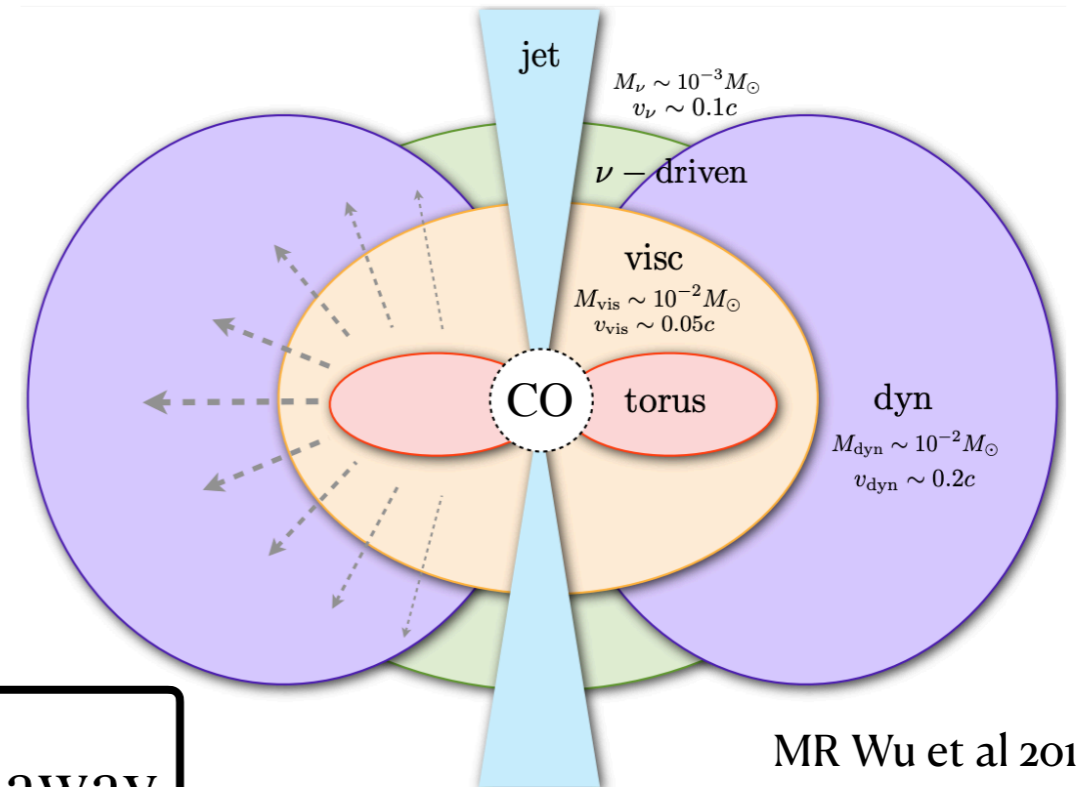
- ✓ Matter-neutrino resonances in a multi-angle framework

Are matter-neutrino resonances still relevant?

Neutrino conversion in compact binary mergers

Mergers can host:

- MSW resonant conversion, \sim km away
- Fast flavor conversion in the proximity of decoupling regions¹, \sim m away
- Matter-neutrino resonances (MNR), \sim m-km away

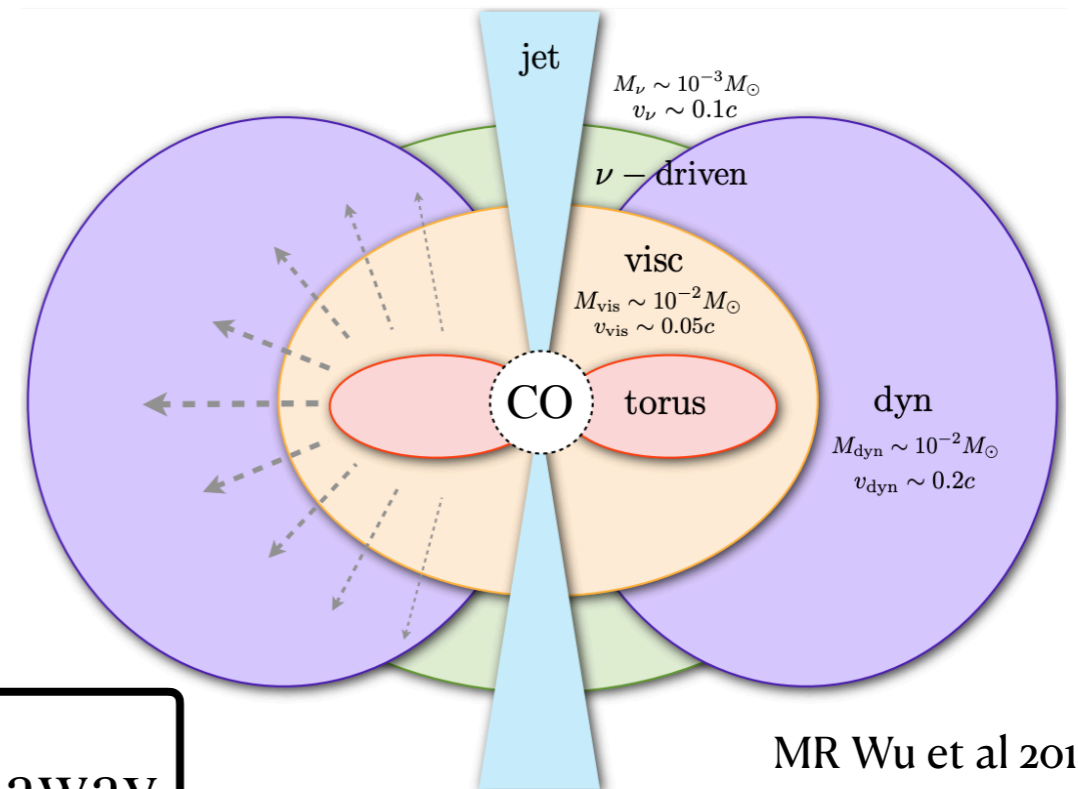


¹Multi-Dimensional Solution of Fast Neutrino Conversions in Binary Neutron Star Merger Remnants, **Padilla-Gay**, Shalgar & Tamborra, JCAP 01 (2021) 017

Neutrino conversion in compact binary mergers

Mergers can host:

- MSW resonant conversion, \sim km away
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Key ingredient: overall excess $\bar{\nu}_e > \nu_e$ in the neutrino emission^{2,3,4}

¹Multi-Dimensional Solution of Fast Neutrino Conversions in Binary Neutron Star Merger Remnants, **Padilla-Gay**, Shalgar & Tamborra, JCAP 01 (2021) 017

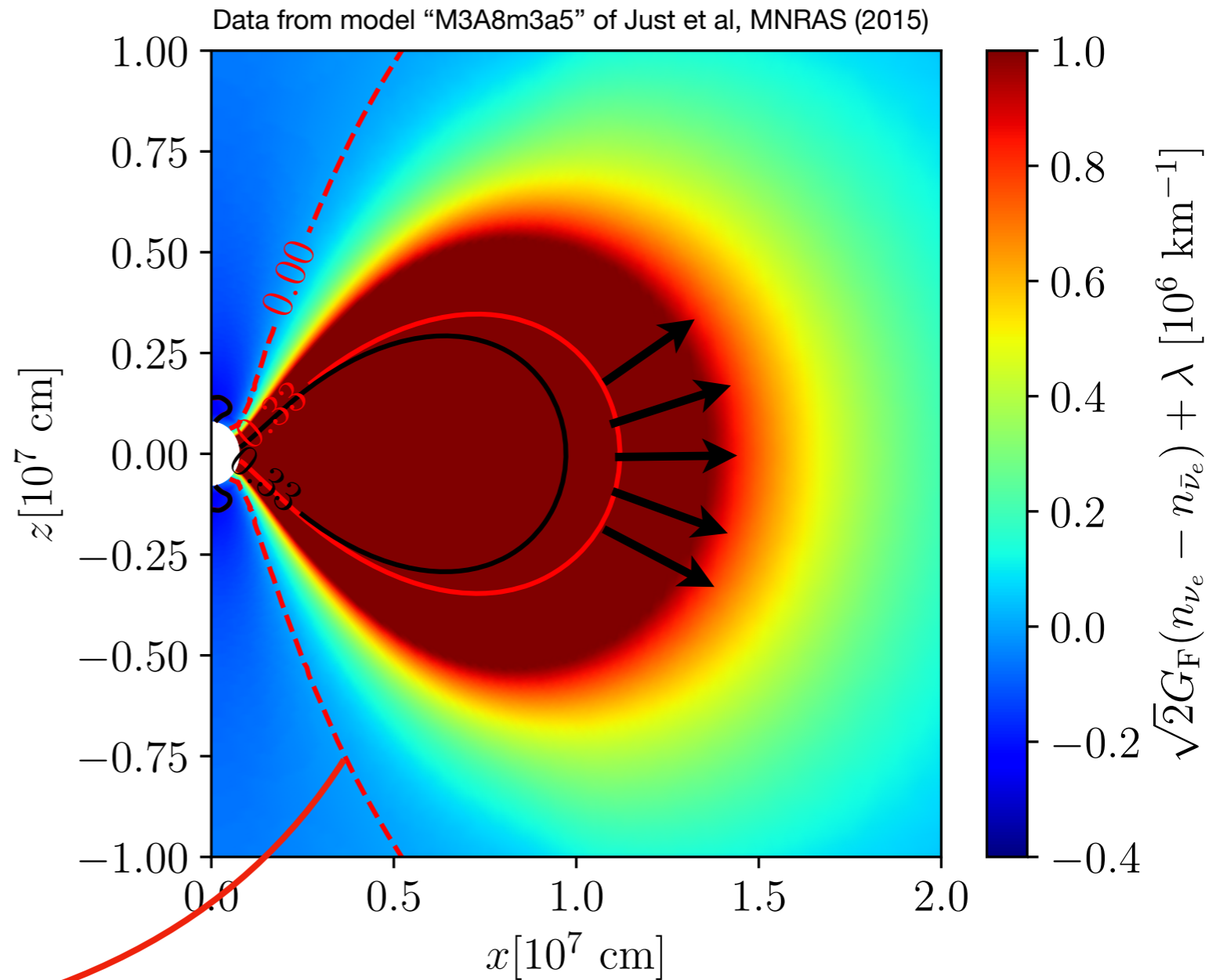
²Coalescing neutron stars, Ruffert, Janka & Takahashi, Astronomy and Astrophysics, v.319, p.122-153

³Post-merger evolution of a neutron star-black hole binary with neutrino transport, Foucart et al, Phys. Rev. D 91, 124021 (2015)

⁴Neutrino-driven winds from neutron star merger remnants, A. Perego et al, *MNRAS*, Volume 443, Issue 4, 2014

MNRs, what are they?

- The MNR is the *enhancement* of flavor conversion due to the *cancellation* of neutrino and matter Hamiltonians¹
- Conditions for MNR have been recognized in the past

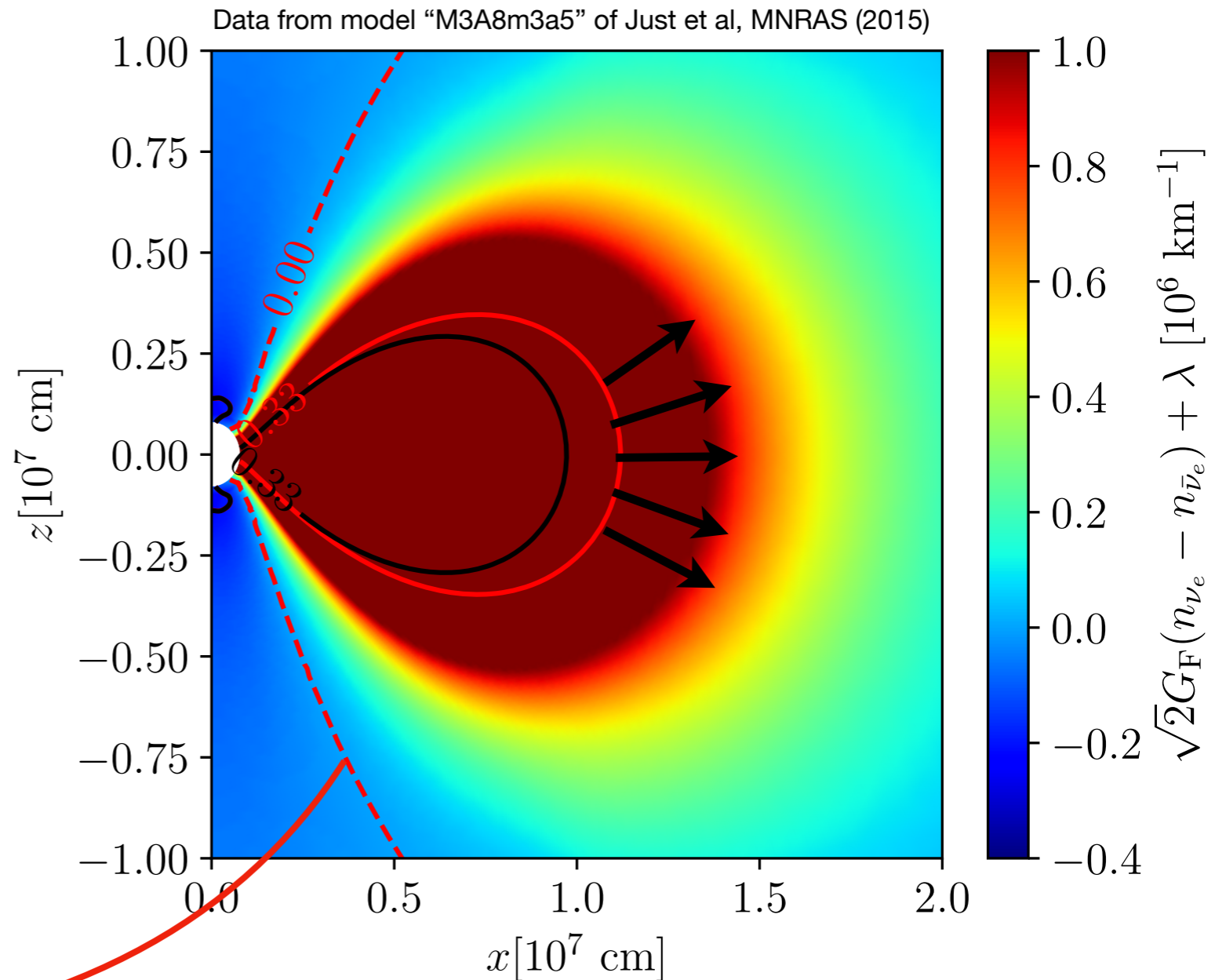


**Interesting regions for MNR
(near & far)**

¹Matter-Neutrino Resonance Above Merging Compact Objects, Malkus, Friedland & McLaughlin, 1403.5797

MNRs, what are they?

- The MNR is the *enhancement* of flavor conversion due to the *cancellation* of neutrino and matter Hamiltonians¹
- Conditions for MNR have been recognized in the past
- However, most studies assume there is no dependence on the emission angle¹⁻⁵ ...
- ...other papers assume there is^{6,7} (kind of)



**Interesting regions for MNR
(near & far)**

¹Matter-Neutrino Resonance Above Merging Compact Objects, Malkus, Friedland & McLaughlin, 1403.5797

²Uncovering the Matter-Neutrino Resonance, Vaananen & McLaughlin, Phys.Rev.D 93 (2016) 10, 105044

³Symmetric and Standard Matter-Neutrino Resonances Above Merging Compact Objects, Malkus, McLaughlin & Surman, Phys.Rev.D 93 (2016) 4, 045021

⁴Matter Neutrino Resonance Transitions above a Neutron Star Merger Remnant, Zhu, Perego & McLaughlin, Phys. Rev. D 94, 105006 (2016)

⁵Physics of neutrino flavor transformation through matter-neutrino resonances, Wu, Duan & Qian, Physics Letters B (2016), pp. 89-94

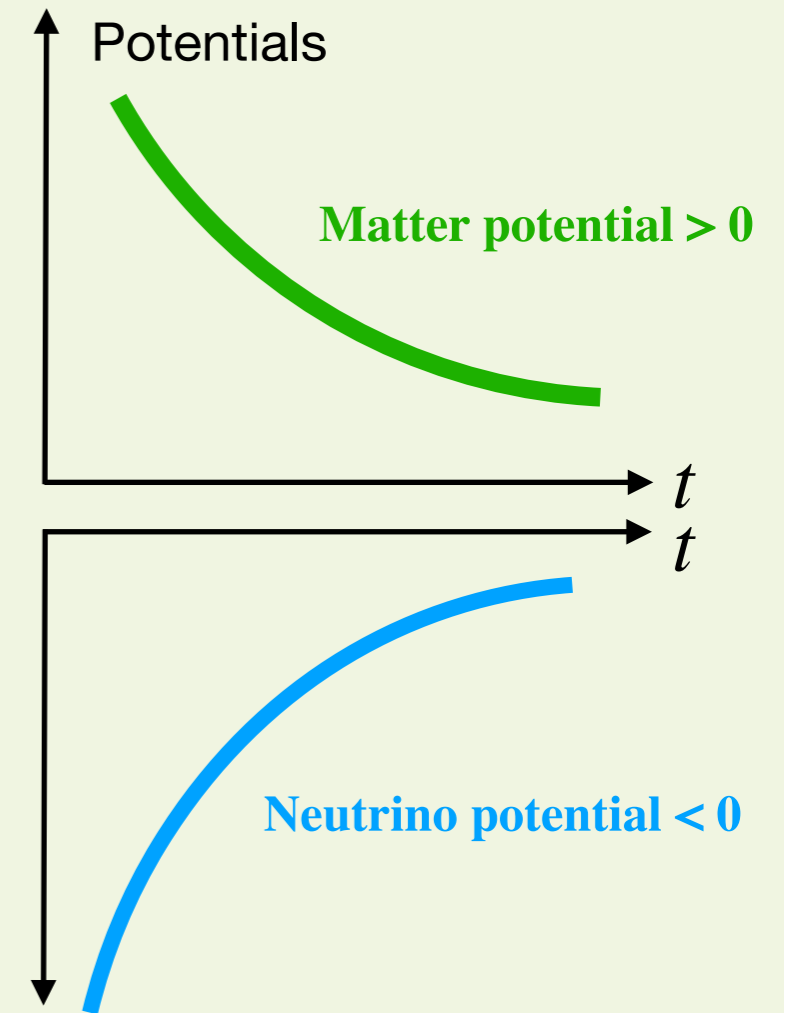
⁶Matter-neutrino resonance in a multiangle neutrino bulb model, Vlasenko, A. and McLaughlin, Phys. Rev. D 97, 083011 (2018)

⁷Multi-angle calculation of the matter-neutrino resonance near an accretion disk, Shahank Shalgar, JCAP02(2018)010

Matter-neutrino resonance: basic example

$$H_{\text{mat}} = \begin{pmatrix} \lambda & 0 \\ 0 & 0 \end{pmatrix}, \text{ where } \lambda = \frac{\sqrt{2}G_F\rho_B}{m_N}Y_e \text{ is } \textit{positive}$$

$$H_{ee}^{\nu\nu}(\nu) = \sqrt{2}G_F(n_{\nu_e} - n_{\bar{\nu}_e})^* \textit{ negative} \text{ (NS mergers)}$$

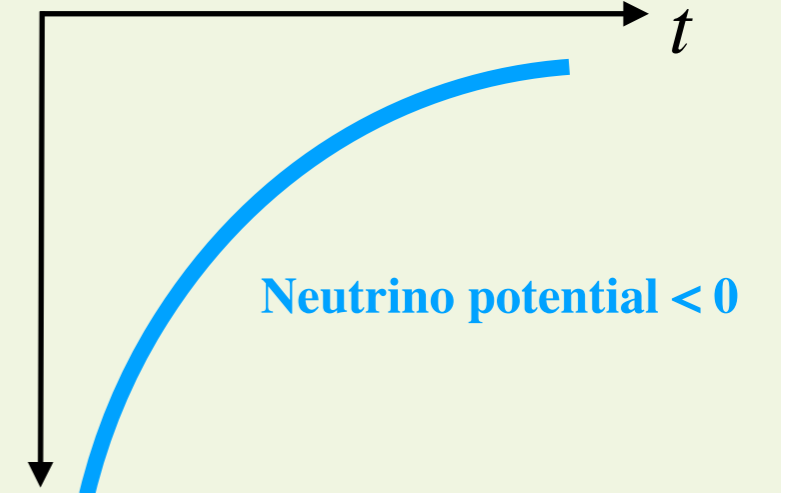
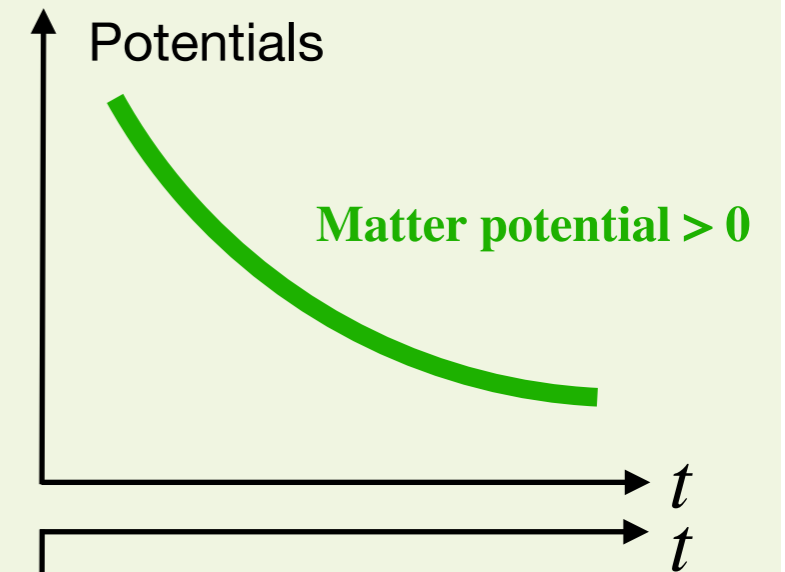


*No angular dependence → single angle approx.

Matter-neutrino resonance: basic example

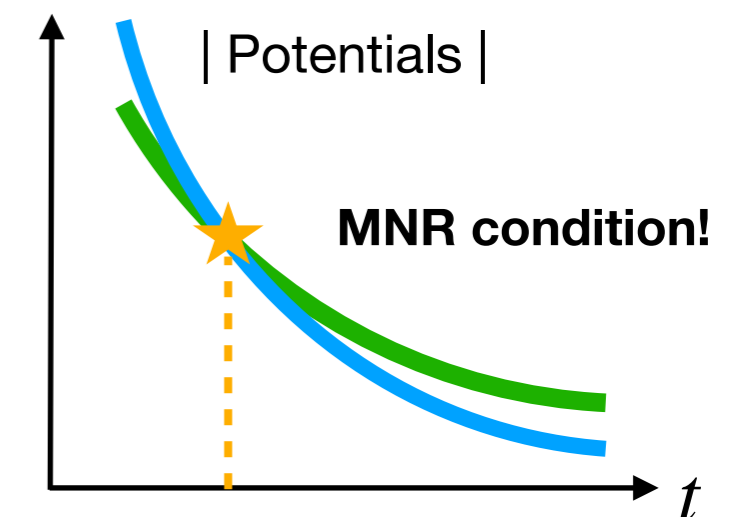
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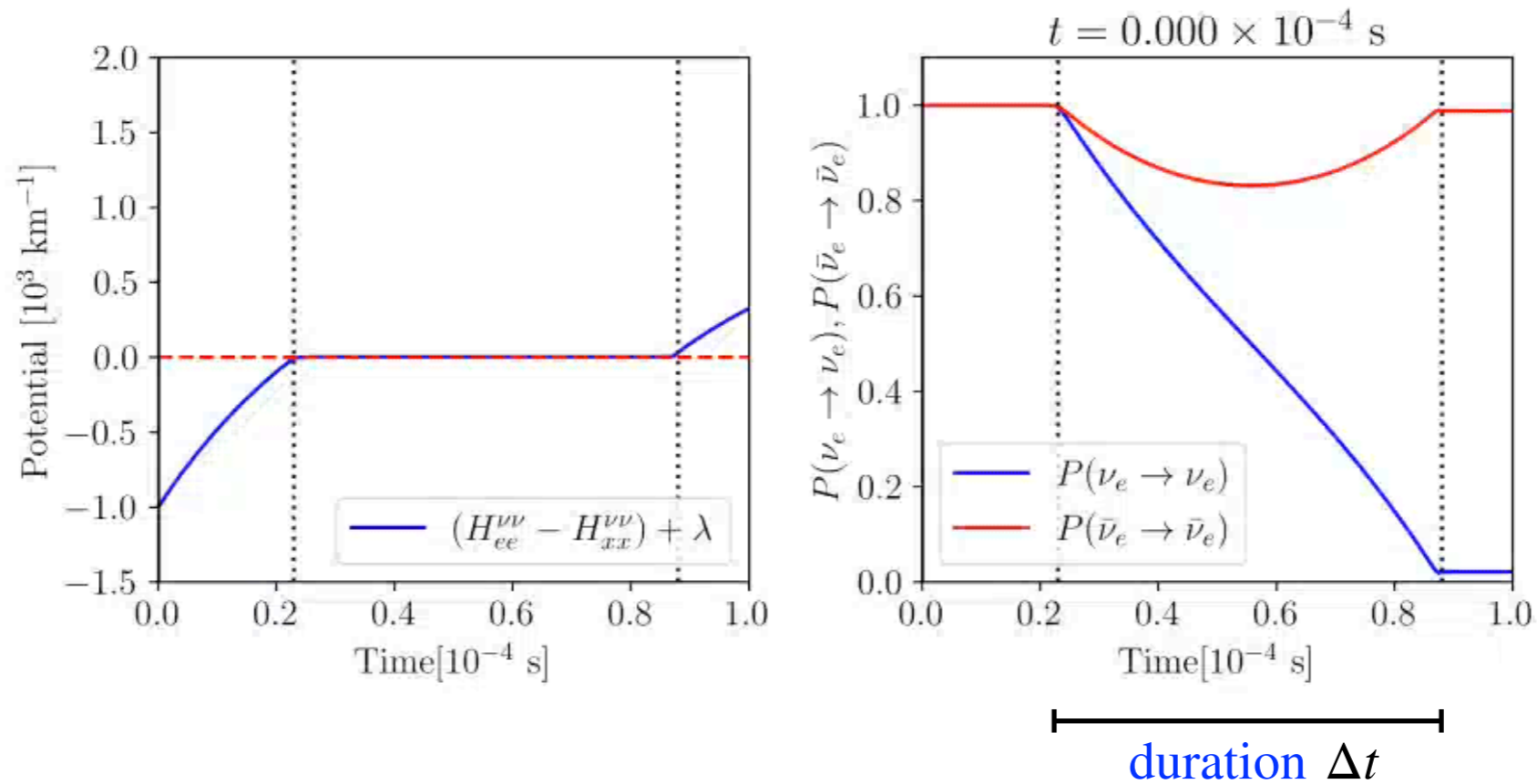
$$H_{ee}^{\nu\nu} - H_{xx}^{\nu\nu} + \lambda \approx 0$$

*No angular dependence → single angle approx.



Matter-neutrino resonance: basic example

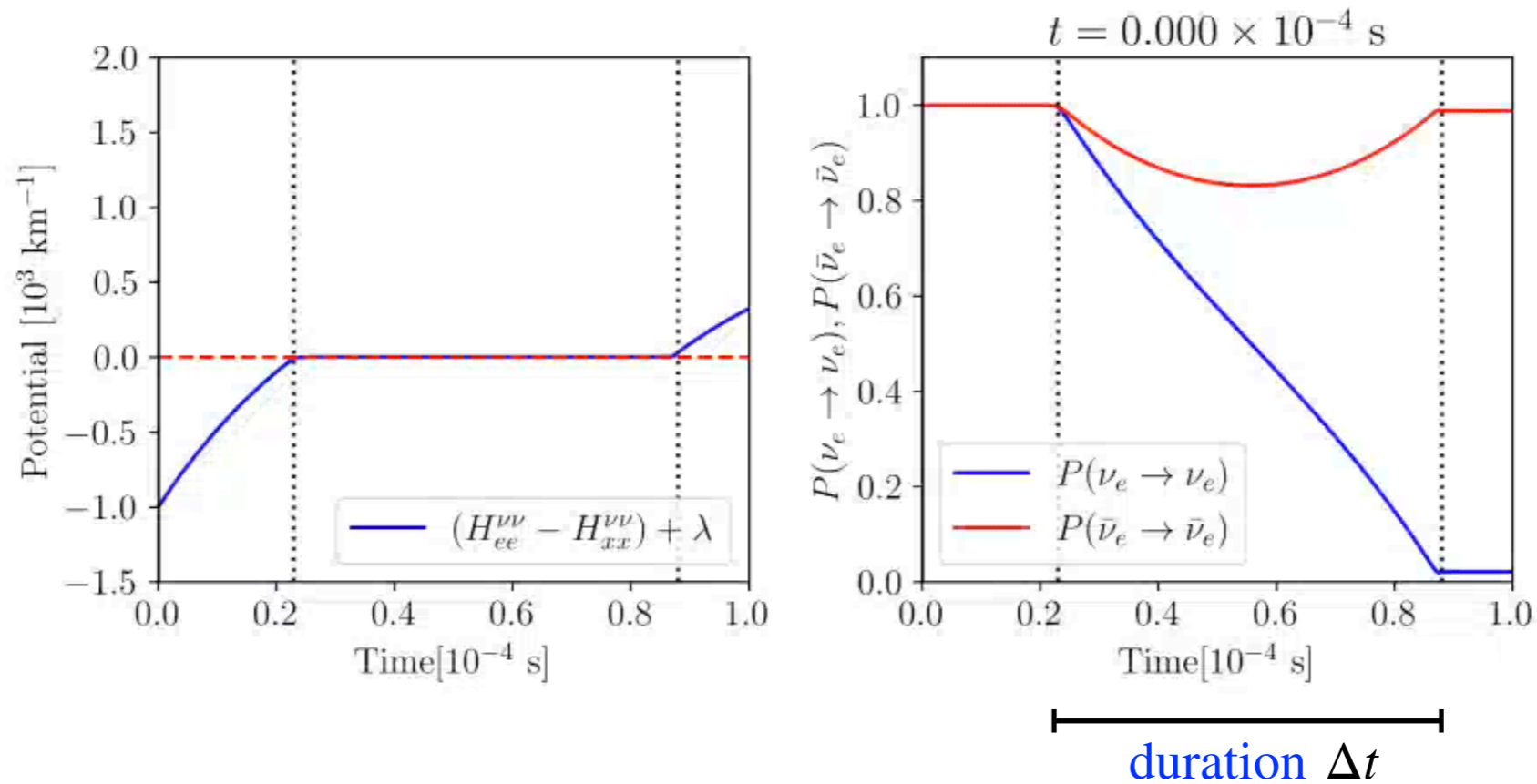
Single-angle case



- When the neutrino and matter potential cancel each other: neutrinos completely change flavor

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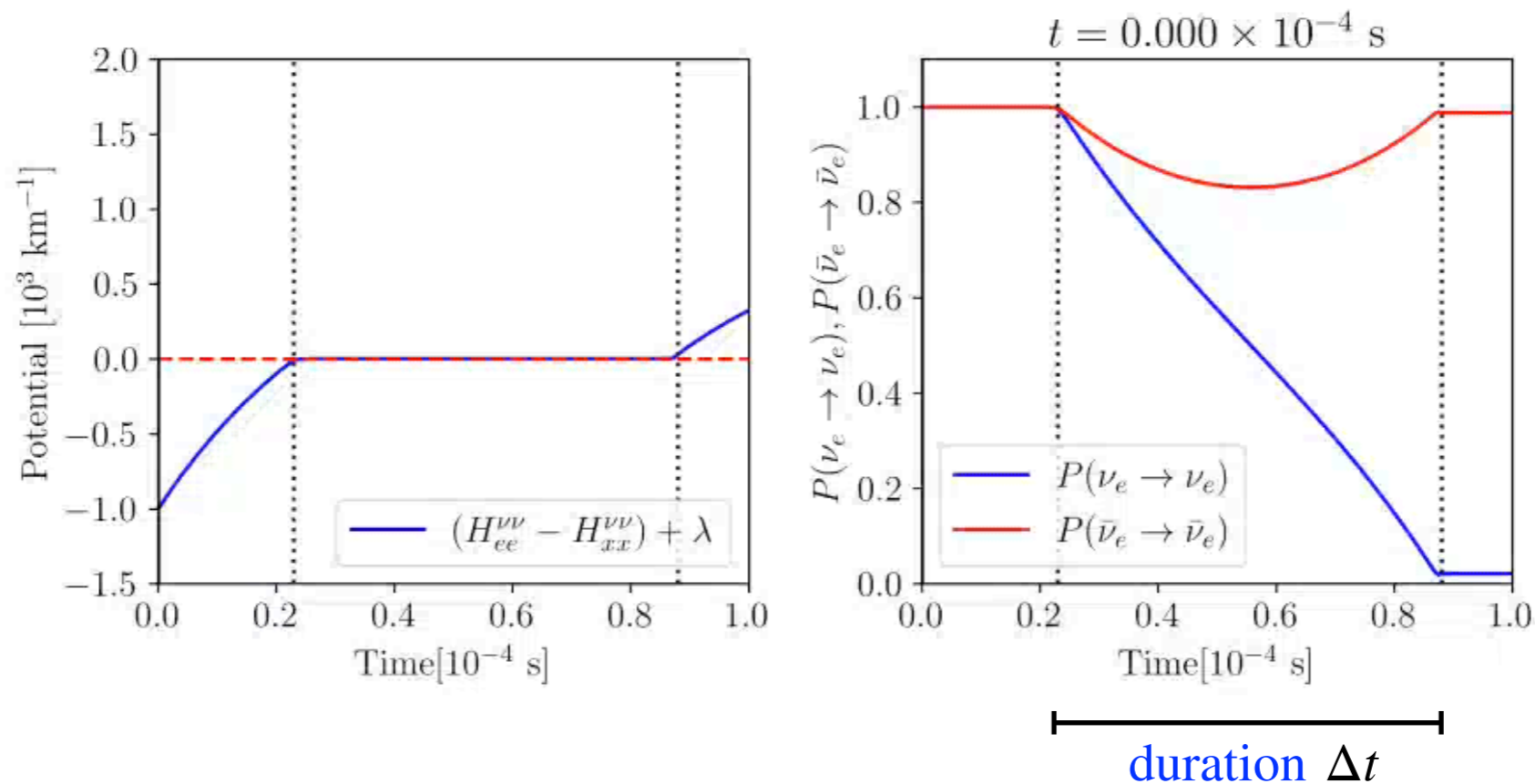
Single-angle case



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- Occurs for both mass hierarchies (unlike the MSW effect)

Matter-neutrino resonance: basic example

Single-angle case



- When the neutrino and matter potential cancel each other: neutrinos completely change flavor
- Occurs for both mass hierarchies (unlike the MSW effect)
- System stays on resonance for a period of time: **duration** $\Delta t \approx \tau_{\lambda/\mu} \log \left(\frac{1 + \alpha}{\alpha - 1} \right)$ where

$$\tau_{\lambda/\mu} = \left| \frac{d \log[\lambda(t)/\mu(t)]}{dt} \right|^{-1} \text{ is the **effective timescale** and } \alpha = n_{\bar{\nu}_e}/n_{\nu_e} \text{ the neutrino/antineutrino **asymmetry**}$$

Matter-neutrino resonance: advanced example

$$H_{\text{mat}} = \begin{pmatrix} \lambda & 0 \\ 0 & 0 \end{pmatrix}, \text{ where } \lambda = \frac{\sqrt{2}G_F\rho_B}{m_N}Y_e \text{ is } \textit{positive}$$

$$H_{\nu\nu}(\mathbf{v}) = \sqrt{2}G_F n_{\nu_e} \int d\mathbf{v}' [\rho(\mathbf{v}') - \frac{n_{\bar{\nu}_e}}{n_{\nu_e}} \bar{\rho}(\mathbf{v}')] (1 - \mathbf{v}\mathbf{v}') \textit{ negative} \text{ (NS mergers)}$$

Matter-neutrino resonance: advanced example

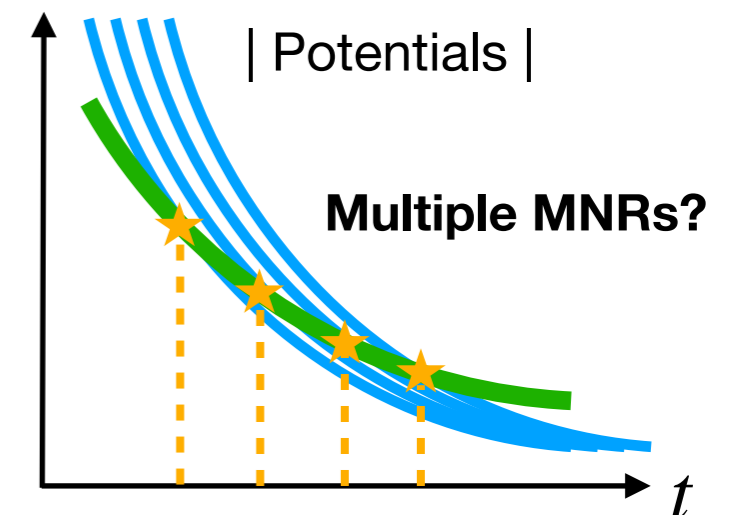
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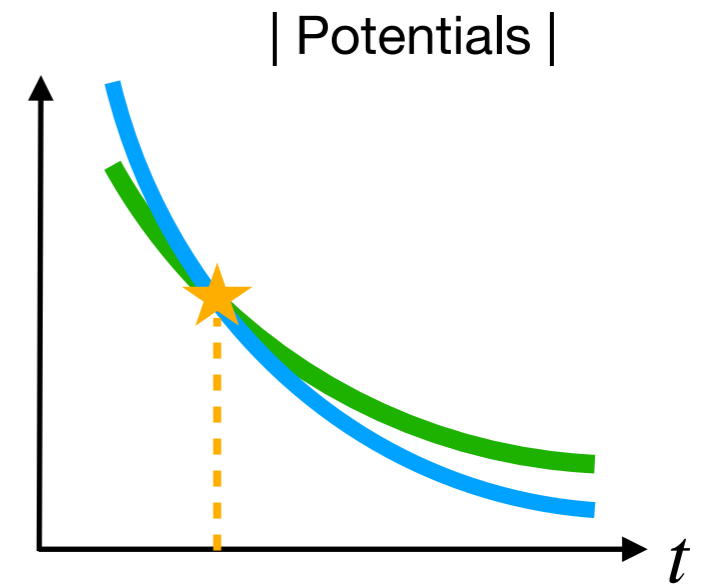
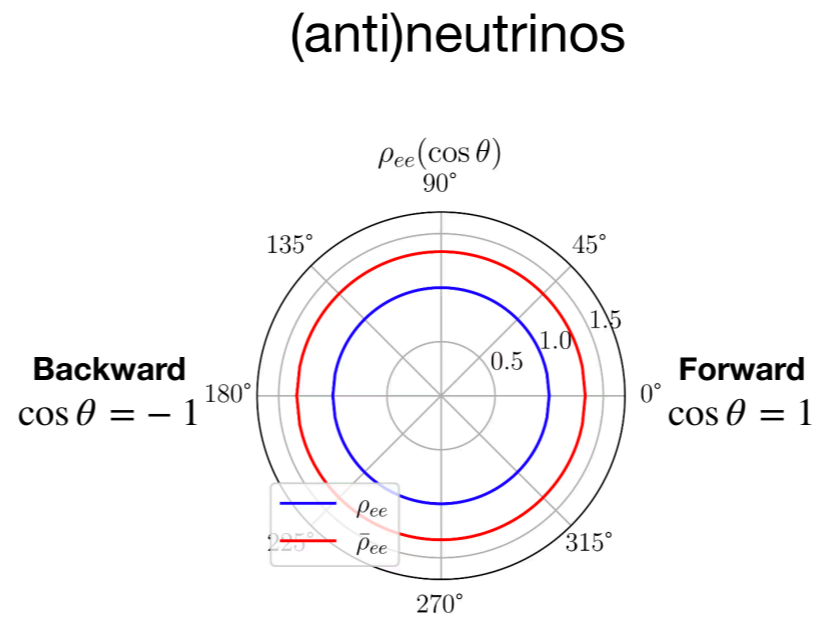
$$H_{ee}^{\nu\nu}(\mathbf{v}) - H_{xx}^{\nu\nu}(\mathbf{v}) + \lambda \approx 0$$

Cancellation does not occur at the same location for different emission angles!



Three interesting cases

1) **Isotropic** neutrino distributions
(recovers the single-angle approx.)

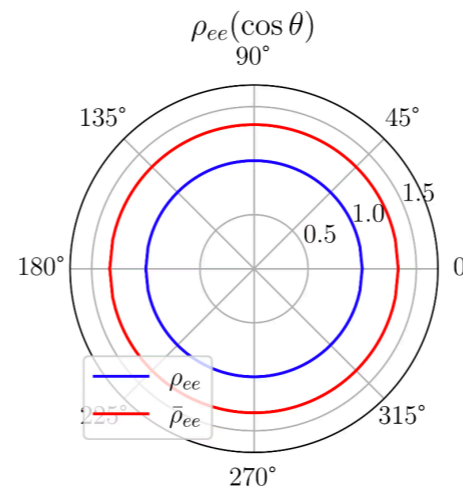
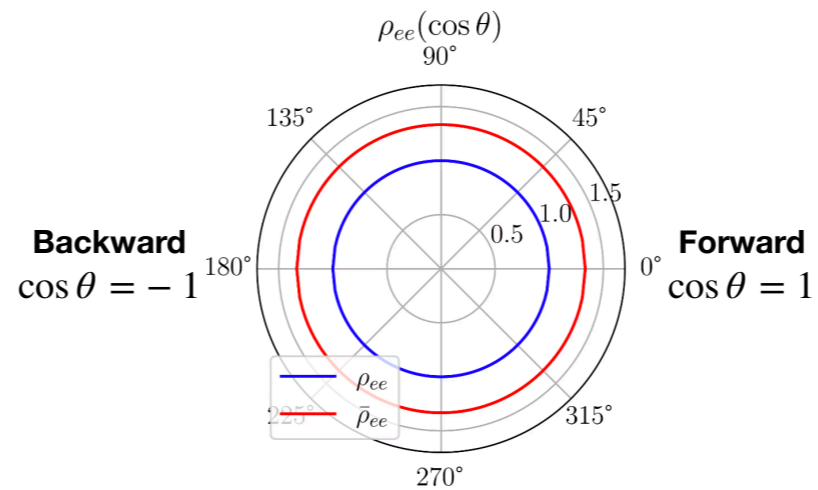


Three interesting cases

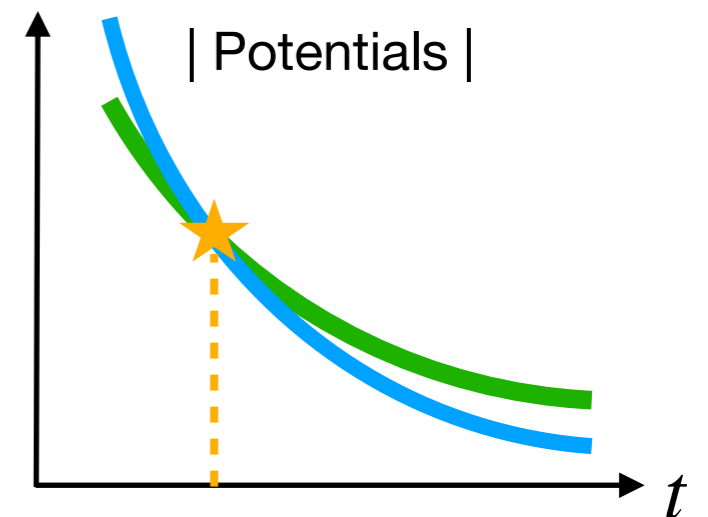
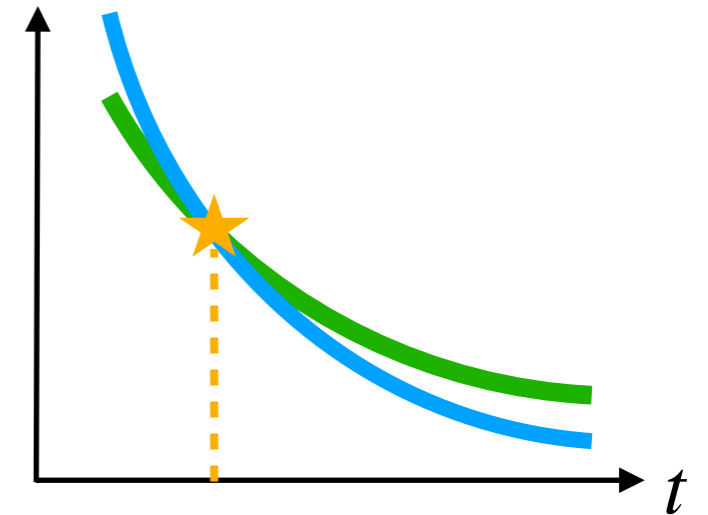
1) **Isotropic** neutrino distributions
(recovers the single-angle approx.)

2) **Isotropic**, but with a very tiny
(10^{-22}) anisotropy. Much larger
perturbations arise naturally in the
medium

(anti)neutrinos



| Potentials |



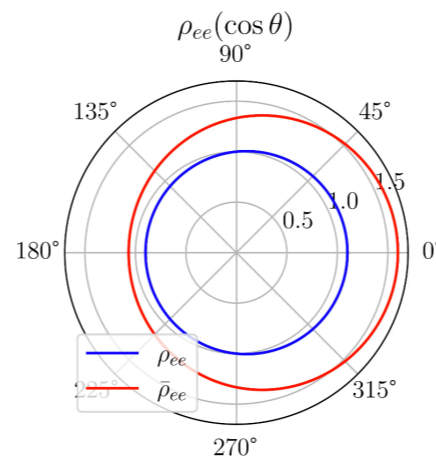
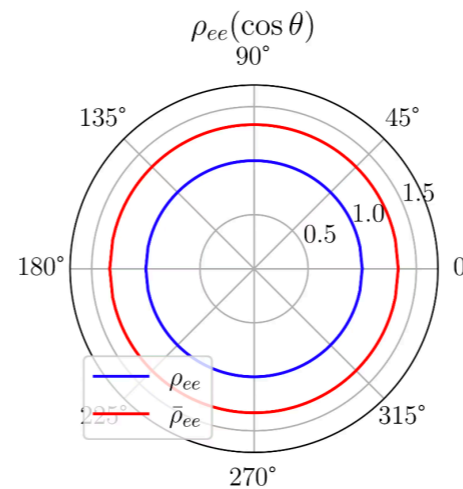
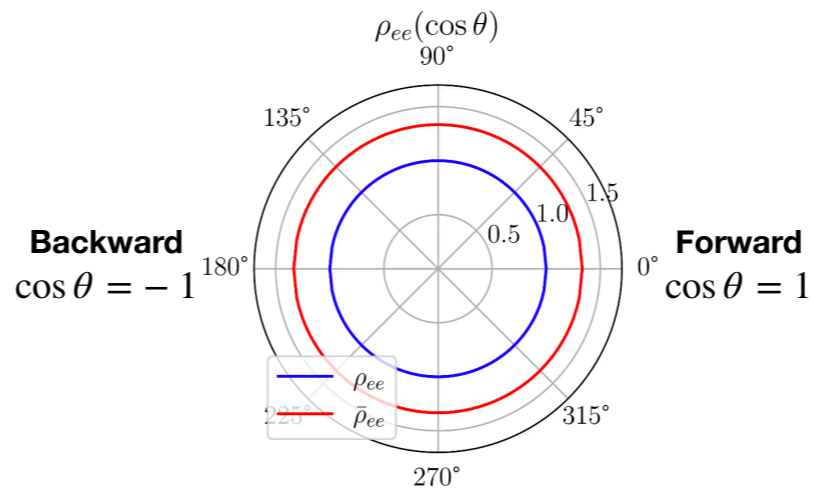
Three interesting cases

1) **Isotropic** neutrino distributions
(recovers the single-angle approx.)

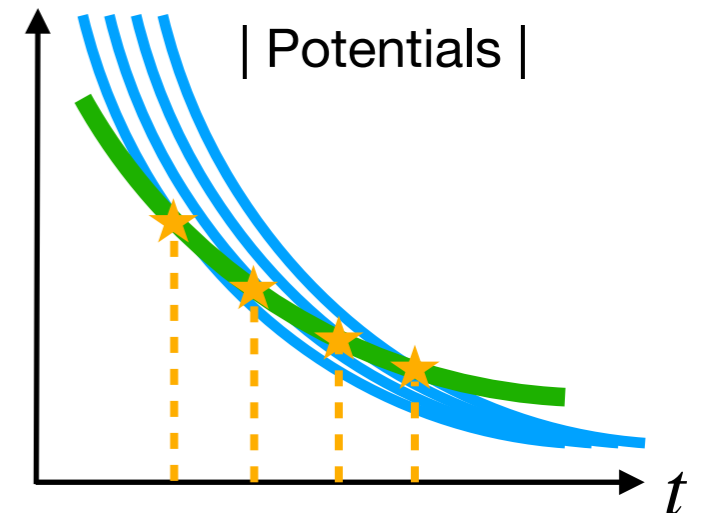
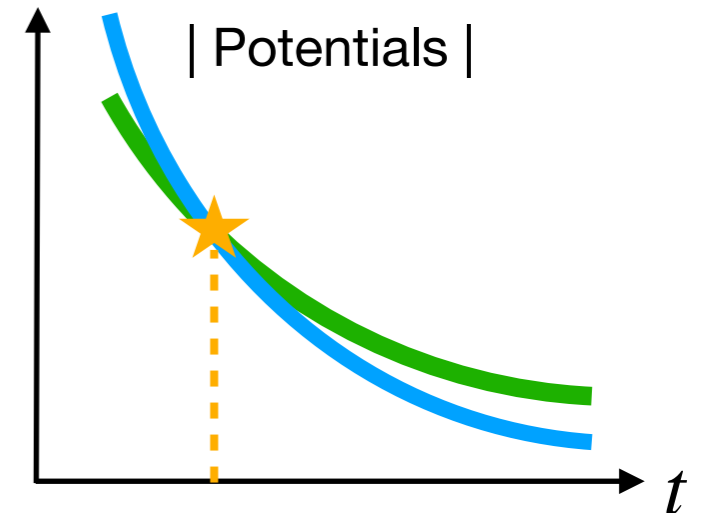
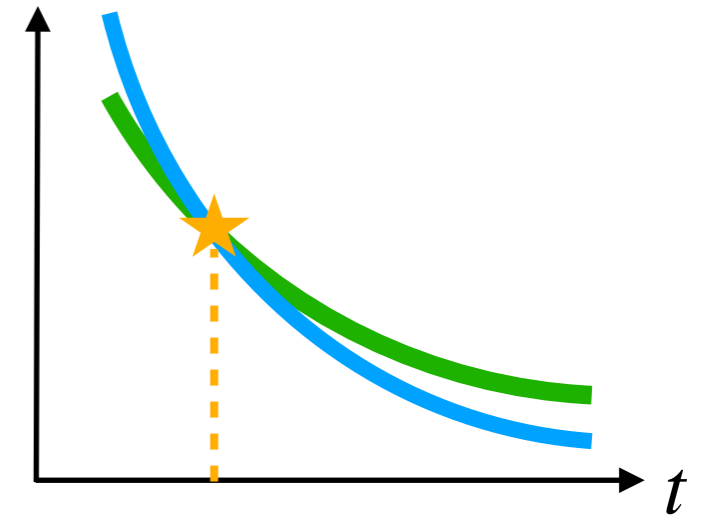
2) **Isotropic**, but with a very tiny
(10^{-22}) anisotropy. Much larger
perturbations arise naturally in the
medium

3) **Non-isotropic** neutrino
distributions. To be expected in
realistic astrophysical
environments

(anti)neutrinos

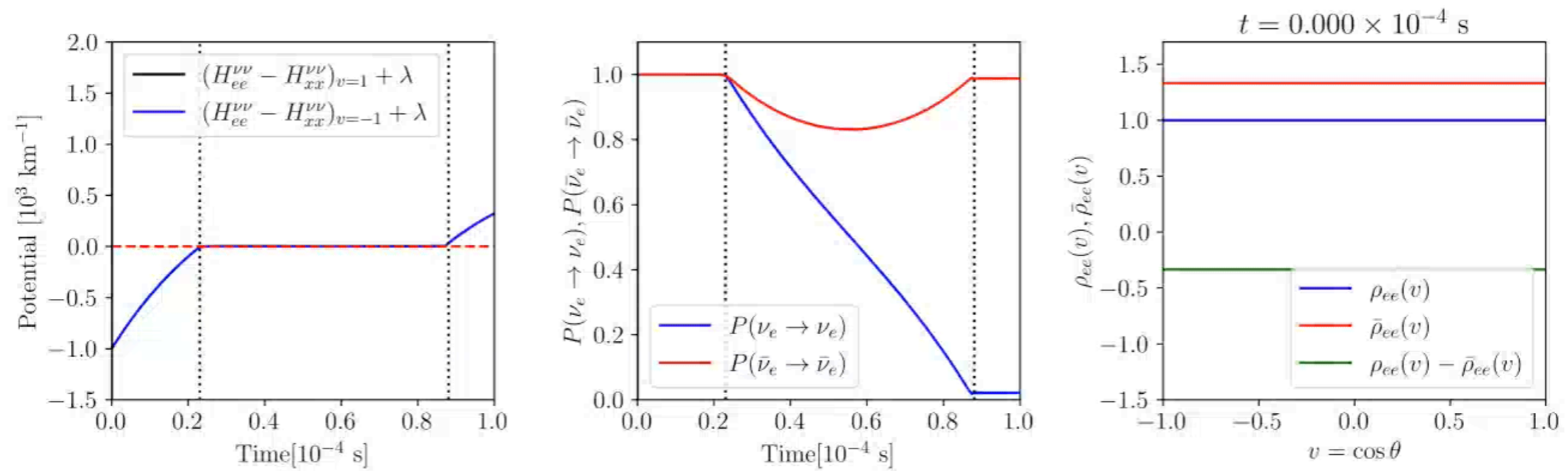


| Potentials |

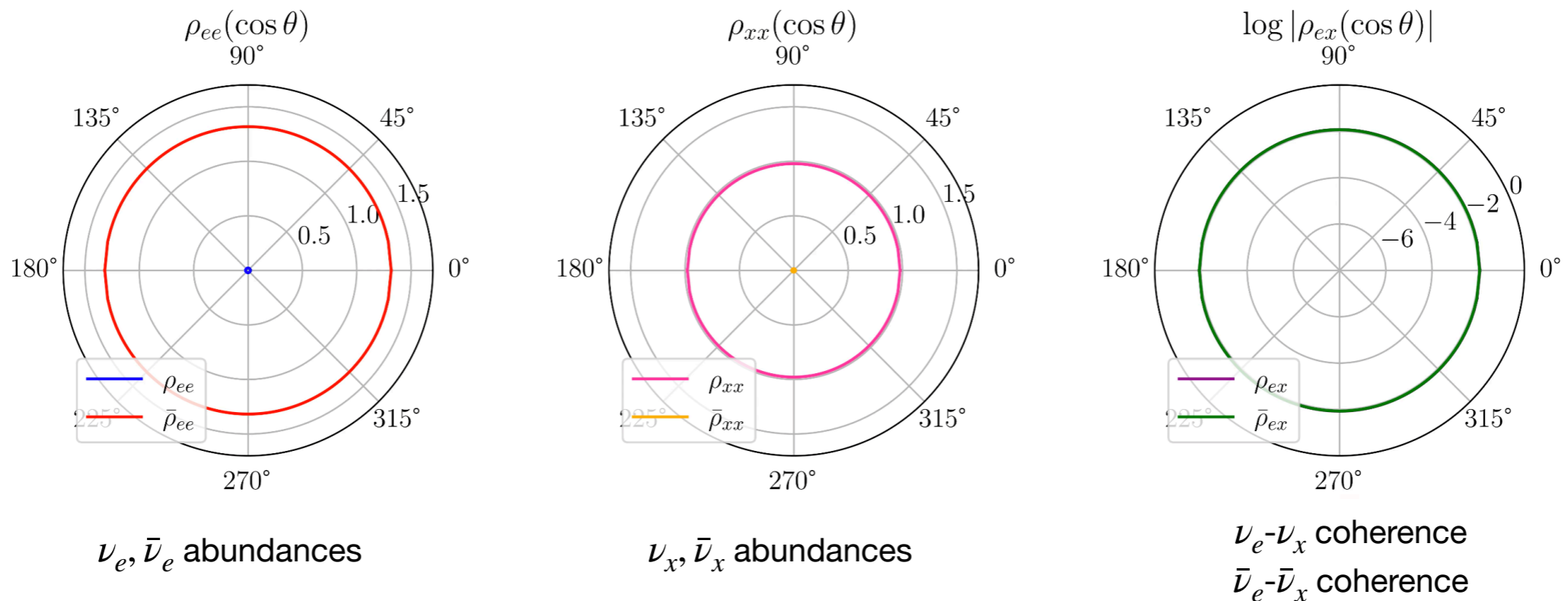


1) Perfectly isotropic distribution. Single-angle approximation recovered

Multi-angle: isotropic case without perturbation

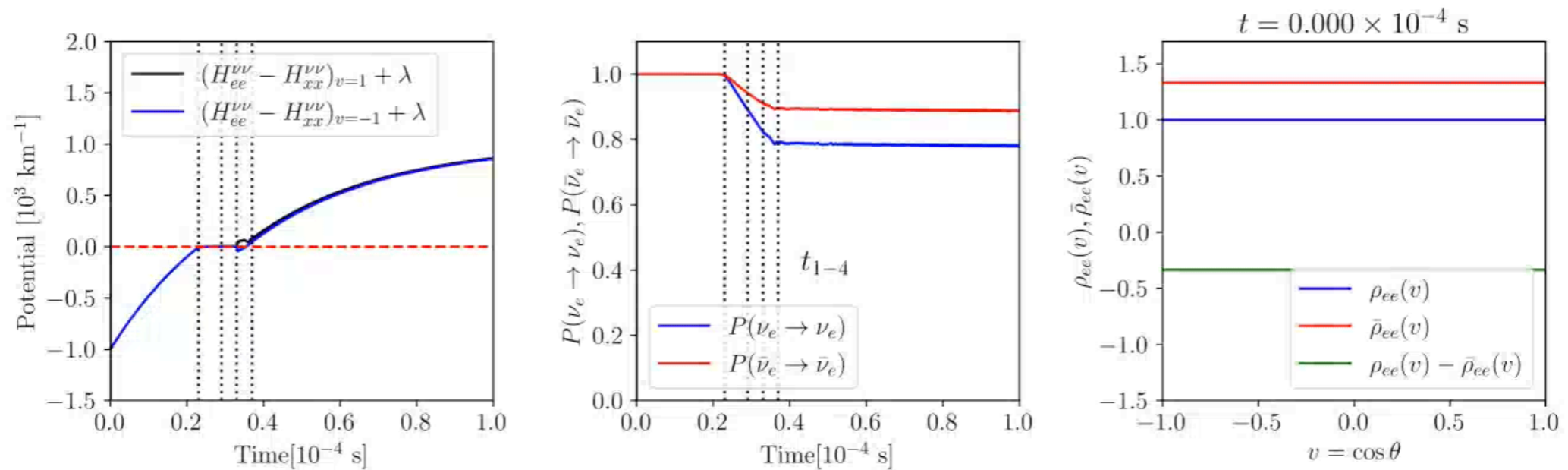


Multi-angle: isotropic case without perturbation at $t = 1.000 \times 10^{-4} \text{ s}$

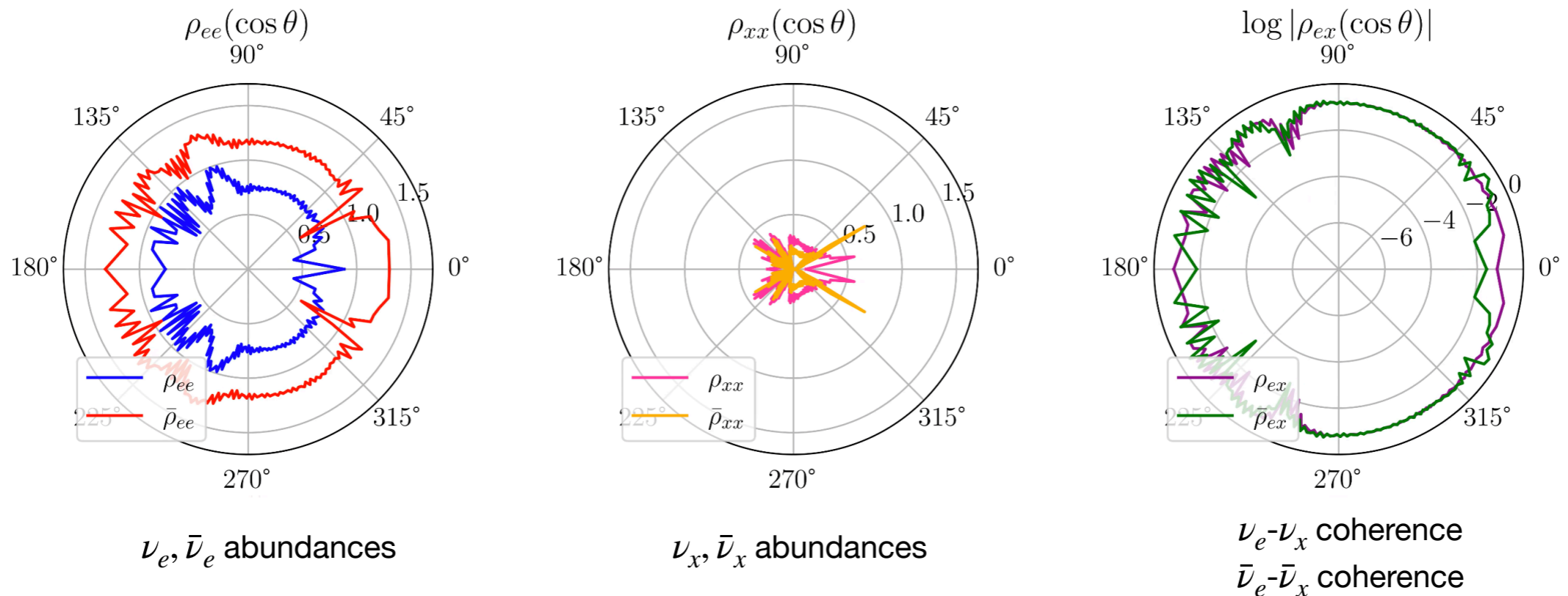


2) Isotropic distribution with a $\sim 10^{-22}$ perturbation. Dipole mode grows exponentially. Isotropy is dynamically broken

Multi-angle: isotropic case with perturbation

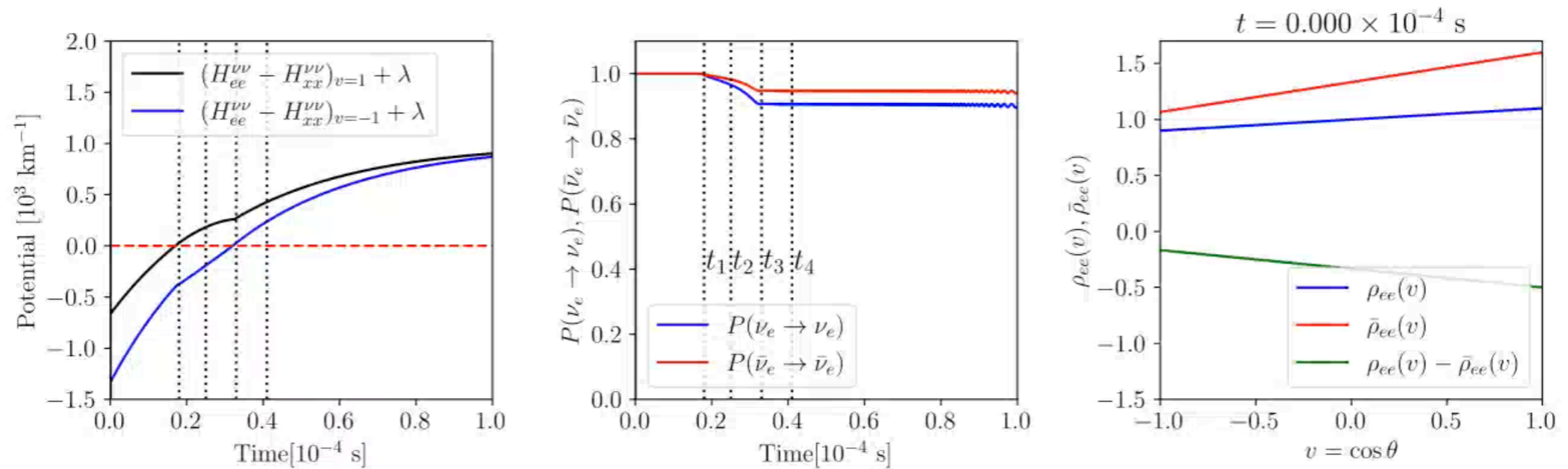


Multi-angle: isotropic case with perturbation at $t = 0.989 \times 10^{-4} \text{ s}$

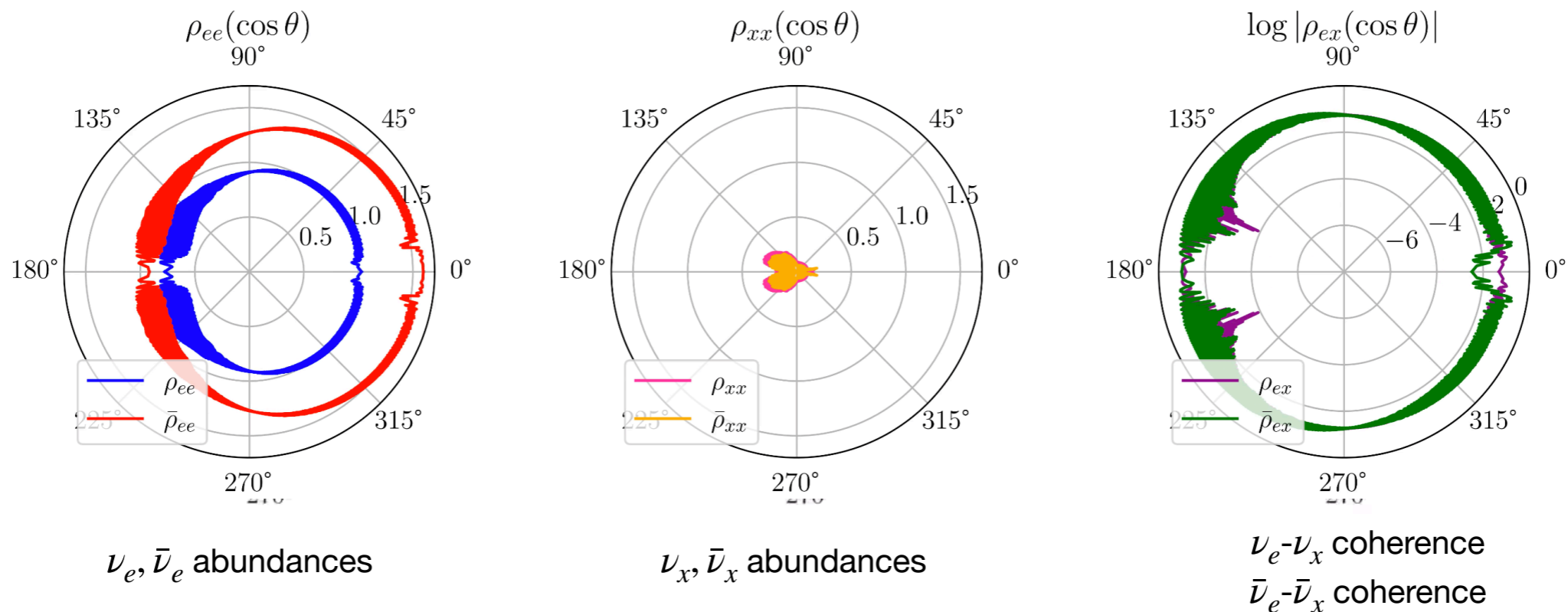


3) Non-isotropic distribution relevant for astrophysical systems. MNR not sustained, different directions interfere

Multi-angle: non-isotropic case



Multi-angle: non-isotropic case at $t = 0.993 \times 10^{-4} \text{ s}$



Part III

Conclusions

Conclusions

- Neutrino flavor evolution in dense astrophysical environments is **very complex** (sensitive to very small variations)
- Non-trivial role of neutrino-neutrino interaction in the equations of motion; **angle-dependence** is hard
- If MNR's occur in NS remnants, they will most likely be **interrupted** by emerging anisotropies
- Implications for **realistic** astrophysical sources remain to be understood

